

- Announcements
 - First exam – Tuesday (2/20)
 - Formula sheet / calculators only.
 - Send Canvas message if you need one.
 - Will publish answers to sample test tho' not solutions
- Last Time
 - Gauss's law
 - More about flux and dot products
 - Fields and conductors
 - Gauss's law
 - Field of symmetrical charge configurations
- Today
 - Gauss law tricks
 - Introduction to electric potential

Stress

- Life is stressful, as is college
 - It's OK to ask for help
 - From me, or any prof.
 - From fellow students
 - From relatives
 - From special crisis counselors
 - Text 741741 for instant crisis connection 24/7
 - Call New Mexico “warm line” 24/7
855-466-7100
“I just need to talk”
 - LGBTQ 866-485-7386
 - Socorro Mental Health 575-835-2444







Gauss's law

“The total flux through any closed surface is equal to the enclosed charge over epsilon naught”.

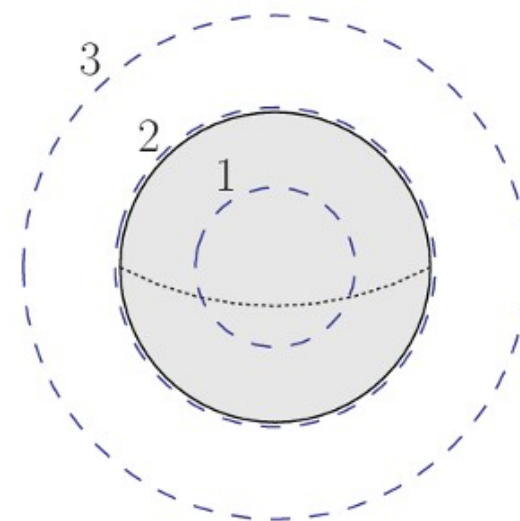
$$\Phi_{\text{total}} = \int \vec{E} \cdot d\vec{A} = \frac{q_{\text{enclosed}}}{\epsilon_0}$$



Online HW #4: Gauss's Law Begin Date: 2/9/2024 8:00:00 AM -- Due Date: 2/15/2024 11:59:00 PM End Date: 5/29/2024 11:59:00 PM

(13%) **Problem 7:** The figure shows a sphere carrying a uniformly distributed volume charge Q . Three Gaussian surfaces are concentric with the sphere as shown.

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A message from your instructor

Problem 7: The trick here is that not all the surfaces enclose all the charge.

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50% Part (a) Which Gaussian surface(s) has the greatest electric flux through it?

- | | |
|---|-------------------------------|
| <input type="radio"/> 2 and 3 | <input type="radio"/> 1 |
| <input type="radio"/> They all have the same electric flux. | <input type="radio"/> 3 |
| <input type="radio"/> 2 | <input type="radio"/> 1 and 2 |

Submit

Hint

Feedback

I give up!

Hints: **0%** deduction per hint. Hints remaining: **2**

Feedback: **0%** deduction per feedback.

Grade Summary

Deductions **0%**
Potential **100%**

Submissions

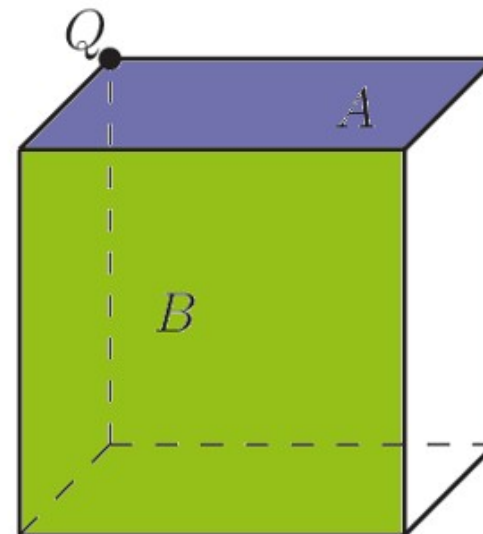
Attempts remaining: **5**
(**20%** per attempt)
[detailed view](#)

Instructor/TA Admin

50% Part (b) On which of Gaussian surface is the electric field the greatest?

(13%) **Problem 8:** A point charge is positioned at the very corner of a cube as shown in the figure.

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A message from your instructor

Problem 8: This one is very cute, but a bit tricky. I recommend waiting till I discuss this in class.

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▶ ⚠ **50% Part (a)** What is the electric flux though the side A (the top) of the cube?

