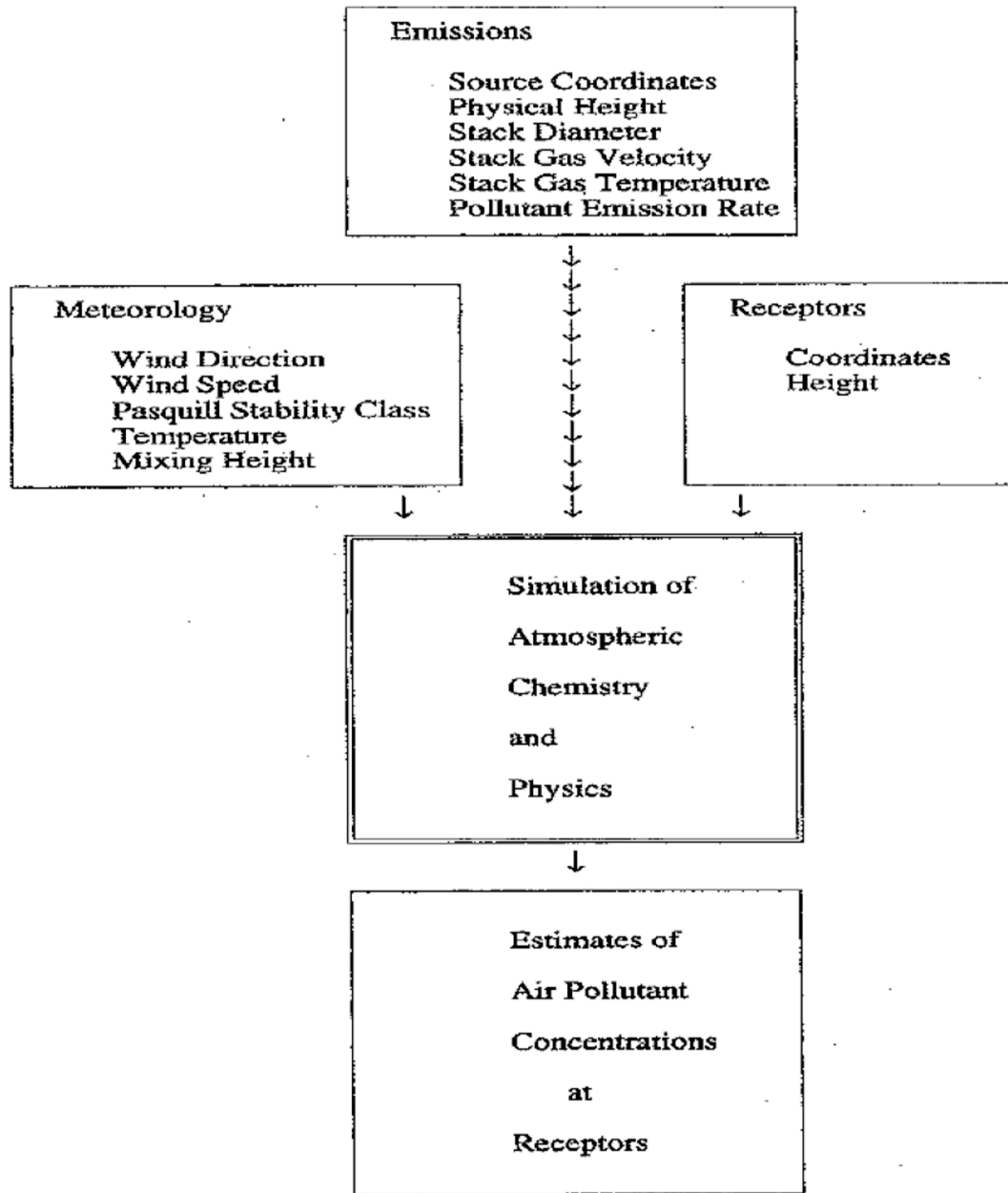
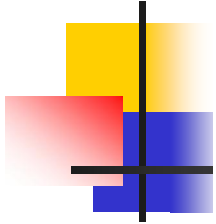




Comparison of Gaussian and Lagrangian dispersion model

Mentor: Prof. Koracin, DRI, Reno, Nevada
Thanks to the student Jerrold McAlpine for Edu-plume toy model
Student: Tamara Hunjak

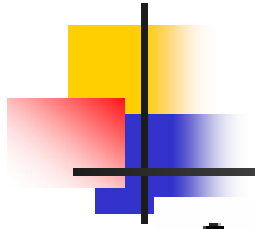
SWAP, BRA , 2010





Gaussian model

- Assumptions in Gaussian modeling
 - Continuous emission
 - Conservation of mass
 - Steady-state conditions
 - Crosswind and vertical concentration distributions

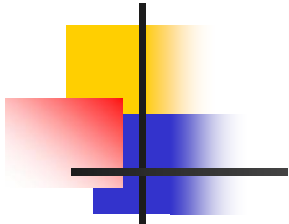


- **Continuous Emissions**

The emissions of pollutant in mass per time are taking place continuously and the rate of these emissions are not variable over time.

- **Conservation of Mass**

During the transport of pollutants from source to receptor, the mass that is emitted from the source is assumed to remain in the atmosphere. None of the material is removed through chemical reaction nor is lost at the ground surface through reaction, gravitational settling, or turbulent impaction. It is assumed that any of the released pollutant that is dispersed close to the ground surface by turbulent eddies is again dispersed away from the ground surface by other subsequent turbulent eddies. This is called eddy reflection.



- **Steady-State Conditions**

The meteorological conditions are assumed to persist unchanged with time, at least over the time period of transport (travel time) from source to receptor. It is very easy to satisfy this assumption for close in receptors under usual conditions. However, for light wind conditions or receptors at great distances, this assumption may not be satisfied.

- **Crosswind and Vertical Concentration Distributions**

It is assumed that the time averaged (over about one hour) concentration profiles at any distance in the crosswind direction, horizontal (perpendicular to the path of transport) are well represented by a Gaussian, or normal, distribution and, similarly, concentration profiles in the vertical direction (also perpendicular to the path of transport) are also well represented by a Gaussian, or normal, distribution.

