

# **PHYSICS 571 – Master's of Science Teaching**

## **“Electromagnetism and Light” Lecture 5 – Magnetic Induction and Flux**

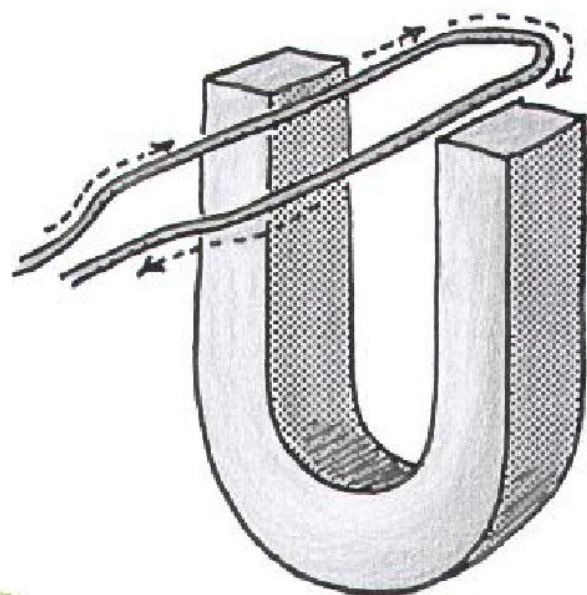
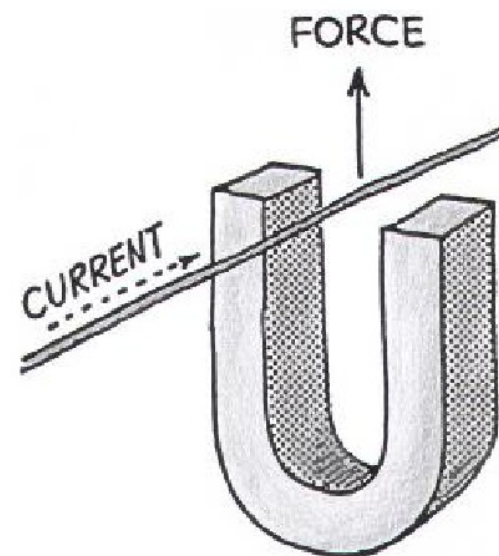
**Instructor – Richard Sonnenfeld**

**[mpsonnenfeld@gmail.com](mailto:mpsonnenfeld@gmail.com) ← Homework and  
Questions**

**575-835-6434**

## NEXT-TIME QUESTION

When current flows in the wire that is placed in the magnetic field shown, the wire is forced upward. If the wire is made to form a loop as shown below, the loop will tend to



- a) rotate clockwise.
- b) rotate counterclockwise.
- c) remain at rest.



# Ways to change flux

Let  $\vec{B}$  be uniform over the loop. Then

$$\Phi_B = \vec{B} \cdot \vec{A}$$

$$\frac{d\Phi_B}{dt} = \frac{d\vec{B}}{dt} \cdot \vec{A} + \frac{d\vec{A}}{dt} \cdot \vec{B}$$

- Can move loop into stronger or weaker B.
- Can increase/decrease B.
- Can rotate B.
- Can increase/decrease size of loop.
- Can rotate loop.

# **Faraday's law, electromagnets, generators etc.**

<http://phet.colorado.edu/en/simulation/faraday>

# Electromagnetic Induction

## CHECK YOUR NEIGHBOR

**More voltage is induced when a magnet is thrust into a coil**

- A. more quickly.
- B. more slowly.
- C. both A and B
- D. neither A nor B

# Electromagnetic Induction

## CHECK YOUR NEIGHBOR

**Not only is voltage induced when a magnet is thrust into a coil of wire, but \_\_\_\_\_ is also induced.**

- A. current
- B. energy
- C. power
- D. none of the above

# Electromagnetic Induction

## CHECK YOUR NEIGHBOR

**The resistance you feel when pushing a piece of iron into a coil involves**

- A. repulsion by the magnetic field you produce.
- B. energy transfer between the iron and coil.
- C. Newton's third law.
- D. resistance to domain alignment in the iron.

# Ways to change flux

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# Outline

Review of magnetic forces and cross products.

Magnetic forces do no Work.

