

# Multiple equilibria in a cloud resolving model – Supplement

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## 1 Model Parameters

Below is a table consisting of the parameters and run times used for the simulations which provided data for this work. Size and grid refer to domain size and grid resolution, both are given in km. Both the potential temperature relaxation time (hours) and its inverse ( $t_\theta^{-1}$ , measured in  $s^{-1}$ ) are specified since the latter is the actual model input parameter.  $f$  is the fraction of the of the radiative convective equilibrium (RCE) moisture profile initially in the domain (equation (3) of section 2).  $x_s$  (km),  $\delta\theta_{local}^{max}$  and  $\delta\theta_{random}^{max}$  are initial perturbations, equation (5) of section 2. The potential temperature perturbations are given as fractional values of the RCE profile,  $\theta_0$ , since this is actual model input. To estimate the absolute temperature perturbation, multiply the values given by 300 K. Time is the model run time in days. Rain rate (in  $mm\ day^{-1}$ ) is not an input parameter, but has been included to identify the runs which correspond to the two possible equilibrium states.

Model parameters for individual runs

Test	size	grid	$v_y$	$t_\theta^{-1}$	$t_\theta$	$f$	$x_s$	$\frac{\delta\theta_{local}^{max}}{\theta_0}$	$\frac{\delta\theta_{random}^{max}}{\theta_0}$	time	rain rate
1	50	0.5	3	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	60	0.0000
2	50	0.5	3	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	60	0.0000
3	50	0.5	4	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	120	0.0000
4	50	0.5	4	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	60	0.0000
5	50	0.5	5	$1.0 \times 10^{-5}$	27.78	0	3	0.03	0.001	120	3.908
6	50	0.5	5	$2.5 \times 10^{-5}$	11.11	0	3	0.03	0.001	120	2.629
7	50	0.5	5	$3.25 \times 10^{-5}$	8.55	0	3	0.03	0.001	120	2.410
8	50	0.5	5	$4.0 \times 10^{-5}$	6.94	0	3	0.03	0.001	120	0.0005
9	50	0.5	5	$7.5 \times 10^{-5}$	3.70	0	1	0.03	0.03	120	0.0001
10	50	0.5	5	$7.5 \times 10^{-5}$	3.70	1	1	0.03	0.03	120	3.288
11	50	0.5	5	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
12	50	0.5	5	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	60	2.964
13	50	0.5	5	$1.0 \times 10^{-3}$	0.28	0.5	3	0.03	0.001	120	0.0000
14	50	0.5	5	$1.0 \times 10^{-3}$	0.28	0.9	3	0.03	0.001	120	0.0000
15	50	0.5	5	$1.0 \times 10^{-3}$	0.28	1.0	3	0.03	0.001	120	0.0000
16	50	0.5	6	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	120	0.0000
17	50	0.5	6	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	60	6.921
18	50	0.5	7	$1.0 \times 10^{-5}$	27.78	0	3	0.03	0.001	120	6.200
19	50	0.5	7	$4.0 \times 10^{-5}$	6.94	0	3	0.03	0.001	120	10.12
20	50	0.5	7	$5.0 \times 10^{-5}$	5.56	0	3	0.03	0.001	120	10.84
21	50	0.5	7	$6.0 \times 10^{-5}$	4.63	0	3	0.03	0.001	120	0.0038
22	50	0.5	7	$7.88 \times 10^{-5}$	3.53	0	1	0.03	0.03	120	0.0004
23	50	0.5	7	$7.88 \times 10^{-5}$	3.53	1	1	0.03	0.03	120	11.13
24	50	0.5	7	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
25	50	0.5	7	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	10.05
26	50	0.5	7	$1.0 \times 10^{-3}$	0.28	0	3	0.03	0.001	120	0.0000
27	50	0.5	7	$1.0 \times 10^{-3}$	0.28	0.5	3	0.03	0.001	120	0.0000
28	50	0.5	7	$1.0 \times 10^{-3}$	0.28	0.8	3	0.03	0.001	120	0.0000
29	50	0.5	7	$1.0 \times 10^{-3}$	0.28	0.9	3	0.03	0.001	120	7.310
30	50	0.5	7	$1.0 \times 10^{-3}$	0.28	1	3	0.03	0.001	120	7.289
31	50	0.5	10	$7.5 \times 10^{-5}$	3.70	0	1	0.03	0.03	120	19.10
32	50	0.5	10	$1.12 \times 10^{-4}$	2.47	0	1	0.03	0.03	120	21.10
33	50	0.5	10	$1.12 \times 10^{-4}$	2.47	1	1	0.03	0.03	120	20.77
34	50	0.5	10	$1.3 \times 10^{-4}$	2.14	0	1	0.03	0.03	120	20.89
35	50	0.5	10	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	182	0.094
36	50	0.5	10	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	20.33
37	50	0.5	10	$1.0 \times 10^{-3}$	0.28	0	3	0.03	0.001	120	0.0001
38	50	0.5	10	$1.0 \times 10^{-3}$	0.28	0.5	3	0.03	0.001	120	0.0000
39	50	0.5	10	$1.0 \times 10^{-3}$	0.28	0.6	3	0.03	0.001	120	0.0002
40	50	0.5	10	$1.0 \times 10^{-3}$	0.28	0.7	3	0.03	0.001	120	13.11

