

Newton's laws of motion

Force causes change in motion.

Force is a vector: magnitude & direction

Experiments show that what matters is the **net** force or **unbalanced force** \Rightarrow meaning the vector sum of all individual forces acting on an object.

1st Newton's law of motion or Law of inertia

Every object continues in its state of rest or state of uniform velocity in a straight line as long as no net force acts on it.

$$\sum \vec{F} = 0$$

The tendency of an object to maintain its state of rest or uniform velocity is called **INERTIA**

— note! only in inertial reference frames does the 1st n. law hold!

inertial reference frame — nonaccelerating reference frame

noninertial r. frame — accelerating

— note: mass / weight

2nd Newton's law of motion

The acceleration of an object is directly proportional to the **NET** force acting on it, and it is inversely proportional to the object's mass. The direction of the acceleration is in the direction of the net force acting on the object.

$$\Sigma \vec{F} = m \vec{a} \quad \rightarrow \quad \underbrace{F}_{[N]} \quad [kg \, m \, s^{-2}] = [N]$$

$$x \quad \Sigma F_x = m a_x$$

$$y \quad \Sigma F_y = m a_y$$

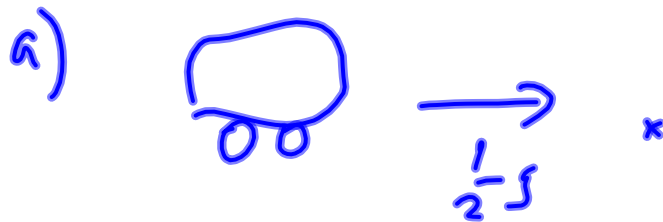
$$z \quad \Sigma F_z = m a_z$$

$$\vec{F} = F_x \hat{i} + F_y \hat{j} + F_z \hat{k}$$

Ex

Estimate a net force needed to accelerate

- a) 1000 kg car at $\frac{1}{2}g$
 b) 200g apple at the same rate



b) \rightarrow
 $\Sigma F_x = 0.2 \text{ kg} \cdot \frac{1}{2}g = 1 \text{ N}$

$$\Sigma F_x = m a_x$$

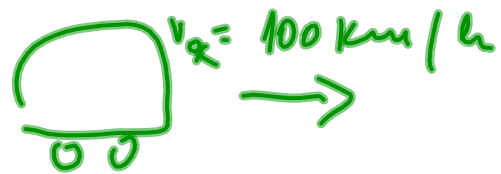
$$a_x = \frac{1}{2}g \quad g \sim 10 \text{ m/s}^2$$

$$m = 1000 \text{ kg}$$

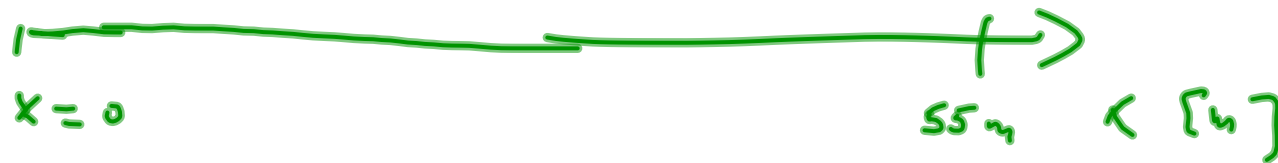
$$\Sigma F_x = 500 \text{ N}$$

Ex 2

What average net force is required to bring a 1500 kg car to rest from a speed of 100 km/h within a distance of 55 m?



$$v = 0$$



$$m = 1500 \text{ kg}$$

$$v_0 = 100 \text{ km/h} = 27.8 \text{ m/s}$$

$$v = 0$$

$$x = 55 \text{ m}$$

the force acts
in opposite
direction than
initial velocity

$$\sum F_x = ?$$

$$\sum F_x = m a_x$$

$$a_x = ?$$

$$\sum F_x = 1500 \cdot (-7) = -1.1 \cdot 10^4 \text{ N}$$

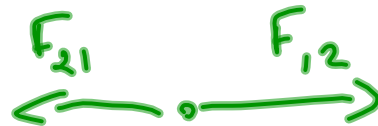
$$a = \frac{v^2 - v_0^2}{2(x - x_0)}$$

$$= \frac{0 - 27.8^2 \text{ m}^2/\text{s}^2}{2 \cdot 55 \text{ m}}$$

$$= -7 \text{ m/s}^2$$

Newton's 3rd law of motion

Whenever one object exerts a force on a second object, the second object exerts an **equal** force in the opposite direction on the first object