Magnetic Induction

Faradays Law

Examples

Changing  $B$ , constant  $A$

Changing  $A$ , constant  $B$

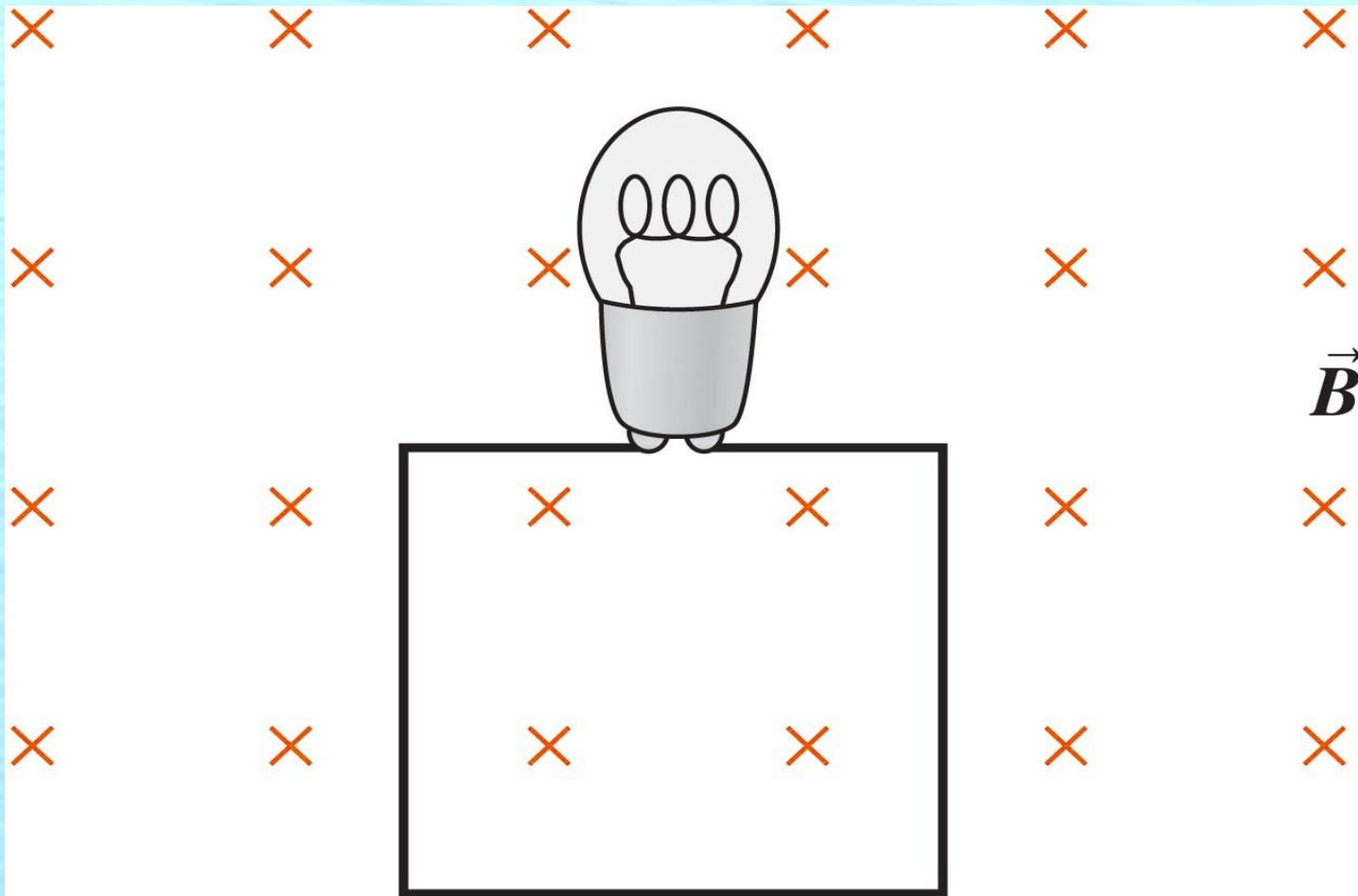
Generators

Constant  $B$ , rotating  $A$

Rigorous definition of Flux

# Changing Flux by Changing B-field

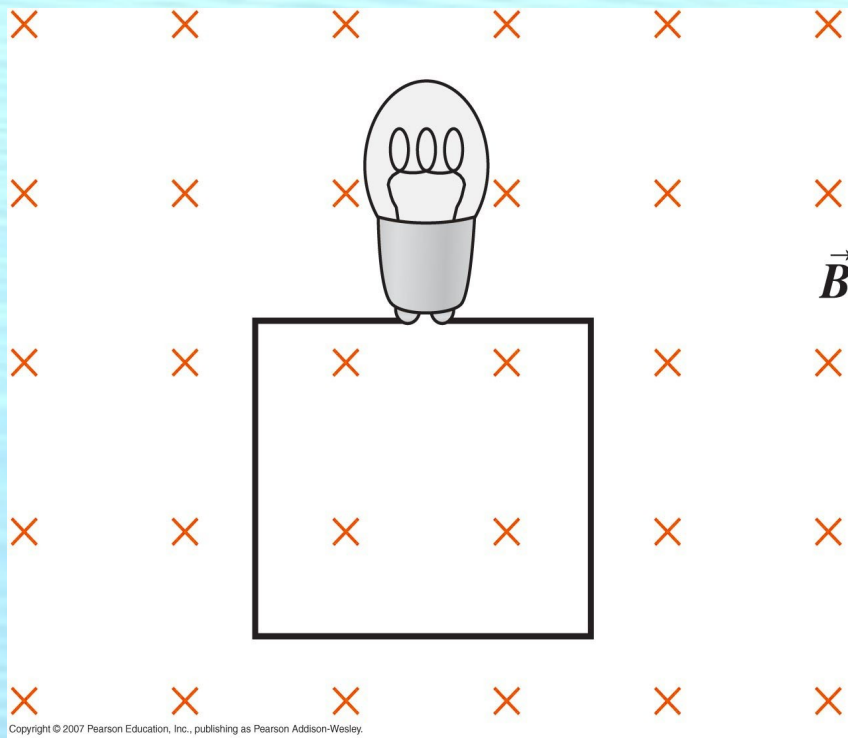
$$\frac{d\Phi_B}{dt} = \frac{d\vec{B}}{dt} \cdot \vec{A} + \frac{d\vec{A}}{dt} \cdot \vec{B} \rightarrow \frac{d\Phi_B}{dt} = \frac{d\vec{B}}{dt} \cdot \vec{A}$$



# Changing B-field parallel to A.

$$\varepsilon = \frac{-d\Phi_B}{dt} = -A \frac{dB}{dt}$$

In the sketch below  $B(t) = 2t^2 + 3$



The loop is square with side 3 m.

At 1 second,  
What voltage is applied to the bulb?

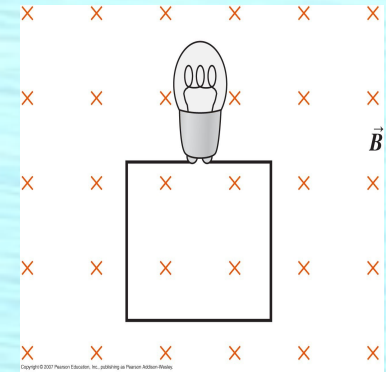
[A] 5 V, [B] 9 V, [C] 18 V, [D] 36 V, [E] 45 V

# Changing B-field parallel to A.

$\varepsilon = -A \frac{dB}{dt}$

In the sketch below  $B(t) = 2t^2 + 3$   
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Examples