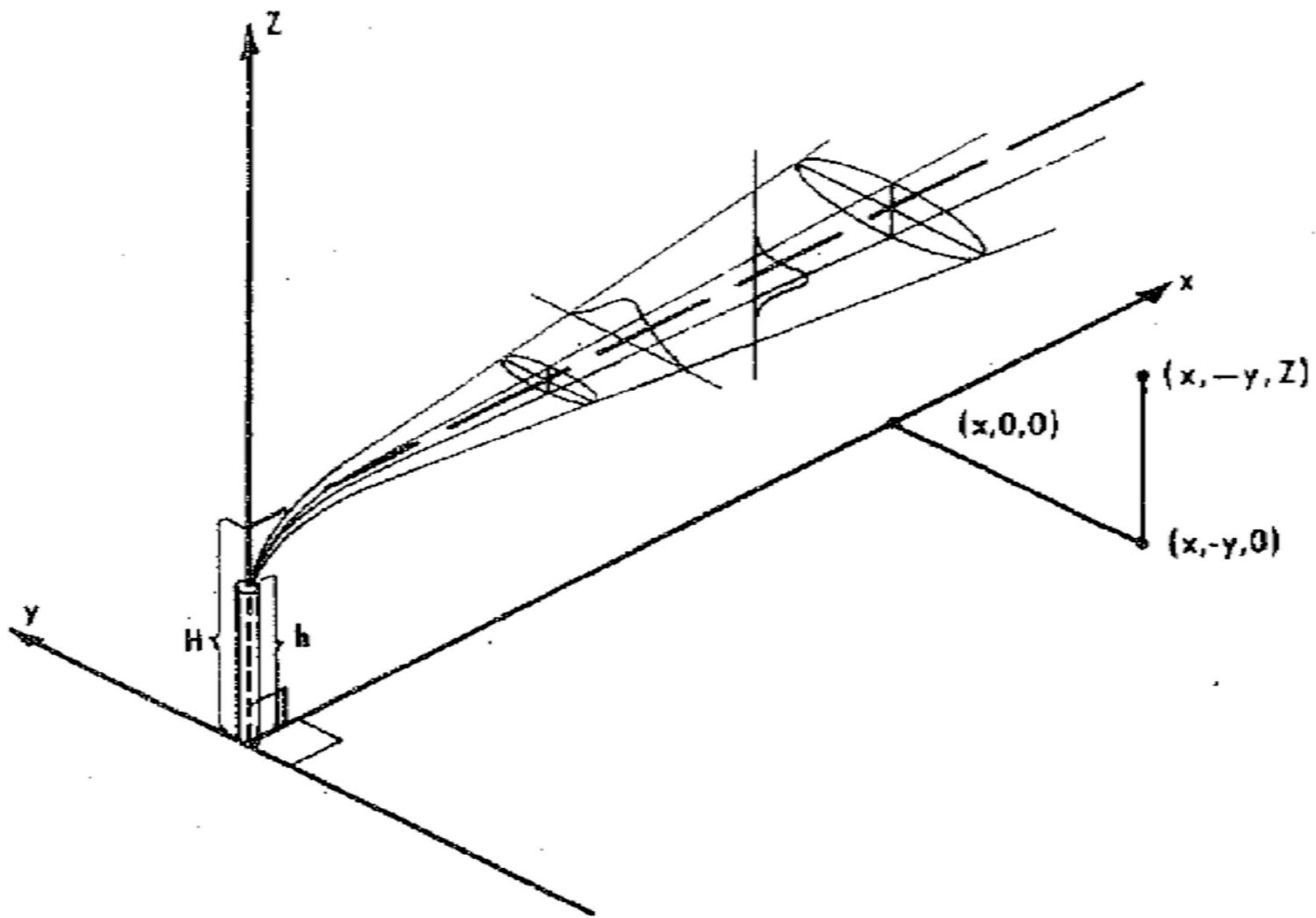


Figure 2.2 Coordinate system showing Gaussian distributions in the horizontal and vertical.



The variables are:

χ	Air pollutant concentration in mass per volume, usually g m^{-3} .
Q	Pollutant emission rate in mass per time, usually g s^{-1} .
u	Wind speed at the point of release, m s^{-1} .
σ_y	The standard deviation of the concentration distribution in the crosswind direction, m, at the downwind distance x .
σ_z	The standard deviation of the concentration distribution in the vertical direction, m, at the downwind distance x .
π	The mathematical constant pi equal to 3.1415926... .
H	The effective height of the centerline of the pollutant plume.

$$\chi(x,y,z;H) =$$

Emissions factor

Q

Downwind factor

$\frac{1}{u}$

Crosswind factor

$$\frac{1}{(2\pi)^{1/2} \sigma_y} \exp\left[-\frac{y^2}{2\sigma_y^2}\right]$$

Vertical factor

$$\frac{1}{(2\pi)^{1/2} \sigma_z} \left\{ \exp\left[-\frac{(H-z)^2}{2\sigma_z^2}\right] + \exp\left[-\frac{(H+z)^2}{2\sigma_z^2}\right] \right\}$$

Pasquill stability categories

Surface wind speed (at 10 m) m s^{-1}	Insolation			Night	
	Strong	Moderate	Slight	Thinly overcast or > 4/8 low cloud	< 3/8 cloud
< 2	A	A - B	B	—	—
2 - 3	A - B	B	C	E	F
3 - 5	B	B - C	D	D	E
5 - 6	C	C - D	D	D	D
> 6	C	D	D	D	D



Lagrangian particle dispersion model (LAP)

- The main concept of LAP
- The particles are released at the time t at prescribed rate and their new position is determined at time $(t+\Delta t)$ by relations:

$$x(t + \Delta t) = x(t) + [u(t) + u_r(t)]\Delta t$$

$$y(t + \Delta t) = y(t) + [v(t) + v_r(t)]\Delta t$$

$$z(t + \Delta t) = z(t) + [w(t) + w_r(t)]\Delta t$$



Where u_r , v_r and w_r are the corresponding subgrid-scale velocity components.

The subgrid-scale velocity components are iteratively determined as:

$$u_r(t) = u_r(t - \Delta t)R_u(\Delta t) + u_s(t - \Delta t)$$

$$v_r(t) = v_r(t - \Delta t)R_v(\Delta t) + v_s(t - \Delta t)$$

$$w_r(t) = w_r(t - \Delta t)R_w(\Delta t) + w_s(t - \Delta t)$$

where R_u , R_v , and R_w are the Lagrangian autocorrelation functions for each velocity component, and u_s , v_s , and w_s are the random fluctuations of the velocity components.