- $Q/(8\epsilon_0)$
- $Q/(24\epsilon_0)$
- $Q/(3\epsilon_0)$
- $Q/(6\epsilon_0)$
- $Q/(12\epsilon_0)$
- 0

Submit

Hint

Feedback

I give up!

Hints: 0% deduction per hint. Hints remaining: 1

Feedback: 0% deduction per feedback.

Instructor/TA Admin

▶ ⚠ **50% Part (b)** What is the electric flux though the side B (the front) of the cube?

Grade Summary

Deductions **0%**
Potential **100%**

Submissions

Attempts remaining: **5**
(**20%** per attempt)
[detailed view](#)

Gauss's law for symmetrical cases

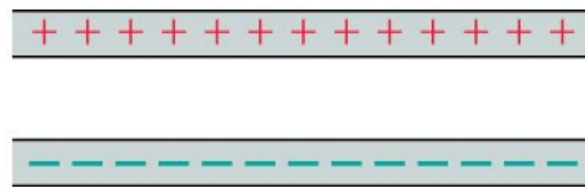
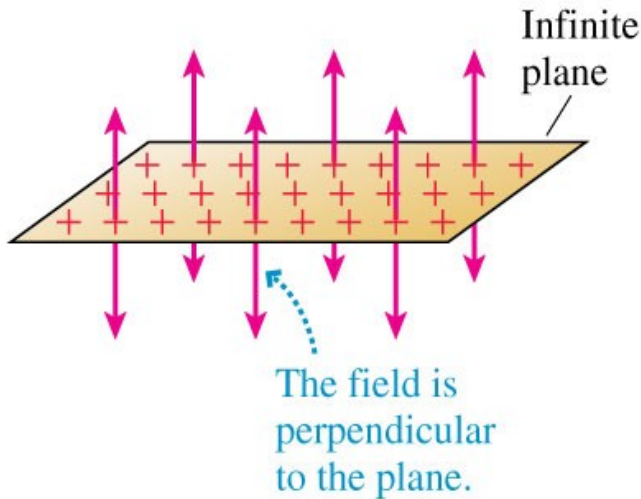
“The total flux through any closed surface is equal to the enclosed charge over epsilon naught”.

$$E \times (\text{Surface Area}) = \frac{q_{\text{enclosed}}}{\epsilon_0}$$



$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{k}$$

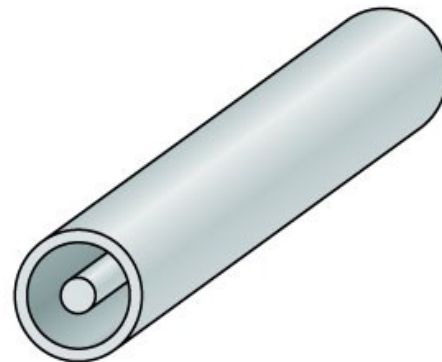
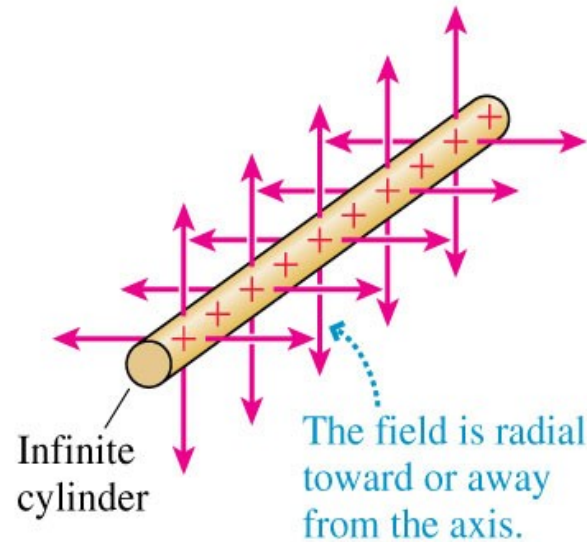
Planar symmetry