Forces

Gravitational force or force of gravity

$$\vec{F}_g = m \vec{g}$$

toward center of earth

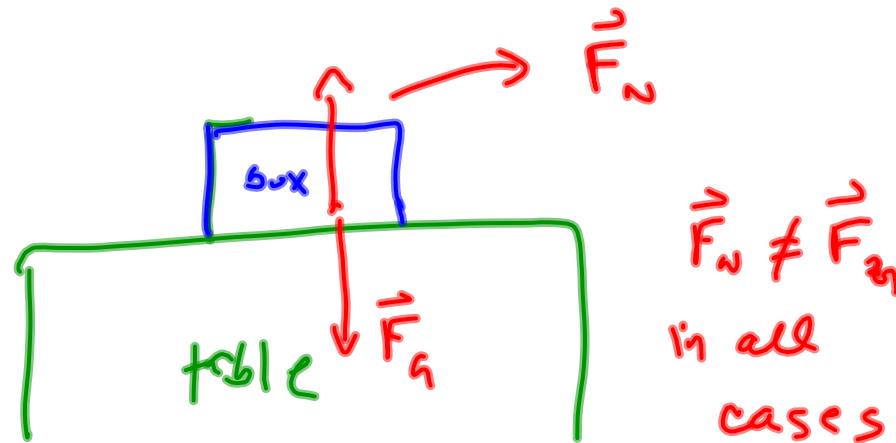
note F_g is also called weight

Normal force

Tension force

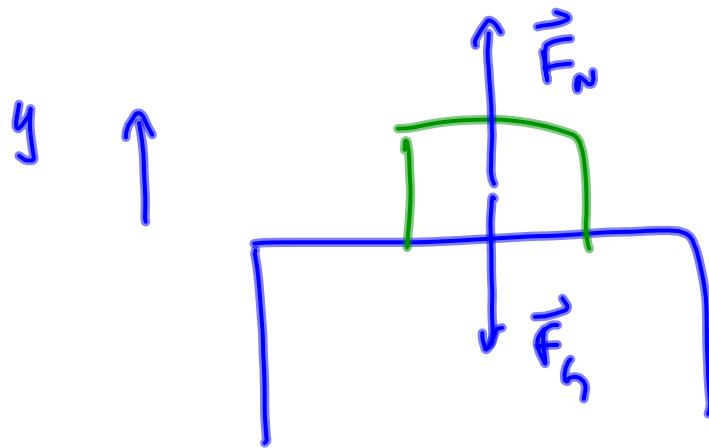
Normal force

- when a contact force acts \perp to the common surface of the contact it is referred to as the normal force



A box of 10 kg mass rests on frictionless horizontal surface

- a) determine the weight of the box & normal force exerted by the table



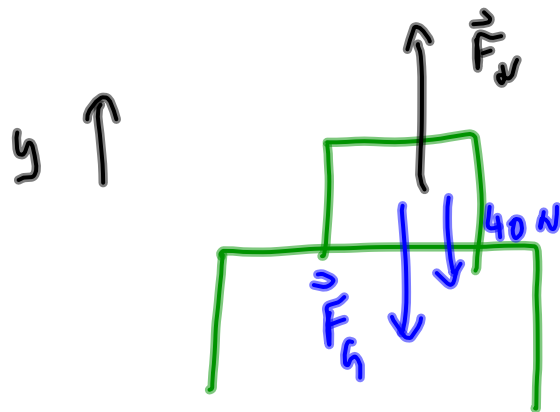
$$\Sigma F_y = F_N - F_g$$

$$a_y = 0$$

$$\Sigma F_y = 0$$

$$F_N = F_g = 98 \text{ N}$$

b) your friend pushes down on the box with a force of 40 N



ΣF_y is a sum

$$\Sigma F_y = F_N - F_h - 40\text{N}$$

c) $a_y = 2\text{m/s}$

$$\Sigma F_y \neq 0$$

$$\Sigma F_y = F_N + (-F_h) !$$