Changing B, constant A

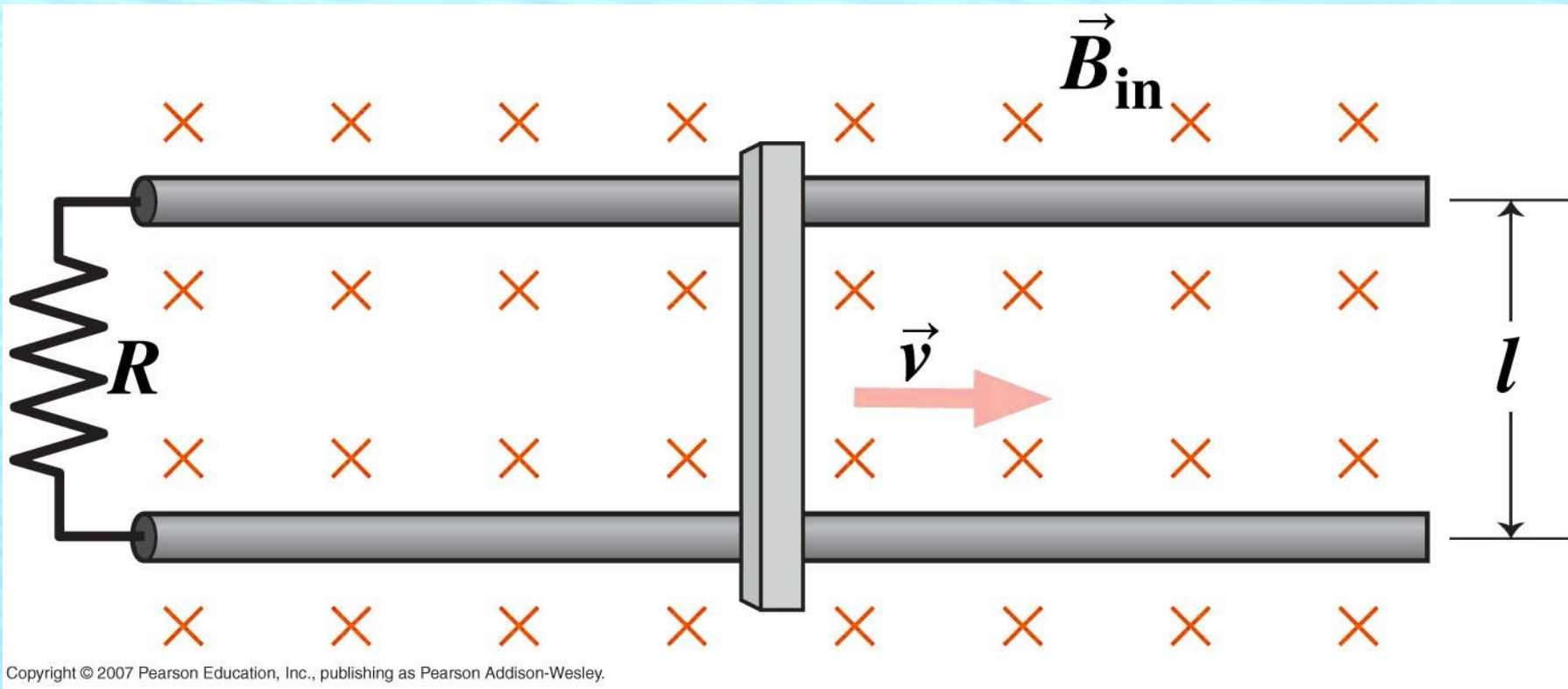
Changing A, constant B

Generators

Constant B, rotating A

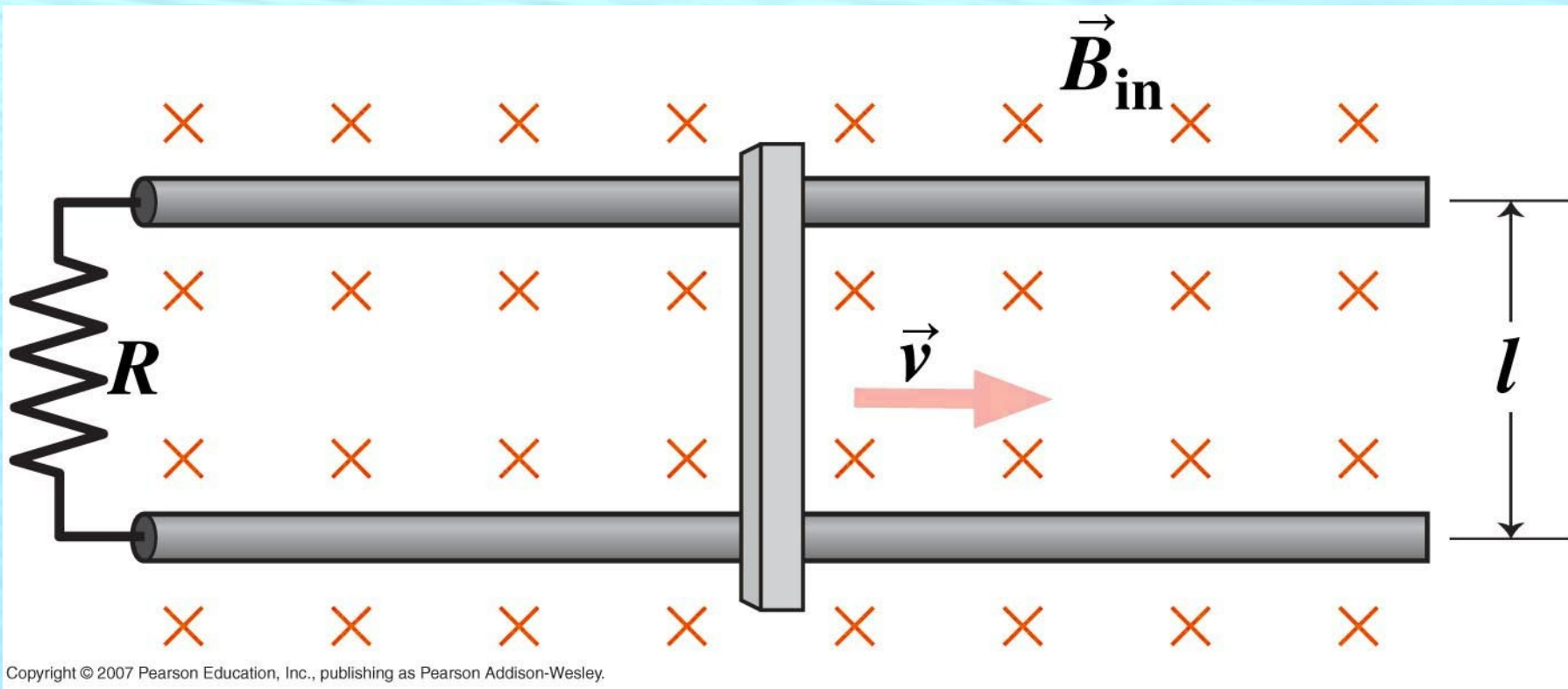
# Changing Flux by Changing size Of Loop

$$\frac{d\Phi_B}{dt} = \frac{d\vec{B} \cdot \vec{A}}{dt} + \frac{d\vec{A} \cdot \vec{B}}{dt} \rightarrow \frac{d\Phi_B}{dt} = \frac{d\vec{A} \cdot \vec{B}}{dt}$$



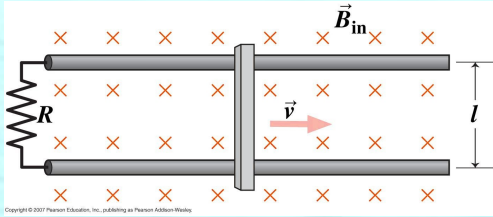
# Changing Flux by Changing size Of Loop

Given  $B=0.1$  T, “ $l$ ”= $0.1$  m,  $v=20$  m/s,  
 $R=30$  Ohms, What are  $V$ ,  $I$ , and  $P$ ?