Infinite parallel-plate capacitor

$$\vec{E} = \frac{\lambda}{2\pi r \epsilon_0} \hat{r}$$

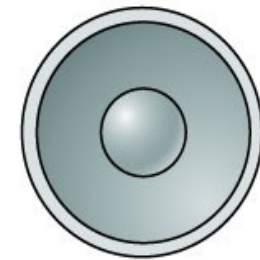
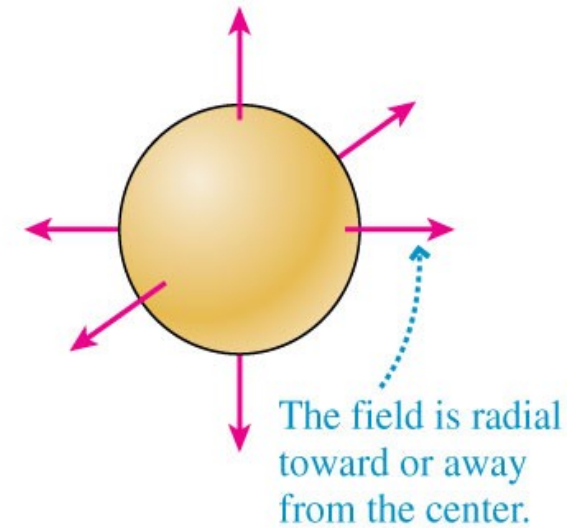
Cylindrical symmetry



