Lecture 39 outline:

11/18/2020

- Magnetic fields and work
- Questions!
- Differential form of Ampere's Law
- Symettry between Faraday and Ampere
- Faraday's Law / Demo

Ch 5 Questions:

Magnets snap together. How can you say B does no work? (Edelman)

- Magnetic forces change particle's direction, how can this not do work? $\vec{F} = q\vec{E} + q\vec{v} \times \vec{B}$
- What's going on on p 218?

Ch 7 Questions:

• Why is it called EMF?

Maxwell's Equations

$$\iint \vec{E} \cdot d\vec{a} = \frac{Q}{\epsilon_0}$$

$$\nabla \cdot \vec{E} = \frac{\rho}{\epsilon_0}$$

The "no monopole"
$$\iint \vec{B} \cdot d\vec{a} = \mu_0 Q_{monopole} = 0$$

$$\nabla \cdot \vec{\mathbf{B}} = 0$$

Ampere's Law

$$\oint \vec{B} \cdot dl = \mu_0 I$$

$$\nabla \times \vec{B} = \mu_0 \vec{J}$$

$$\varepsilon = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

$$\nabla \times \vec{\mathbf{E}} = -\frac{\partial \vec{\mathbf{B}}}{\partial t}$$

Ampere's Law
Integral to
Differential form

$$\begin{split} &\oint \vec{B} \cdot d \vec{l} = \mu_0 I \\ &\oint \vec{B} \cdot d \vec{l} = \mu_0 \int \vec{J} \cdot d \vec{a} \\ &\int \nabla \times \vec{B} \cdot d \vec{a} = \mu_0 \int \vec{J} \cdot d \vec{a} \\ &\nabla \times \vec{B} = \mu_0 \vec{J} \end{split}$$

Ampere's Law

Faraday's Law

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 I$$

$$\oint \vec{B} \cdot d \vec{l} = \mu_0 \int \vec{J} \cdot d \vec{a}$$

$$\int \nabla \times \vec{B} \cdot d\vec{a} = \mu_0 \int \vec{J} \cdot d\vec{a}$$

$$\nabla \times \vec{B} = \mu_0 \vec{J}$$

$$\oint \vec{E} \cdot d \vec{l} = -\frac{\partial}{\partial t} \Phi_B$$

$$\oint \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\int \nabla \times \vec{E} \cdot d\vec{a} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

Faraday's Law

$$\epsilon = -\frac{\partial}{\partial t} \Phi_{B} \stackrel{\oint}{\rightarrow} \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \Phi_{B}$$

$$\epsilon = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a} \stackrel{\oint}{\rightarrow} \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\int \nabla \times \vec{E} \cdot d\vec{a} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$

Faraday's Law:

- You get a current in a loop IF
- B changes magnitude
- Loop area changes
- Angle between B and area changes

Lenz's Law "Back EMF":

• Lenz's law is the minus sign in Faraday's law

• If you try to increase B through a loop, a current in the loop tries to prevent it from increasing

Example 1: Increase B

Example 2: Increase A

Example 3: Change angle between B and A

Ampere's Law

Faraday's Law

(with displacement current)

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 \epsilon_0 \frac{\partial}{\partial t} \Phi_E$$

$$\oint \vec{E} \cdot d\vec{l} = -\frac{\partial}{\partial t} \Phi_B$$

$$\oint \vec{B} \cdot d\vec{l} = \mu_0 \epsilon_0 \frac{\partial}{\partial t} \int \vec{E} \cdot d\vec{a}$$

$$\oint \vec{E} \cdot d \vec{l} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d \vec{a}$$

$$\int \nabla \times \vec{B} \cdot d\vec{a} = \mu_0 \, \varepsilon_0 \frac{\partial}{\partial t} \int \vec{E} \cdot d\vec{a} \, \int \nabla \times \vec{E} \cdot d\vec{a} = -\frac{\partial}{\partial t} \int \vec{B} \cdot d\vec{a}$$

$$\nabla \times \vec{B} = \mu_0 \epsilon_0 \frac{\partial \vec{E}}{\partial t}$$

$$\nabla \times \vec{E} = -\frac{\partial \vec{B}}{\partial t}$$