# Changing Flux by Changing size of Loop

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Changing  $A$ , constant  $B$

Generators

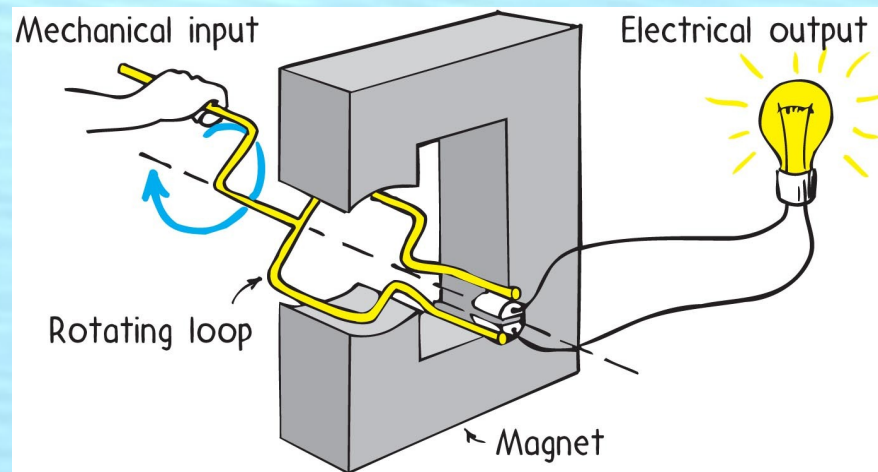
Constant  $B$ , rotating  $A$

Rigorous definition of Flux

# Generators and Alternating Current

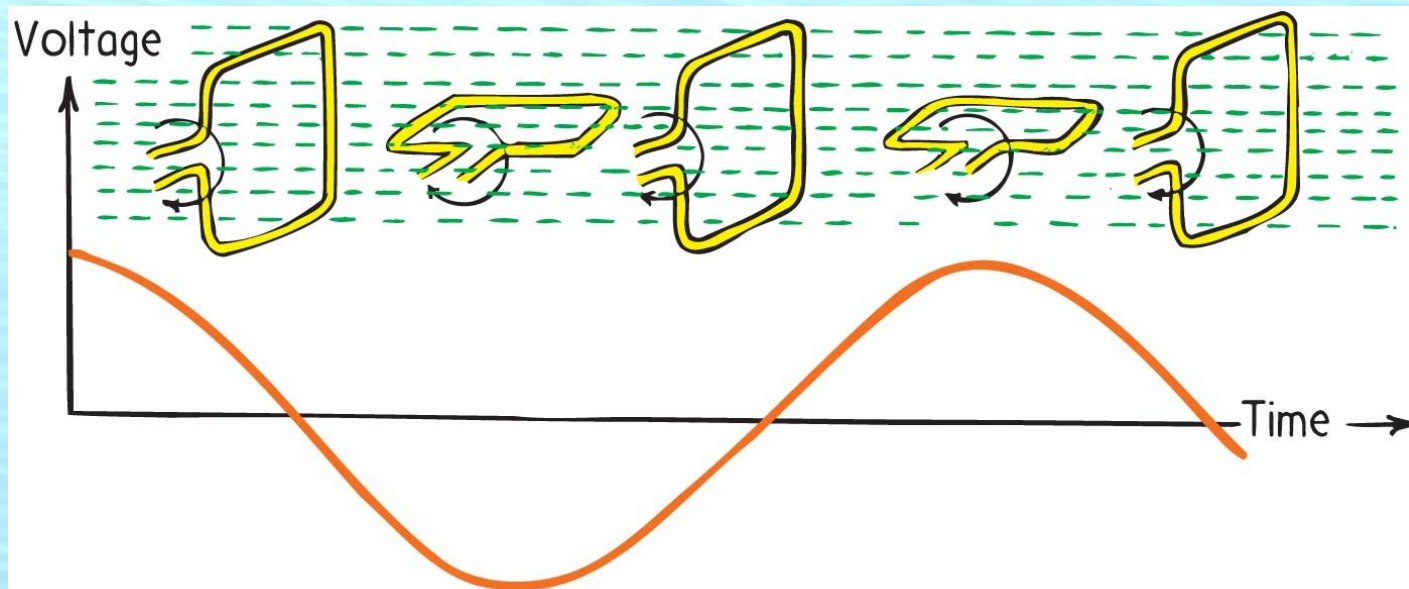
## Generator

- opposite of a motor
- converts mechanical energy into electrical energy via coil motion
- produces alternating voltage and current



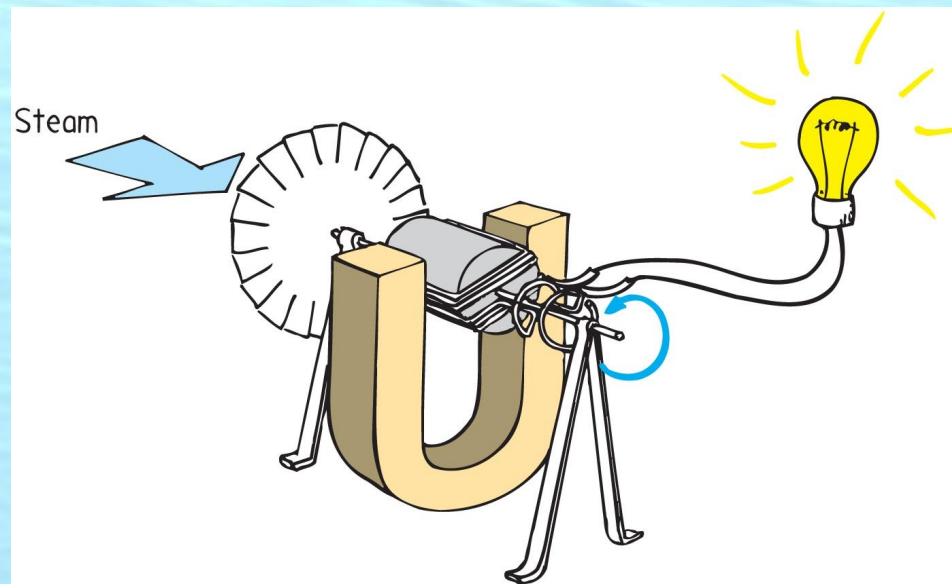
# Generators and Alternating Current

The frequency of alternating voltage induced in a loop is equal to the frequency of the changing magnetic field within the loop.