### Model parameters for individual runs

Test	size	grid	$v_y$	$t_\theta^{-1}$	$t_\theta$	$f$	$x_s$	$\frac{\delta\theta_{local}^{max}}{\theta_0}$	$\frac{\delta\theta_{random}^{max}}{\theta_0}$	time	rain rate
41	50	0.5	10	$1.5 \times 10^{-3}$	0.19	0	1	0.03	0.03	120	0.0001
42	50	0.5	10	$3.0 \times 10^{-2}$	0.01	0	1	0.03	0.003	364	0.0000
43	50	0.5	12	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	103.75	25.49
44	50	0.5	15	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	74.75	31.85
45	50	0.5	15	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	31.48
46	50	0.5	15	$5.7 \times 10^{-4}$	0.49	0	3	0.03	0.001	101	22.94
47	50	0.5	15	$7.85 \times 10^{-4}$	0.35	0	3	0.03	0.001	120	21.57
48	50	0.5	15	$1.0 \times 10^{-3}$	0.28	0	3	0.03	0.001	120	0.0000
49	50	0.5	15	$1.0 \times 10^{-3}$	0.28	0.3	3	0.03	0.001	120	0.0000
50	50	0.5	15	$1.0 \times 10^{-3}$	0.28	0.4	3	0.03	0.001	120	22.43
51	50	0.5	15	$1.0 \times 10^{-3}$	0.28	0.5	3	0.03	0.001	120	23.32
52	50	0.5	15	$3.0 \times 10^{-2}$	0.01	0	1	0.03	0.03	364	0.0000
53	50	0.5	20	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	75.25	40.45
54	50	0.5	20	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	60	40.64
55	50	0.5	20	$1.0 \times 10^{-3}$	0.28	0	3	0.03	0.001	120	0.0461
56	50	0.5	20	$1.0 \times 10^{-3}$	0.28	0.1	3	0.03	0.001	120	30.33
57	50	0.5	20	$1.0 \times 10^{-3}$	0.28	0.3	3	0.03	0.001	120	31.93
58	50	1	0	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	0.0000
59	50	1	3	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	2.535
60	50	1	4	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
61	50	1	4	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	2.944
62	50	1	5	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
63	50	1	5	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	3.927
64	50	1	6	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
65	50	1	6	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	6.011
66	50	1	7	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0000
67	50	1	7	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	9.118
68	50	1	10	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	0.0007
69	50	1	10	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	17.95
70	50	1	12	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	23.11
71	50	1	15	$1.5 \times 10^{-4}$	1.85	0	3	0.03	0.001	120	29.33
72	50	1	15	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	29.67
73	100	1	4	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	0.0000
74	100	1	5	$1.0 \times 10^{-5}$	27.78	0	3	0.03	0.001	120	3.818
75	100	1	5	$4.0 \times 10^{-5}$	6.94	0	3	0.03	0.001	120	0.0000
76	100	1	5	$7.5 \times 10^{-5}$	3.70	0	3	0.03	0.001	120	0.0007
77	100	1	5	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	120	0.0000
78	100	1	5	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	3.884
79	100	1	5	$5.0 \times 10^{-4}$	0.56	0.9	3	0.03	0.001	120	0.0000
80	100	1	5	$5.0 \times 10^{-4}$	0.56	1	3	0.03	0.001	120	4.057