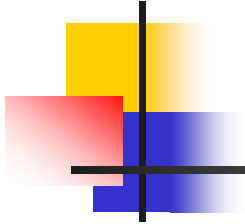
The Lagrangian correlation functions are calculated from:

$$R_u(\Delta t) = e^{-\Delta t/T_{Lu}}$$

$$R_v(\Delta t) = e^{-\Delta t/T_{Lv}}$$


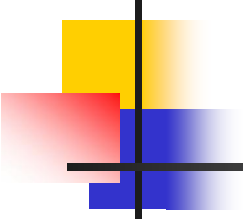
$$R_w(\Delta t) = e^{-\Delta t/T_{Lw}}$$

where T_{Lu} , T_{Lv} and T_{Lw} are the Lagrangian time scales for the corresponding velocity components.



After that the calculations of the Lagrangian time scale, the autocorrelation functions, and the range of velocity fluctuations as Gaussian standard deviations from a mean, are determined.


For each particle a random velocity fluctuation is generated and used to calculate the new particle velocity, and then the new particle position is calculated by applying the velocity over the time interval (Δt).



Edu-plume

Edu-plume is a toy model created by Prof.Koracins student

The Gaussian plume model used is the standard model using P-G stability classes and plume spread equations. The equations used are those estimated from the P-G curves and commonly used in EPA screening dispersion models.



The Lagrangian particle model used is a statistical displacement model using a simplified lagrangian timescale estimate using the equation:

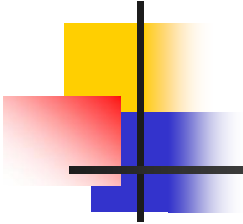
$$Tl = 2 * \sigma^2 / Co * \epsilon$$

where sigma is the standard deviation of u, v, and w wind components, Co is an empirical constant (5.7) and epsilon is the dissipation rate of turbulent kinetic energy.

Sigmas for the different P-G stability classes are estimated using linear relations to friction velocity.

Future versions of this model should include a more sophisticated method of computing the sigmas using Monin-Obukov similarity theory and one of the standard particle model turbulence equation sets used in the DRI particle model.

More realistic atmospheric inputs using a M-O based equation set would be beneficial also.



The wind profile equation used in this model is a simple exponential equation used a different exponent for each stability class.

Friction velocity and epsilon are estimated using the neutral log-law-of the wall equation set and a friction length of 0.01 meters.

The model also includes Brigg's plume rise equation and a plume reflection scheme for both the Gaussian and LPM models.

STACK PARAMETERS



Stack height meters

outflow velocity m/s

gas temp. deg K

emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="600"/> seconds

Plot axis

X
 Y
 Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

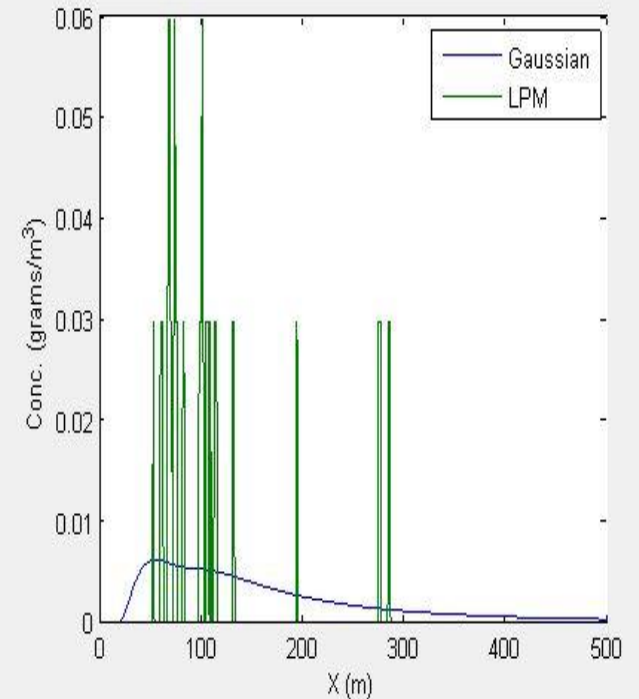
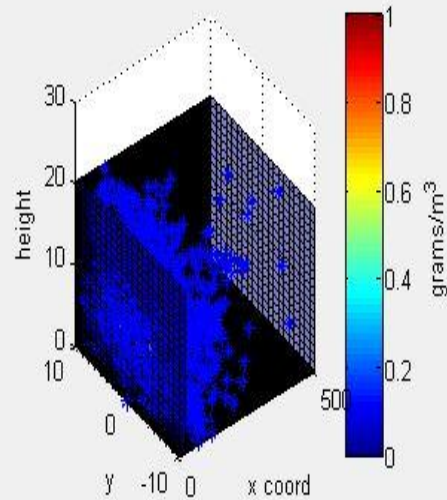
Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height: 5 meters
outflow velocity: 5 m/s
gas temp.: 285 deg K
emission rate: 100 grams/second
inside diameter: 1 meters



Grid Dimensions
500 meters 20 meters 20 meters
X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model
Mass/particle: 1 grams
Timestep size: 10 second
Max. # of particles: 2000
LPM timestep: 860 seconds
LPM initialize

Plot axis
 X
 Y
 Z

Coord. 1: 10 meters Y coord.
Coord. 2: 10 meters Z coord.