Coaxial cylinders

$$\vec{E} = \frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

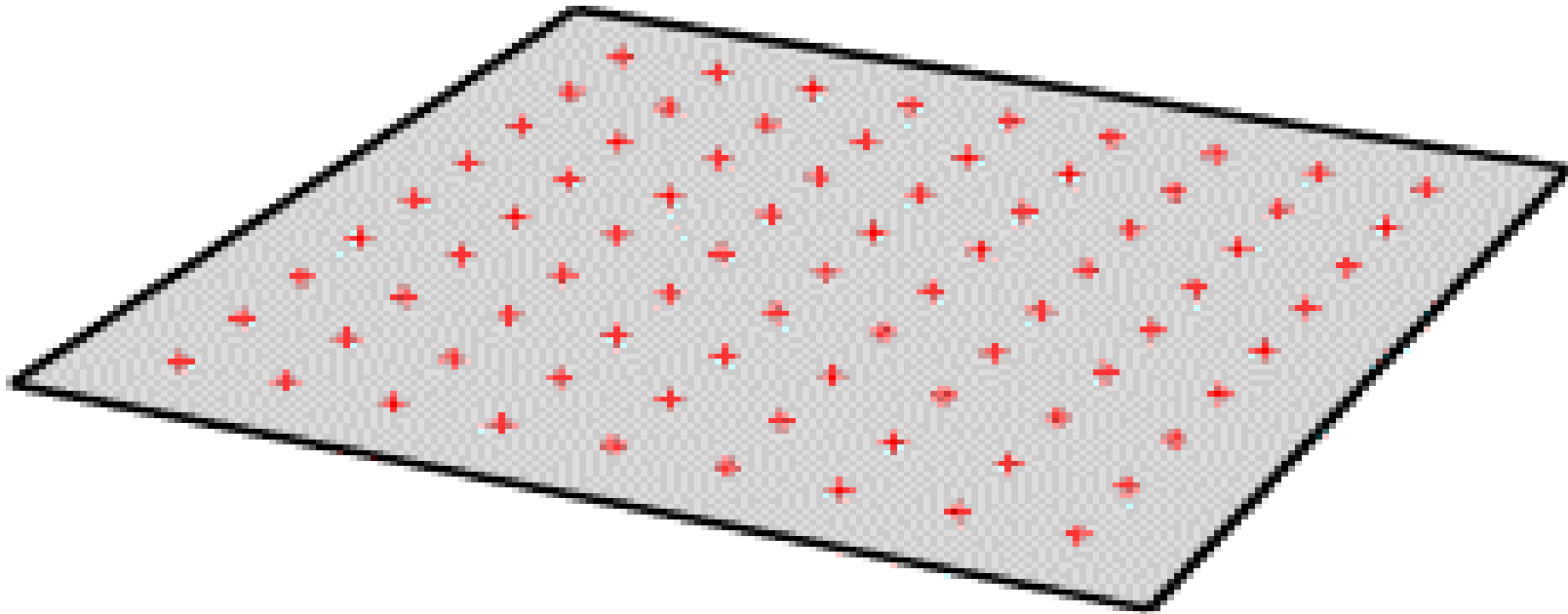
Spherical symmetry



Concentric spheres

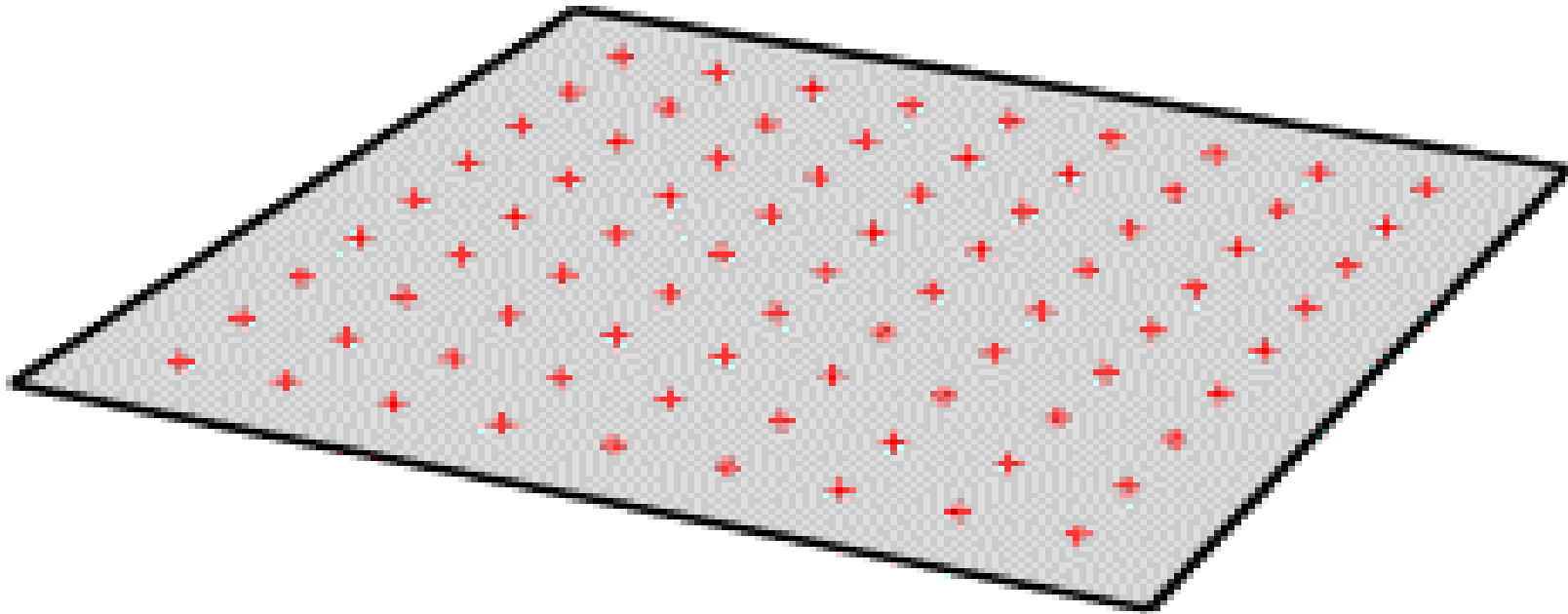
Relation between symmetry and Electric Field

Imagine an infinite plane of charge.



Relation between symmetry and Electric Field

Because you can't tell what direction you are facing, the field must be **ONLY** Perpendicular to the plane.