Model parameters for individual runs

Test	size	grid	$v_y$	$t_\theta^{-1}$	$t_\theta$	$f$	$x_s$	$\frac{\delta\theta_{local}^{max}}{\theta_0}$	$\frac{\delta\theta_{random}^{max}}{\theta_0}$	time	rain rate
81	100	1	7	$7.5 \times 10^{-5}$	3.7	0	3	0.03	0.001	120	9.670
82	100	1	7	$1.0 \times 10^{-4}$	2.78	0	3	0.03	0.001	120	9.283
83	100	1	7	$1.25 \times 10^{-4}$	2.22	0	3	0.03	0.001	120	0.0093
84	100	1	7	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	120	0.0003
85	100	1	7	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	8.156
86	100	1	7	$2.1 \times 10^{-4}$	1.32	0	1	0.03	0.03	120	0.0000
87	100	1	7	$5.0 \times 10^{-4}$	0.56	0	3	0.03	0.001	120	0.0000
88	100	1	7	$5.0 \times 10^{-4}$	0.56	0.5	3	0.03	0.001	120	0.0000
89	100	1	7	$5.0 \times 10^{-4}$	0.56	0.7	3	0.03	0.001	120	0.0000
90	100	1	7	$5.0 \times 10^{-4}$	0.56	0.8	3	0.03	0.001	120	7.507
91	100	1	10	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	75.75	17.07
92	100	1	10	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	17.45
93	100	1	10	$1.88 \times 10^{-4}$	1.48	0	1	0.03	0.03	120	17.21
94	100	1	10	$2.25 \times 10^{-4}$	1.23	0	1	0.03	0.03	120	15.41
95	100	1	10	$2.25 \times 10^{-4}$	1.23	1	3	0.03	0.001	360	15.70
96	100	1	10	$2.6 \times 10^{-4}$	1.07	0	1	0.03	0.03	120	0.0018
97	100	1	10	$3.0 \times 10^{-4}$	0.93	0	1	0.03	0.03	120	0.0040
98	100	1	10	$5.0 \times 10^{-4}$	0.56	0	3	0.03	0.001	120	0.0003
99	100	1	10	$5.0 \times 10^{-4}$	0.56	0.5	3	0.03	0.001	120	0.0004
100	100	1	10	$5.0 \times 10^{-4}$	0.56	0.6	3	0.03	0.001	120	12.33
101	100	1	10	$5.0 \times 10^{-4}$	0.56	0.7	3	0.03	0.001	120	13.03
102	100	1	10	$1.5 \times 10^{-3}$	0.19	0	1	0.03	0.03	120	0.0000
103	100	1	15	$7.5 \times 10^{-5}$	3.70	0	3	0.03	0.001	120	24.36
104	100	1	15	$2.88 \times 10^{-4}$	0.96	0	3	0.03	0.001	120	28.51
105	100	1	15	$4.0 \times 10^{-4}$	0.69	0	3	0.03	0.001	120	0.0000
106	100	1	15	$5.0 \times 10^{-4}$	0.56	0	3	0.03	0.001	120	0.0000
107	100	1	15	$5.0 \times 10^{-4}$	0.56	0.3	3	0.03	0.001	120	0.0000
108	100	1	15	$5.0 \times 10^{-4}$	0.56	0.4	3	0.03	0.001	120	0.0000
109	100	1	15	$5.0 \times 10^{-4}$	0.56	0.5	3	0.03	0.001	120	23.00
110	100	1	20	$5.0 \times 10^{-4}$	0.56	0	3	0.03	0.001	120	34.94
111	200	1	4	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	0.0000
112	200	1	5	$1.0 \times 10^{-5}$	27.78	0	3	0.03	0.001	120	4.280
113	200	1	5	$4.25 \times 10^{-5}$	6.54	0	3	0.03	0.001	120	1.784
114	200	1	5	$7.5 \times 10^{-5}$	3.70	0	3	0.03	0.001	120	0.0804
115	200	1	5	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	120	0.0000
116	200	1	5	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	4.050
117	200	1	5	$2.5 \times 10^{-4}$	1.11	0.8	3	0.03	0.001	120	0.0000
118	200	1	5	$2.5 \times 10^{-4}$	1.11	0.9	3	0.03	0.001	120	3.735
119	200	1	7	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	182	8.775
120	200	1	7	$1.5 \times 10^{-4}$	1.85	1	1	0.03	0.03	182	8.567