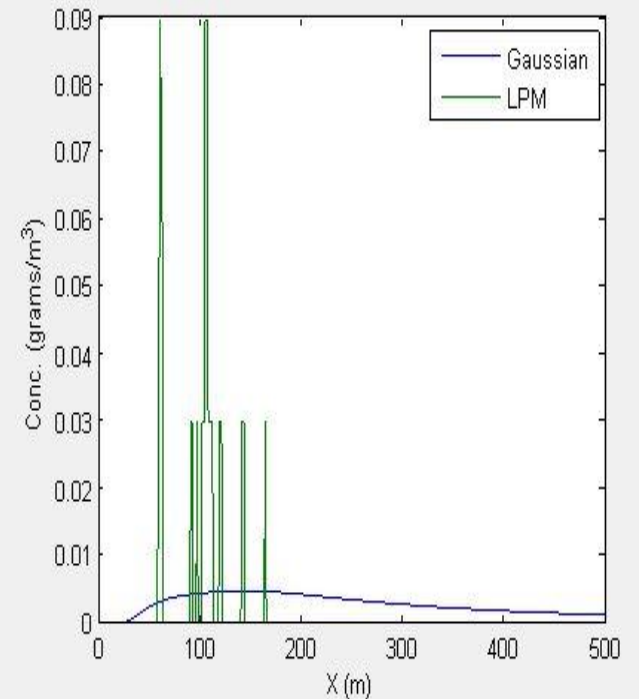
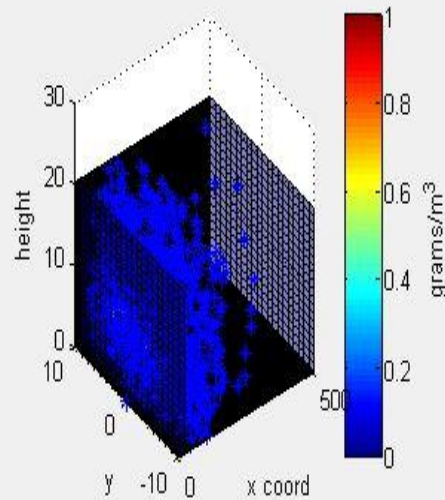
Plot concentrations
output concentration file

ATMOSPHERIC CONDITIONS



2m temp: 285 deg K
Stability Class: A B C D E F
Unstable ----- Neutral ----- Stable
10m wind vel.: 3 m/s

Concentration at point
20 X
0 Y
9 Z
grams/m³
Gaussian: 0.45711
Particle Model: 0.059683
LPM sampling radius: 2 meters
Colorbar Conc. Max.: 1 grams/m³
View direction: default



grid resolution: 1 meters
Slice type: crosswind vertical downwind
1 slice coord.: 20
Number of slices through plume: 1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="830"/> seconds

Plot axis

X Y Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X Y Z

Colorbar Conc. Max. grams/m³

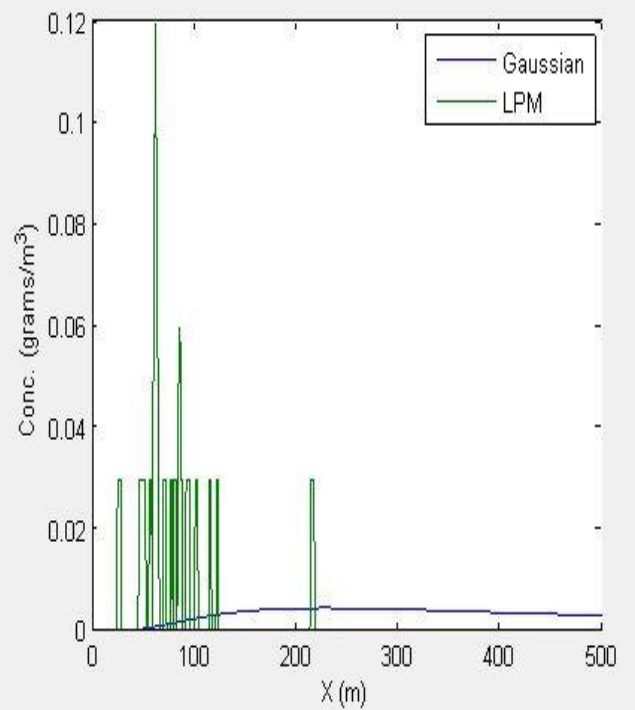
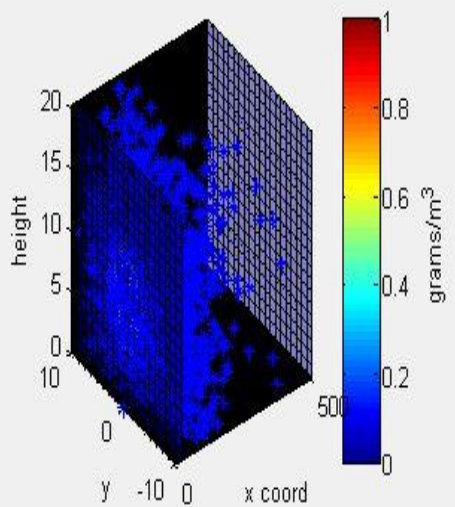
Gaussian: grams/m³

Particle Model:

LPM sampling radius meters

View direction

default from behind from the side from above



grid resolution meters

Slice type crosswind vertical downwind

1 slice coord.

Number of slices through plume 1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="960"/> seconds

Plot axis

- X
- Y
- Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X

Y

Z

grams/m³

Gaussian:

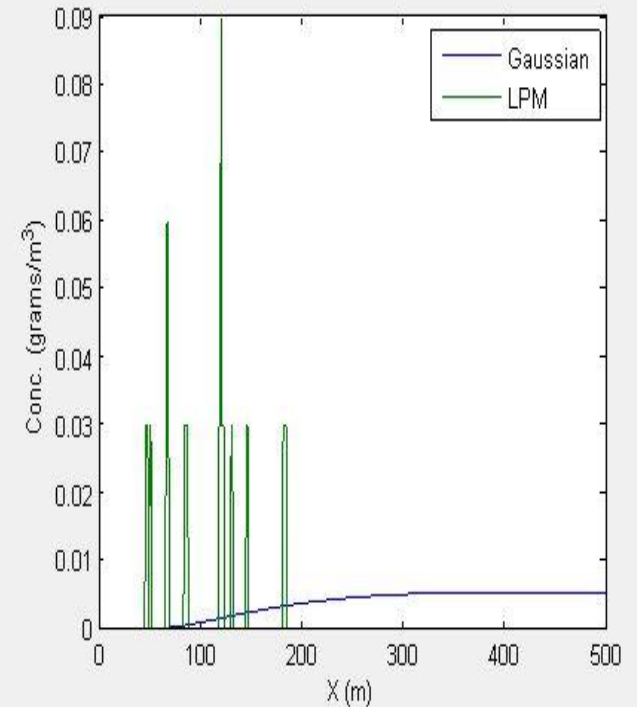
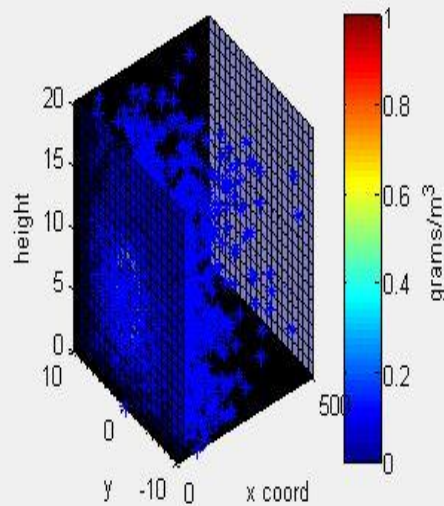
Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

View direction

- default
- from behind
- from the side
- from above



grid resolution meters

Slice type

- crosswind
- vertical
- downwind

1 slice coord.