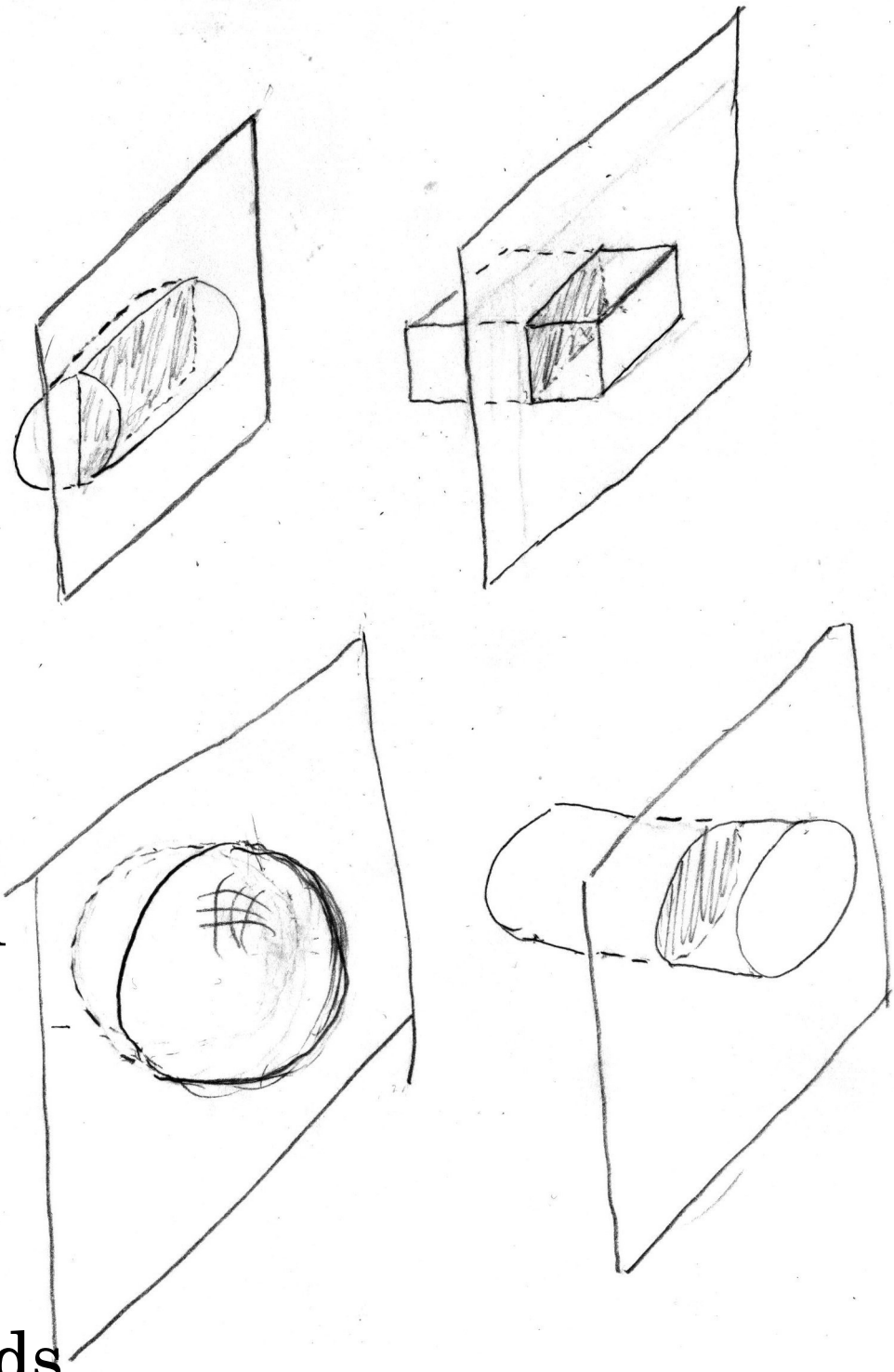


Why would I want a Gaussian surface?

A Gaussian surface is any surface that encloses some of a charge distribution.