Model parameters for individual runs

Test	size	grid	$v_y$	$t_\theta^{-1}$	$t_\theta$	$f$	$x_s$	$\frac{\delta\theta_{local}^{max}}{\theta_0}$	$\frac{\delta\theta_{random}^{max}}{\theta_0}$	time	rain rate
121	200	1	7	$1.8 \times 10^{-4}$	1.54	0	3	0.03	0.001	120	0.0000
122	200	1	7	$2.1 \times 10^{-4}$	1.32	0	1	0.03	0.03	360	0.0011
123	200	1	7	$2.1 \times 10^{-4}$	1.32	0	3	0.03	0.001	360	0.0000
124	200	1	7	$2.1 \times 10^{-4}$	1.32	1	1	0.03	0.03	120	7.873
125	200	1	7	$2.5 \times 10^{-4}$	1.11	0	3	0.03	0.001	120	0.0000
126	200	1	7	$2.5 \times 10^{-4}$	1.11	0.5	3	0.03	0.001	120	0.0000
127	200	1	7	$2.5 \times 10^{-4}$	1.11	0.7	3	0.03	0.001	120	0.0008
128	200	1	7	$2.5 \times 10^{-4}$	1.11	0.8	3	0.03	0.001	120	7.816
129	200	1	7	$3.0 \times 10^{-2}$	0.01	0	1	0.03	0.03	364	0.0000
130	200	1	10	$1.5 \times 10^{-4}$	1.85	0	1	0.03	0.03	60	17.93
131	200	1	10	$1.5 \times 10^{-4}$	1.85	1	3	0.03	0.001	120	17.09
132	200	1	10	$2.5 \times 10^{-4}$	1.11	0	3	0.03	0.001	105	14.67
133	200	1	10	$2.5 \times 10^{-4}$	1.11	0.5	3	0.03	0.001	120	14.70
134	200	1	10	$3.0 \times 10^{-4}$	0.93	0	1	0.03	0.03	120	13.53
135	200	1	10	$6.0 \times 10^{-4}$	0.46	0	1	0.03	0.03	120	11.47
136	200	1	10	$7.0 \times 10^{-4}$	0.40	0	3	0.03	0.001	120	0.0053
137	200	1	10	$8.0 \times 10^{-4}$	0.35	0	1	0.03	0.03	120	0.0036
138	200	1	10	$1.0 \times 10^{-3}$	0.28	0	1	0.03	0.03	120	0.0018
139	200	1	10	$1.5 \times 10^{-3}$	0.19	0	1	0.03	0.03	120	0.0000
140	200	1	10	$3.75 \times 10^{-3}$	0.07	0	1	0.03	0.03	120	0.0000
141	200	1	15	$2.5 \times 10^{-4}$	1.11	0	3	0.03	0.001	120	27.24
142	200	1	15	$2.5 \times 10^{-4}$	1.11	0.5	3	0.03	0.001	120	27.37
143	200	1	15	$1.5 \times 10^{-3}$	0.19	0	3	0.03	0.001	120	15.80
144	200	1	15	$2.5 \times 10^{-3}$	0.11	0	3	0.03	0.001	120	13.74
145	200	1	15	$4.0 \times 10^{-3}$	0.07	0	3	0.03	0.001	120	0.0000
146	200	1	15	$6.25 \times 10^{-3}$	0.04	0	3	0.03	0.001	120	0.0000
147	200	1	15	$1.0 \times 10^{-2}$	0.03	0	3	0.03	0.001	120	0.0000
148	200	1	15	$3.0 \times 10^{-2}$	0.01	0	3	0.03	0.001	120	0.0000
149	200	1	20	$2.5 \times 10^{-4}$	1.11	0	3	0.03	0.001	120	37.92

## 2 References

Sessions, S. L., S. Sugaya, D. J. Raymond, and A. H. Sobel: Multiple equilibria in a cloud resolving model. Submitted to *J. Geophys. Res. - Atmospheres*.