Number of slices through plume

- 1
- 2
- 3
- 4
- 5

STACK PARAMETERS



Stack height meters

outflow velocity m/s

gas temp. deg K

emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="910"/> seconds

Plot axis

X

Y

Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X

Y

Z

grams/m³

Gaussian:

Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

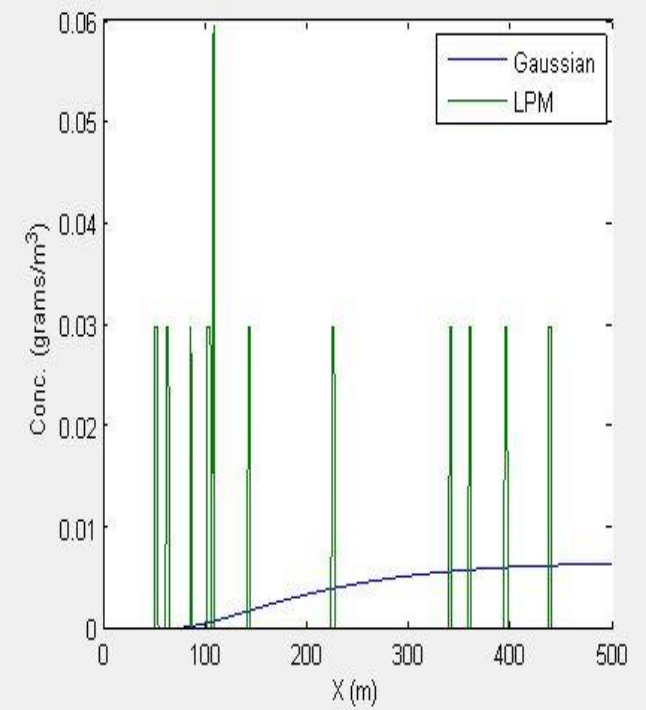
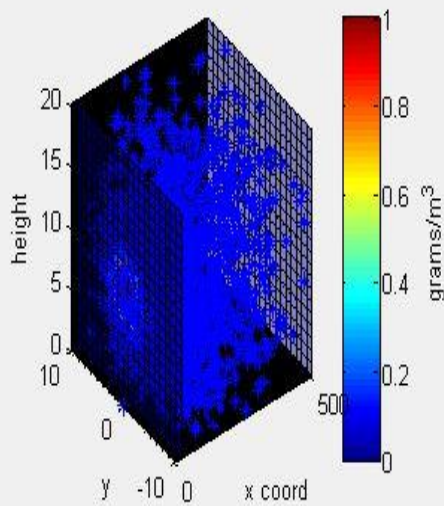
View direction

default

from behind

from the side

from above



grid resolution meters

Slice type crosswind vertical downwind

1 slice coord.

Number of slices through plume 1 2 3 4 5

STACK PARAMETERS



Stack height meters

outflow velocity m/s

gas temp. deg K

emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1030"/> seconds

Plot axis

X

Y

Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X

Y

Z

grams/m³

Gaussian:

Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

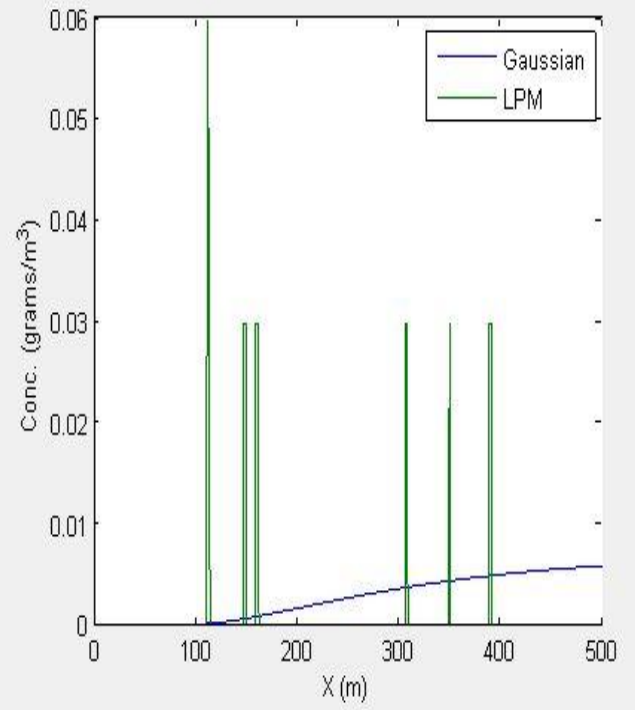
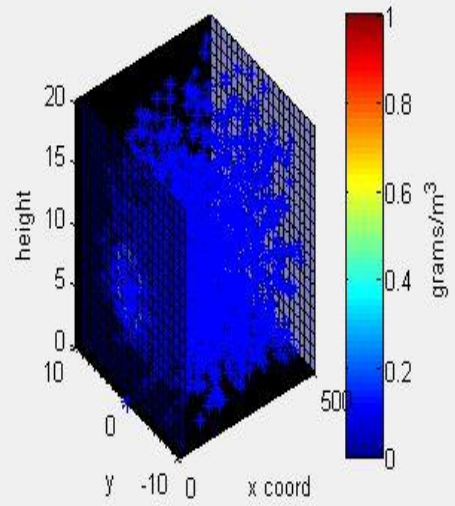
View direction

default

from behind

from the side

from above



grid resolution meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height meters

outflow velocity m/s

gas temp. deg K

emission rate grams/second

inside diameter meters

Edu-plume

Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1010"/> seconds

Plot axis

X

Y

Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X

Y

Z

Colorbar Conc. Max. grams/m³

Gaussian: grams/m³

Particle Model:

LPM sampling radius meters

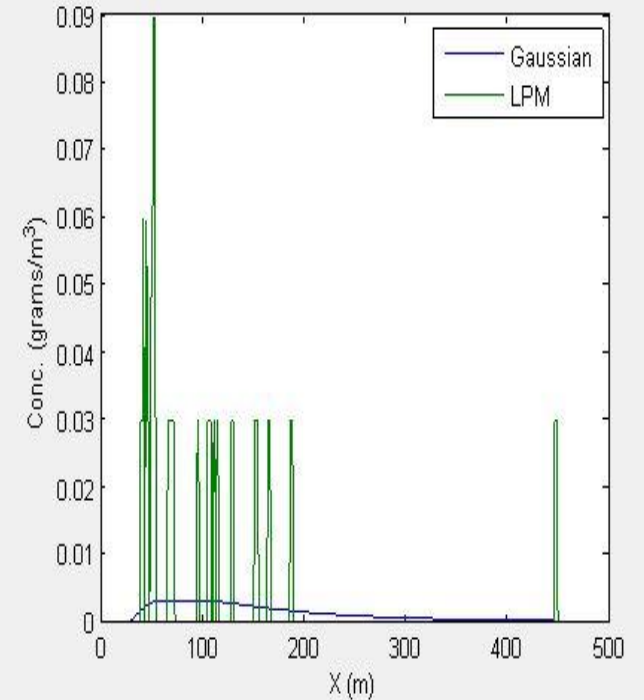
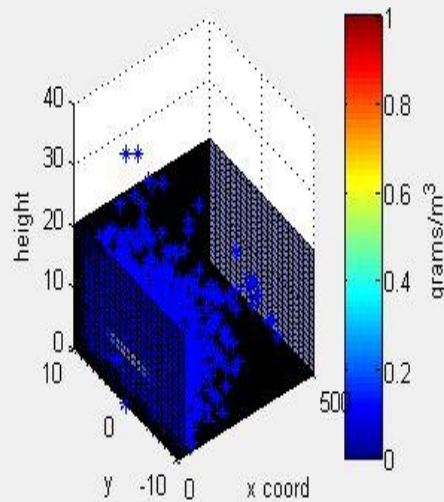
View direction

default

from behind

from the side

from above



grid resolution meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X:downwind Y:crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1010"/> seconds

Plot axis

X
 Y
 Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

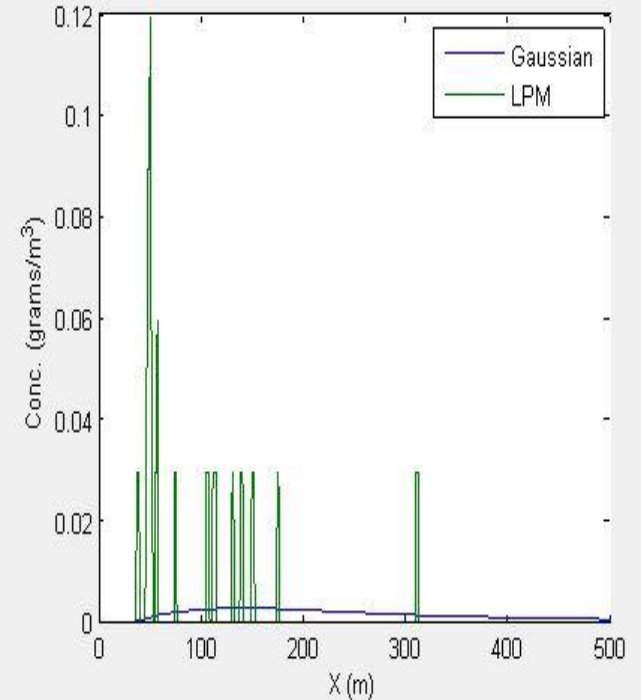
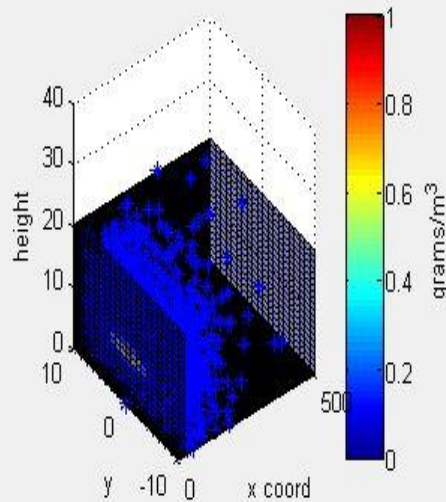
Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution meters

Slice type crosswind vertical downwind

1 slice coord.

Number of slices through plume 1 2 3 4 5

STACK PARAMETERS



Stack height meters
outflow velocity m/s
gas temp. deg K
inside diameter meters
emission rate grams/second



Grid Dimensions

meters meters meters
X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle grams
Timestep size second
Max. # of particles
LPM timestep seconds
LPM initialize

Plot axis

X
 Y
 Z

Coord. 1

meters

Y coord.

Coord. 2

meters

Z coord.

Plot concentrations

output concentration file

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

Particle Model:

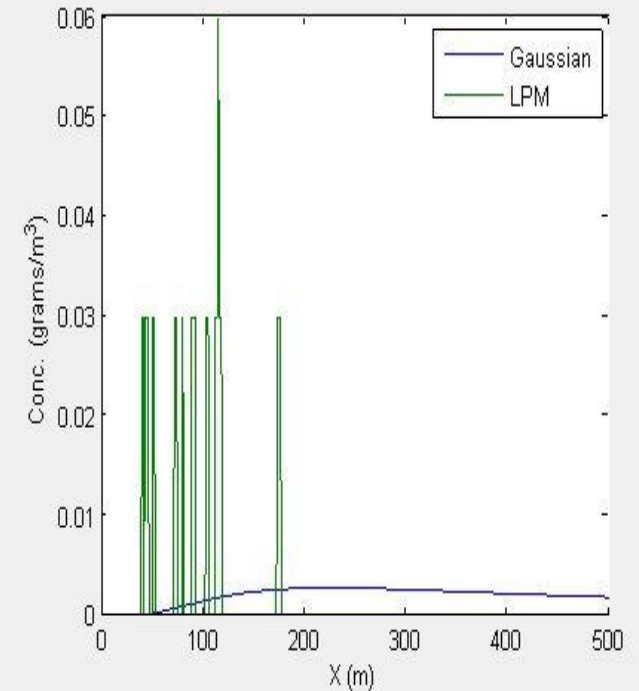
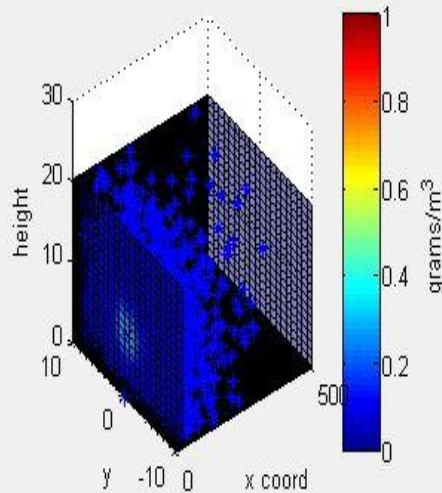
LPM sampling radius meters

Colorbar Conc. Max.

grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution

meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X:downwind Y:crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1080"/> seconds

Plot axis

X
 Y
 Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

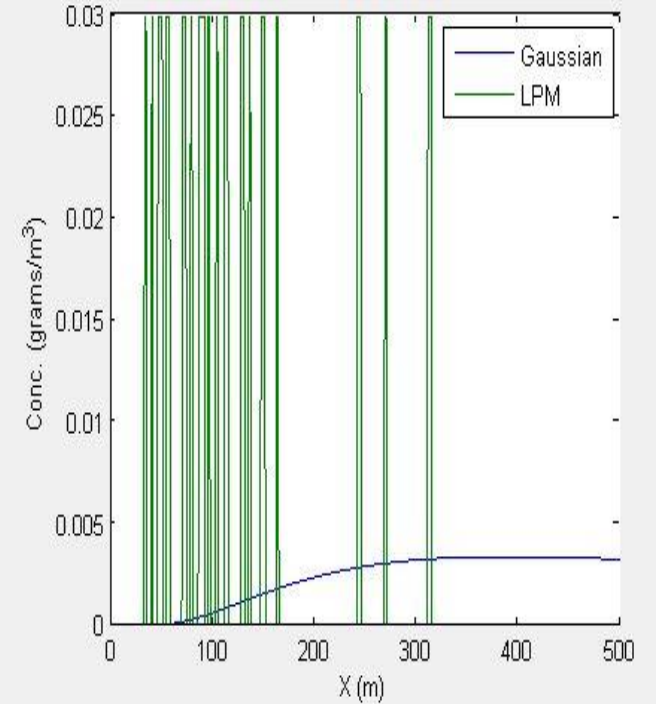
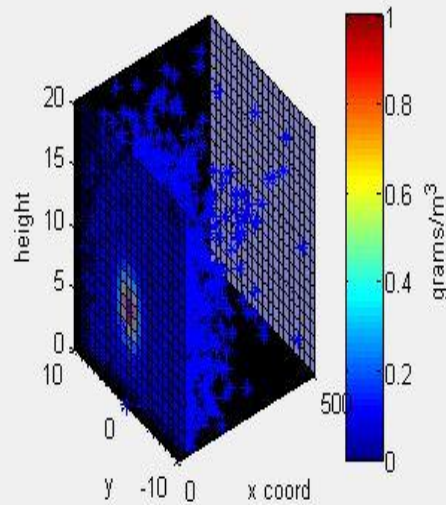
Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution meters

Slice type crosswind vertical downwind

1 slice coord.

Number of slices through plume 1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters

Edu-plume

Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle grams Timestep size second Max. # of particles

LPM timestep seconds

Plot axis

X
 Y
 Z

Coord. 1

meters

Y coord.

Coord. 2

meters

Z coord.

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

Particle Model:

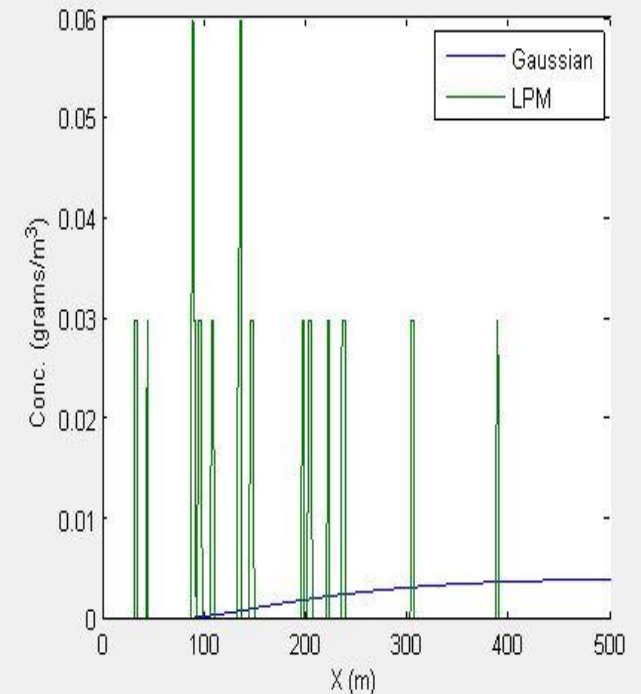
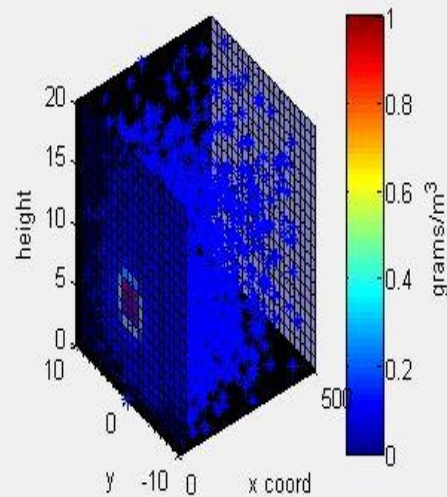
LPM sampling radius meters