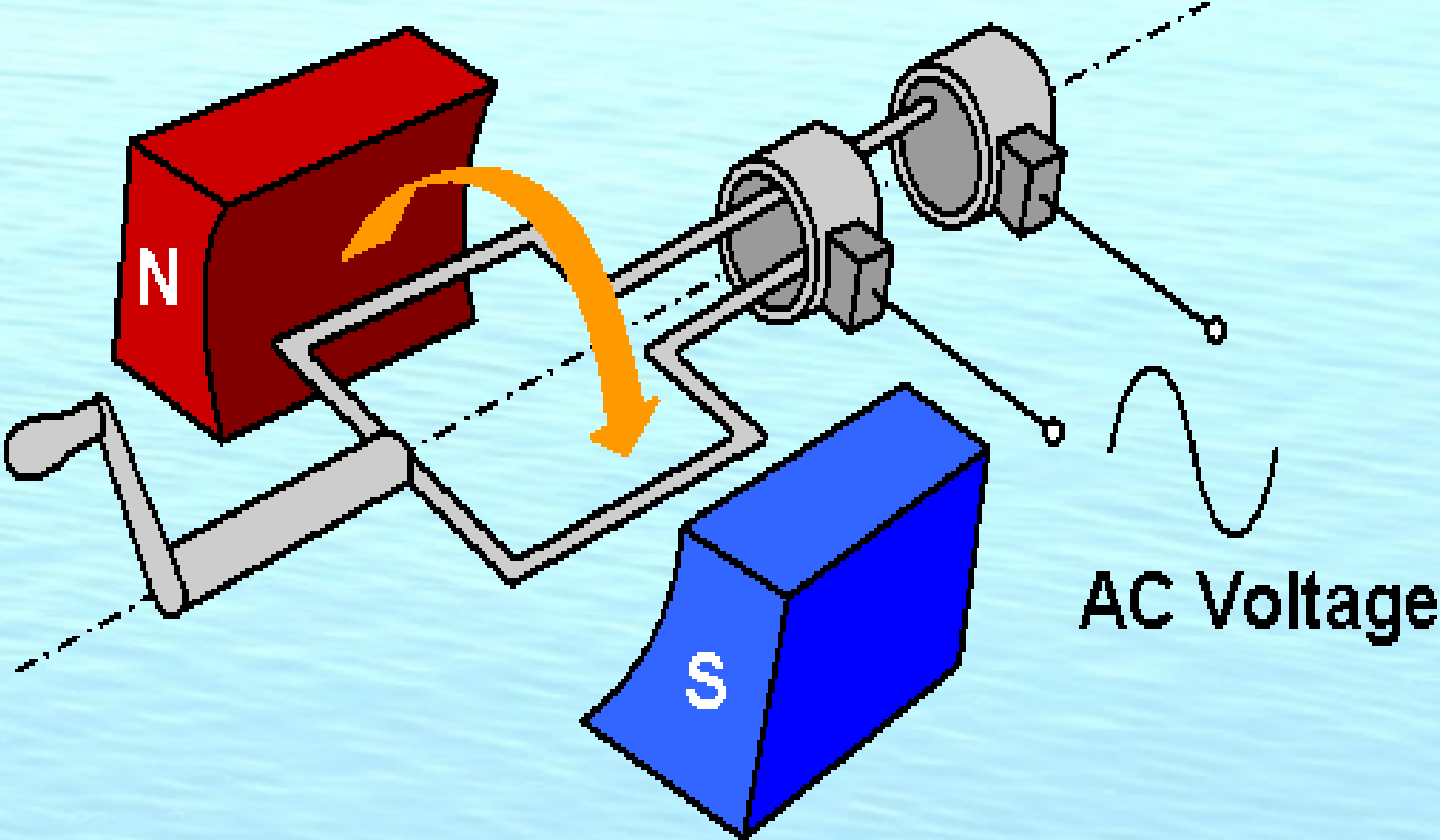


# Power Production

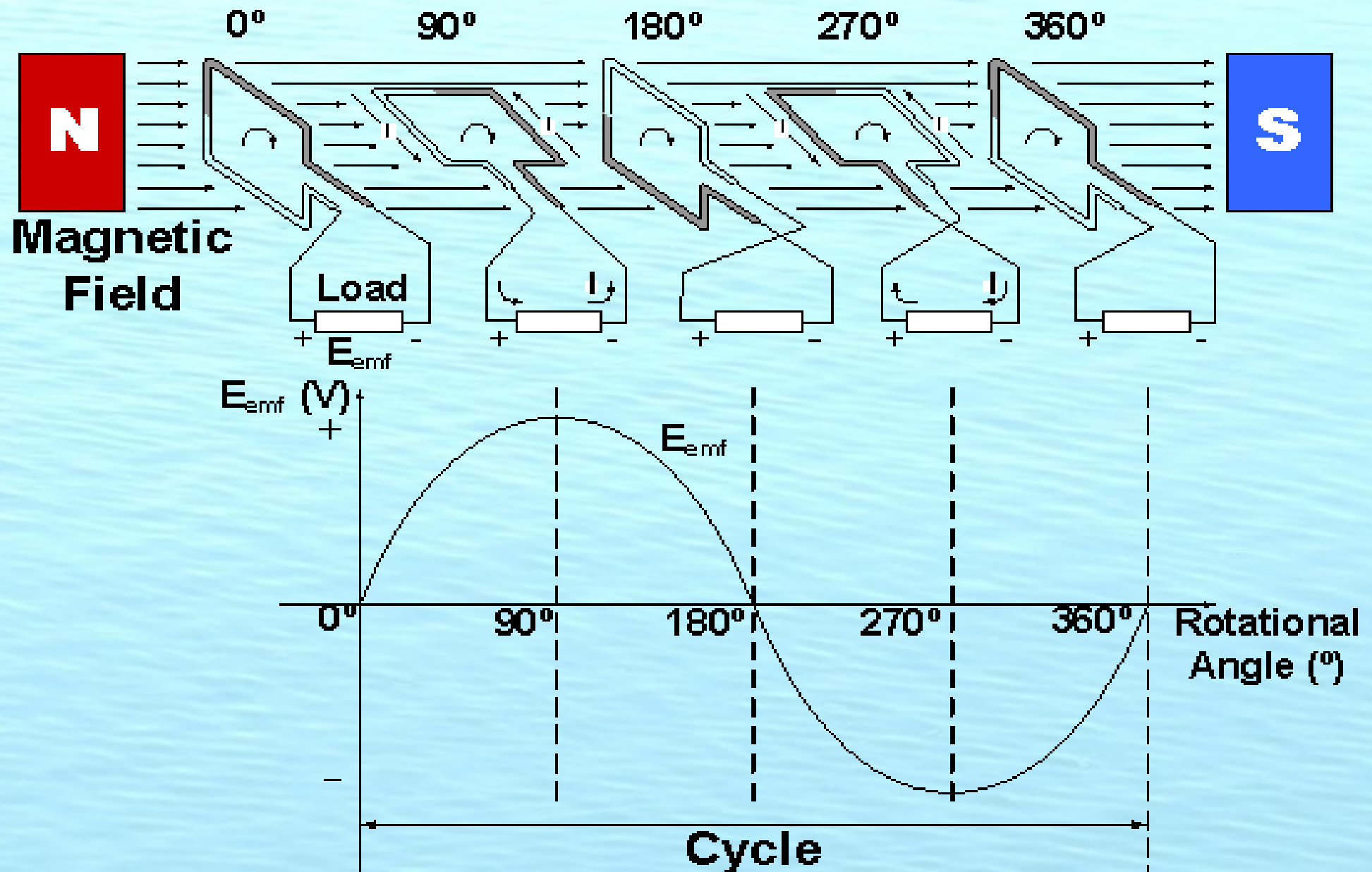
Using Faraday and Henry's discovery of electromagnetic induction, Nikola Tesla and George Westinghouse showed that electricity could be generated in sufficient quantities to light cities.