Colorbar Conc. Max.

grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution

meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K emission rate grams/second

inside diameter meters



Grid Dimensions

meters meters meters

X:downwind Y:crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1070"/> seconds

Plot axis

X Y Z

Coord. 1 meters **Y coord.**

Coord. 2 meters **Z coord.**

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X Y Z

grams/m³

Gaussian:

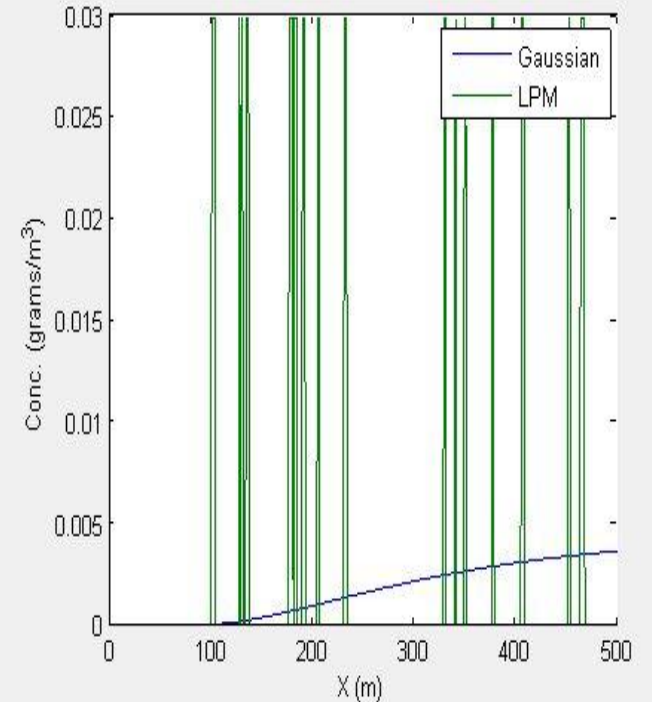
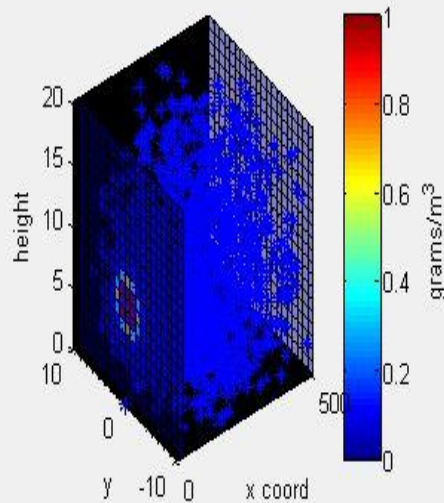
Particle Model:

LPM sampling radius meters

Colorbar Conc. Max. grams/m³

View direction

default from behind from the side from above



grid resolution meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5

STACK PARAMETERS



Stack height meters outflow velocity m/s

gas temp. deg K

inside diameter meters emission rate grams/second

Edu-plume

Grid Dimensions

meters meters meters

X: downwind Y: crosswind Z (height)

Edu-plume is a matlab based simple plume dispersion model that includes a steady state Gaussian dispersion model and a Lagrangian particle model based on a simplified Lagrangian timescale equation

Lagrangian Particle Model

Mass/particle	Timestep size	Max. # of particles	LPM timestep
<input type="text" value="1"/> grams	<input type="text" value="10"/> second	<input type="text" value="2000"/>	<input type="text" value="1070"/> seconds

Plot axis

X
 Y
 Z

Coord. 1

meters

Y coord.

Coord. 2

meters

Z coord.

ATMOSPHERIC CONDITIONS



2m temp deg K

Stability Class

A B C D E F

Unstable ----- Neutral ----- Stable

10m wind vel. m/s

Concentration at point

X
 Y
 Z

grams/m³

Gaussian:

Particle Model:

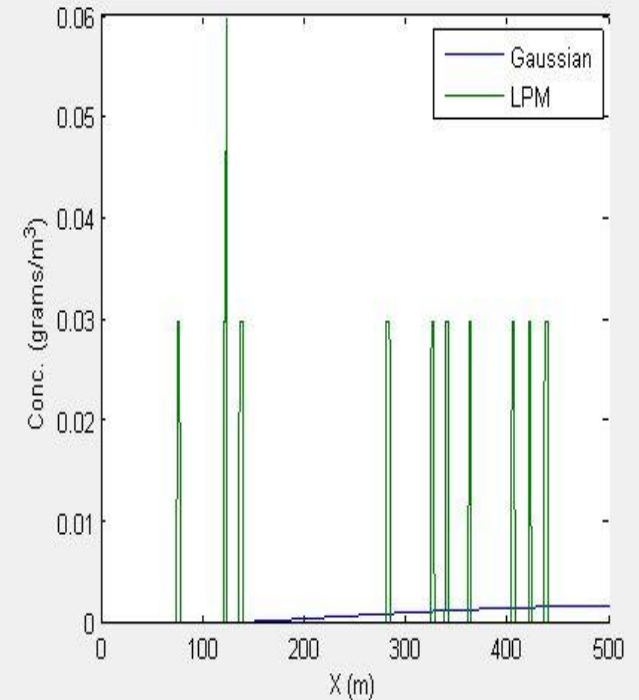
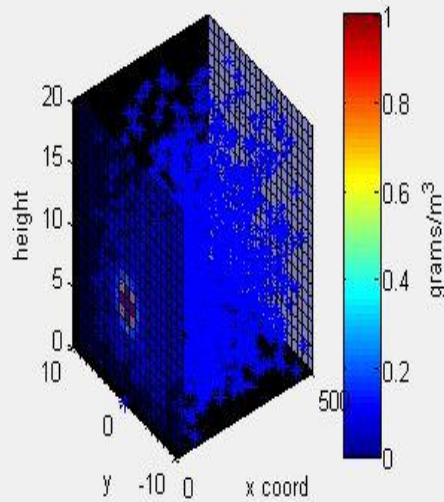
LPM sampling radius meters

Colorbar Conc. Max.

grams/m³

View direction

default
 from behind
 from the side
 from above



grid resolution

meters

Slice type

crosswind vertical downwind

1 slice coord.

Number of slices through plume

1 2 3 4 5



THANK YOU !!!