# Changing flux by rotating loop



# Changing flux by rotating loop



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Changing  $A$ , constant  $B$

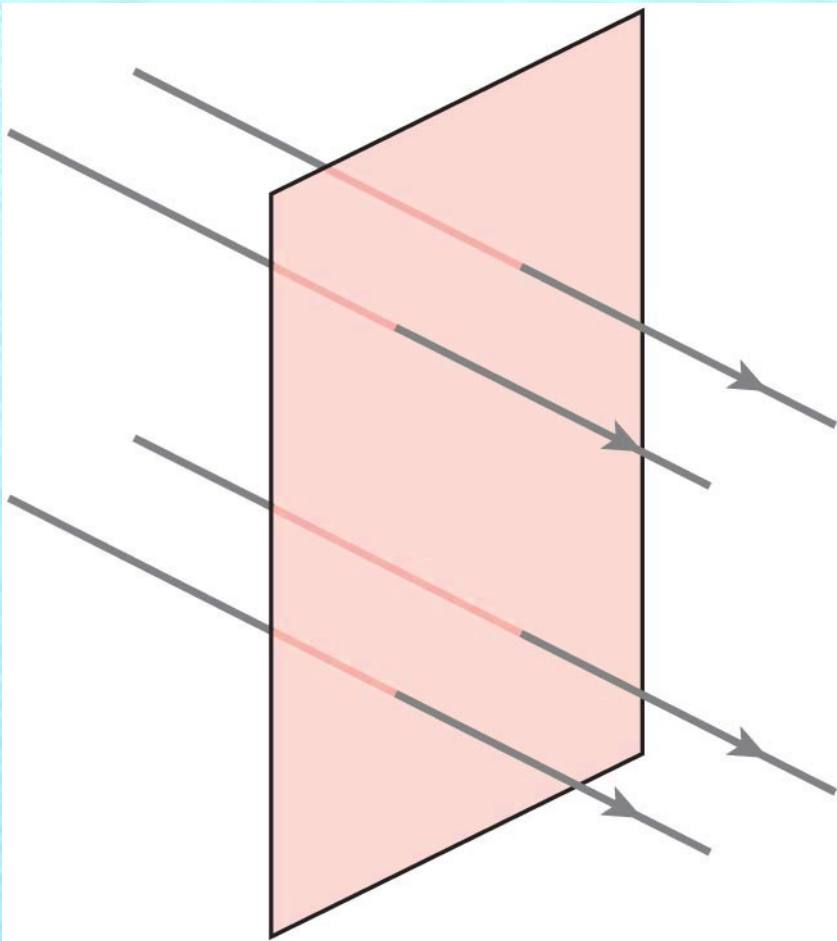
Generators

Constant  $B$ , rotating  $A$

**Rigorous definition of Flux**

# What is magnetic flux?

Flux – flow – like water through a river, or magnetic field lines through a surface.



$$\Phi_E = \int \vec{E} \cdot d\vec{A}$$

$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

For  $B$  uniform  
over area  $A$ :

$$\Phi_B = \vec{B} \cdot \vec{A}$$



# Flux in science and engineering

The word flux comes from Latin: fluxus means "flow",

Electric flux, Magnetic flux amount of E or B-field crossing a unit of area ← **Physics, EE**

Momentum flux, the rate of transfer of momentum across a unit area – Viscosity ← **Mech. E, Chem E.**

Heat flux – Rate of heat flow across a unit area  
--Heat conduction – (Fourier's law) ← **Mech. E.**

Diffusion flux, the # of molecules across a unit area per second – (Fick's law of diffusion) ← **Chem, Bio.**

Volumetric flux, the # of kilograms of water crossing a unit area per second (Darcy's law, groundwater flow)

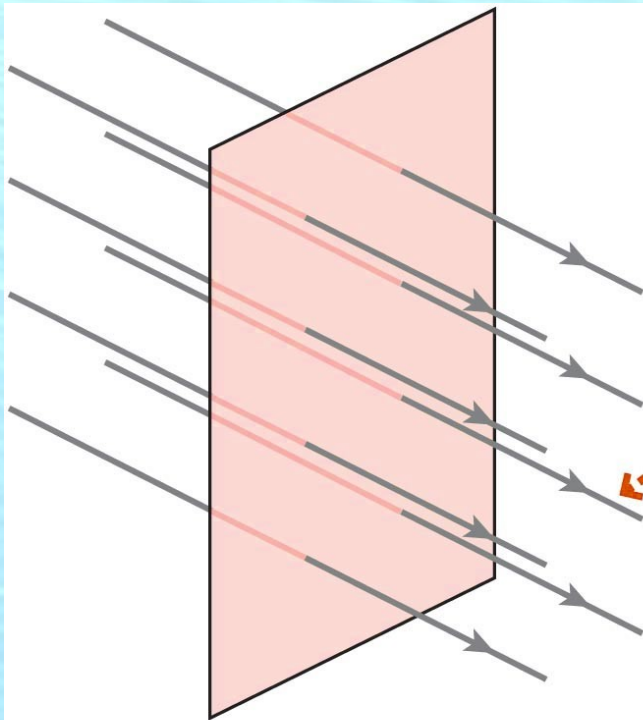
**Hydrology**

# What is flux?

**Flux – flow – like water through a river, or electric field lines through a surface.**

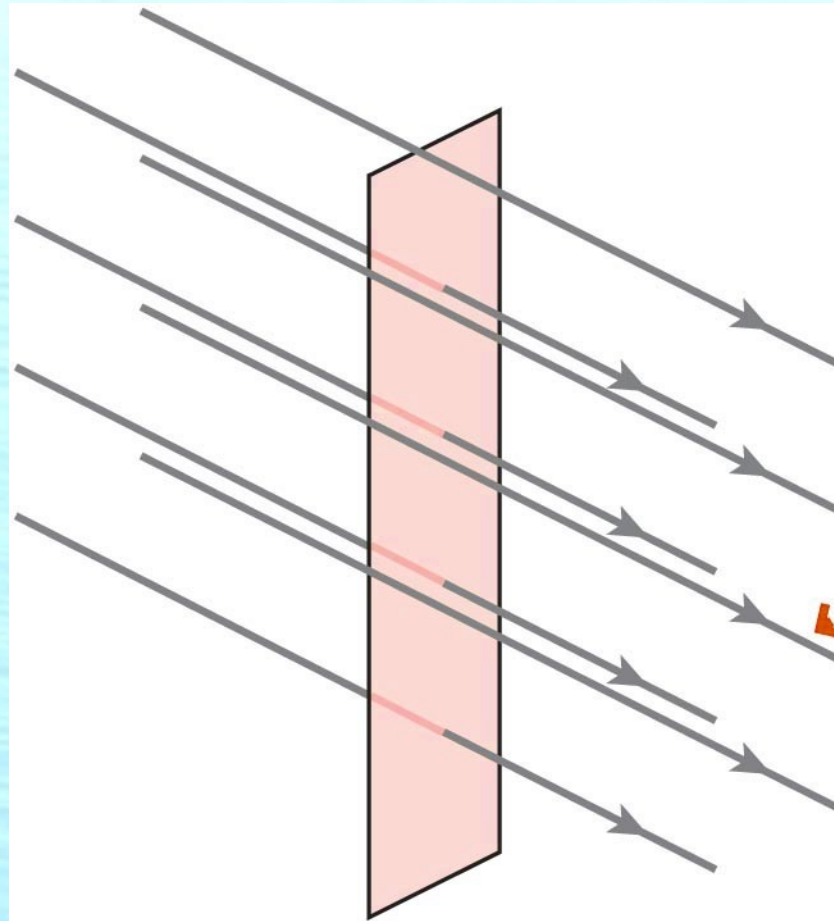
$$\Phi_B = \vec{B} \cdot \vec{A}$$

**With a stronger field than in (a), the flux increases.**



**(b)**

$$\Phi_B = \vec{B} \cdot \vec{A}$$

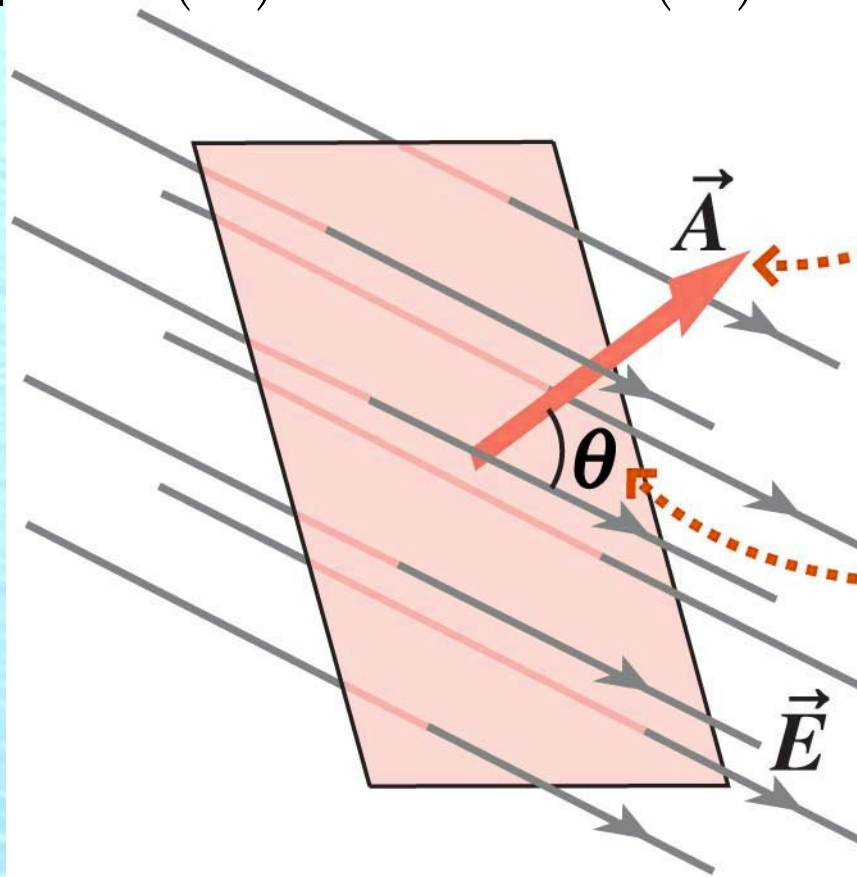


**A smaller surface area than in (b) reduces the flux.**

**(c)**

$$\Phi = \vec{B} \cdot \vec{A}$$

$$\Phi = |\vec{B}| |\vec{A}| \cos(\theta) = B A \cos(\theta)$$



The vector  $\vec{A}$  is perpendicular to the surface and has a magnitude equal to the surface area.

The electric flux  $\Phi$  depends on the angle  $\theta$  between  $\vec{A}$  and  $\vec{E}$ .

(d)

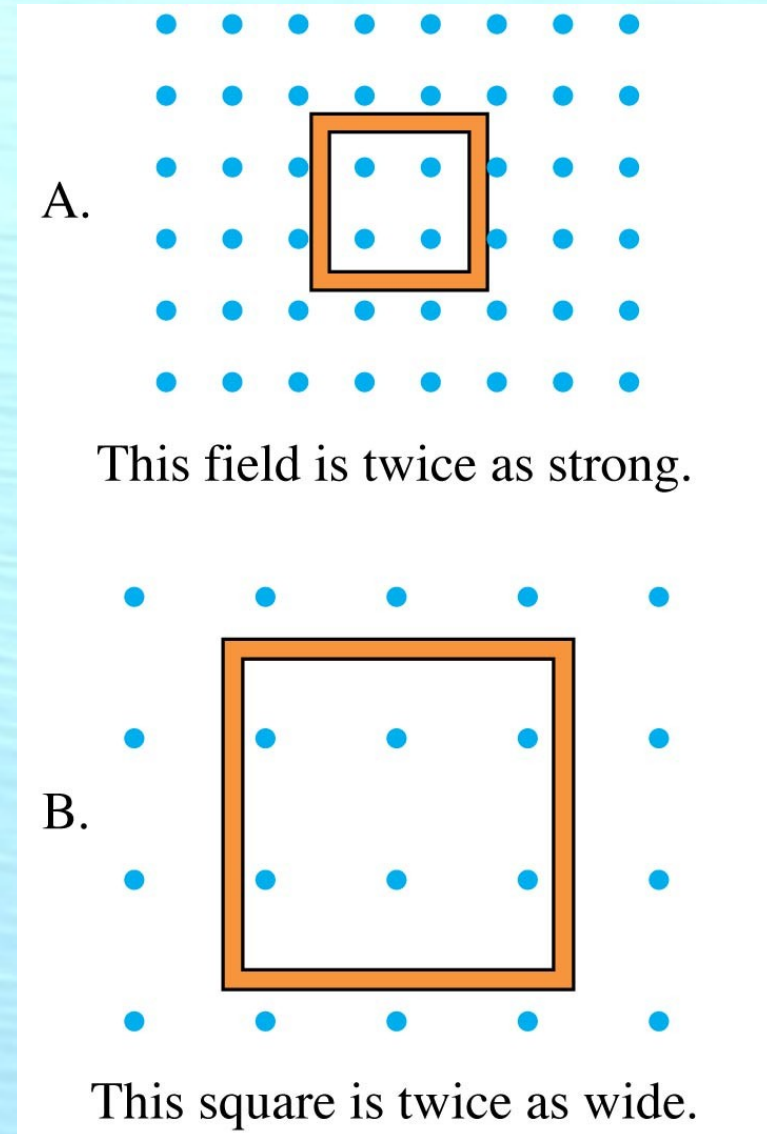
**Flux videos**

[www.youtube.com/user/pelletierphysics](http://www.youtube.com/user/pelletierphysics)

**Electric Flux**

Which loop has the larger magnetic flux through it?

- A. Loop A.
- B. Loop B.
- C. The fluxes are the same.
- D. Not enough information to tell.



## Clicker

Find the flux through a square loop 10 cm on a side with the loop normal at 60 degrees to a uniform 0.08 T magnetic field

(A)  $8 \times 10^0 \text{ T} \cdot \text{m}^2$

(B)  $8 \times 10^{-2} \text{ T} \cdot \text{m}^2$

(C)  $8 \times 10^{-4} \text{ T} \cdot \text{m}^2$

(D)  $6.9 \times 10^{-4} \text{ T} \cdot \text{m}^2$

(E)  $4 \times 10^{-4} \text{ T} \cdot \text{m}^2$

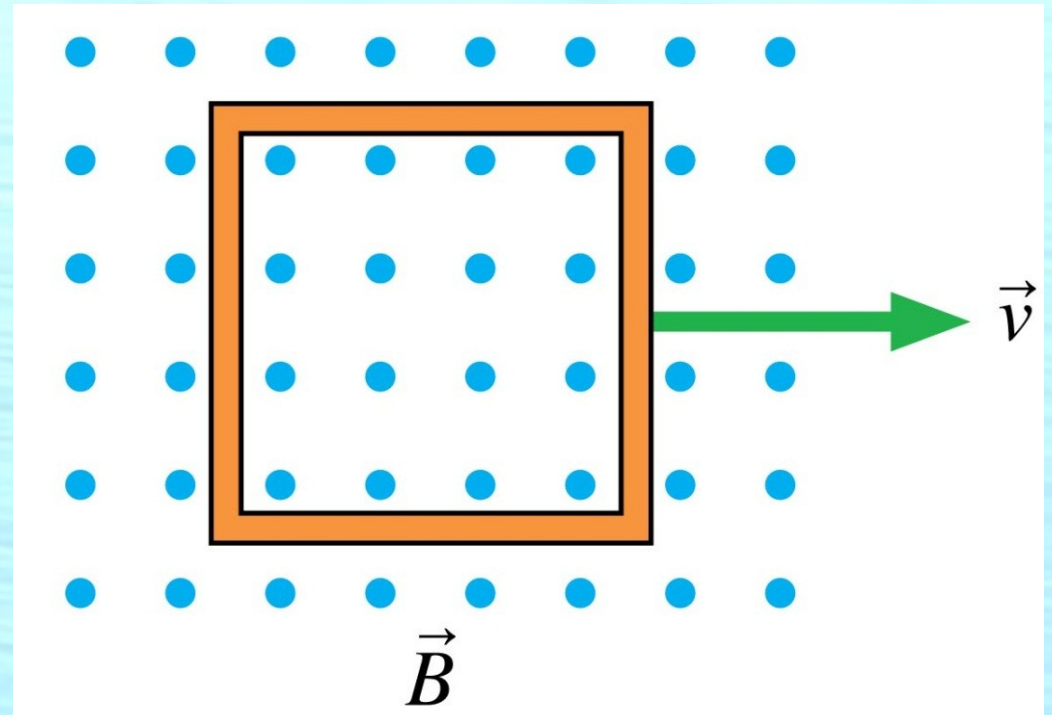
$$\Phi_B = \int \vec{B} \cdot d\vec{A}$$

# Clicker

The metal loop is being pulled through a uniform magnetic field. Is the magnetic flux through the loop changing?

A. Yes.

B. No.

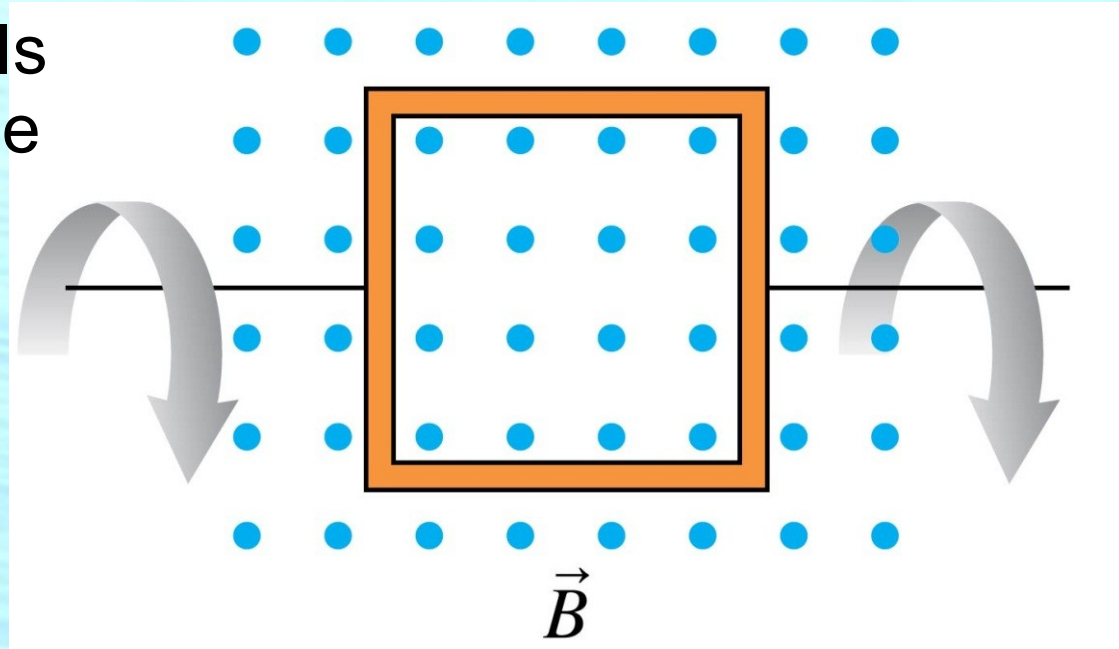




# Clicker

The metal loop is rotating in a uniform magnetic field. Is the magnetic flux through the loop changing?

- A. Yes.
- B. No.



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    Changing  $A$ , constant  $B$

Generators

    Constant  $B$ , rotating  $A$

Rigorous definition of Flux

**Next Time**

Transformers

Connection between Electromagnetism and  
waves