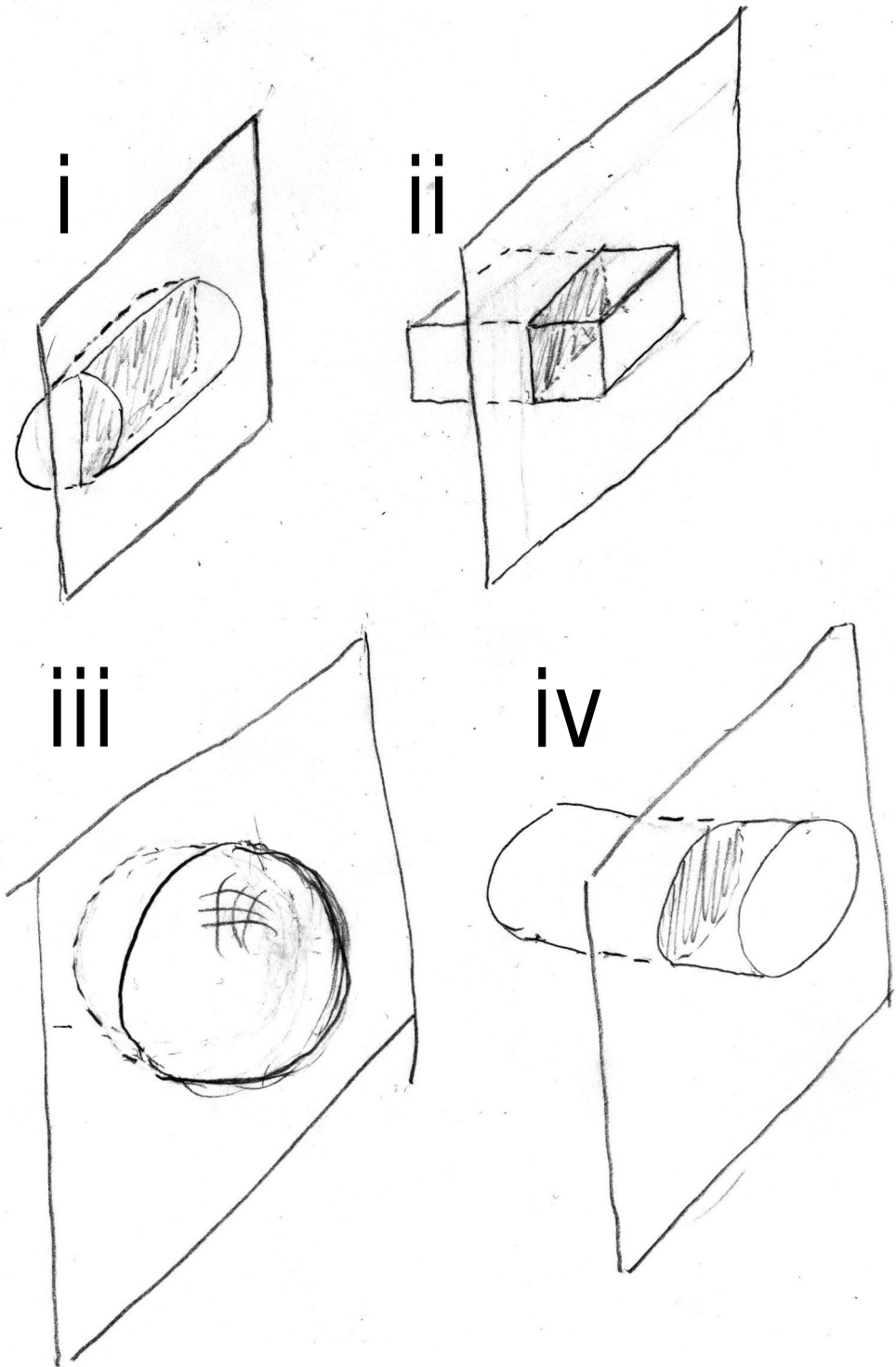
You draw it to have the correct symmetry to turn the surface integral into mere multiplication.

It can lead directly to a formula or provide insight into the behavior of materials in electric fields.

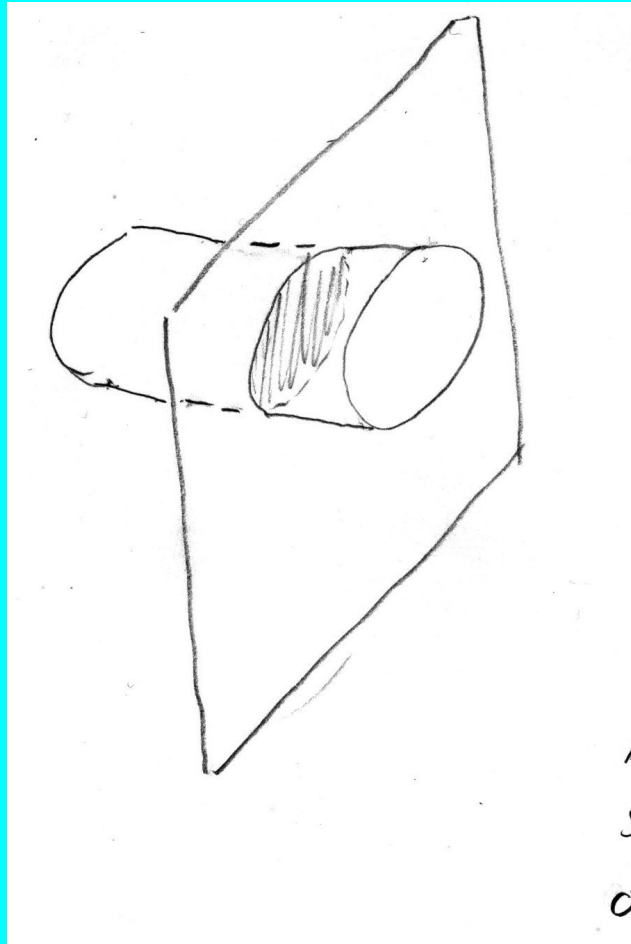


Which of these surfaces are best to calculate the field of a charged plate?

- (A) i
- (B) i or ii
- (C) ii or iii
- (D) i or iv
- (E) ii or iv



Symmetrical Case: Large (infinite) Plane



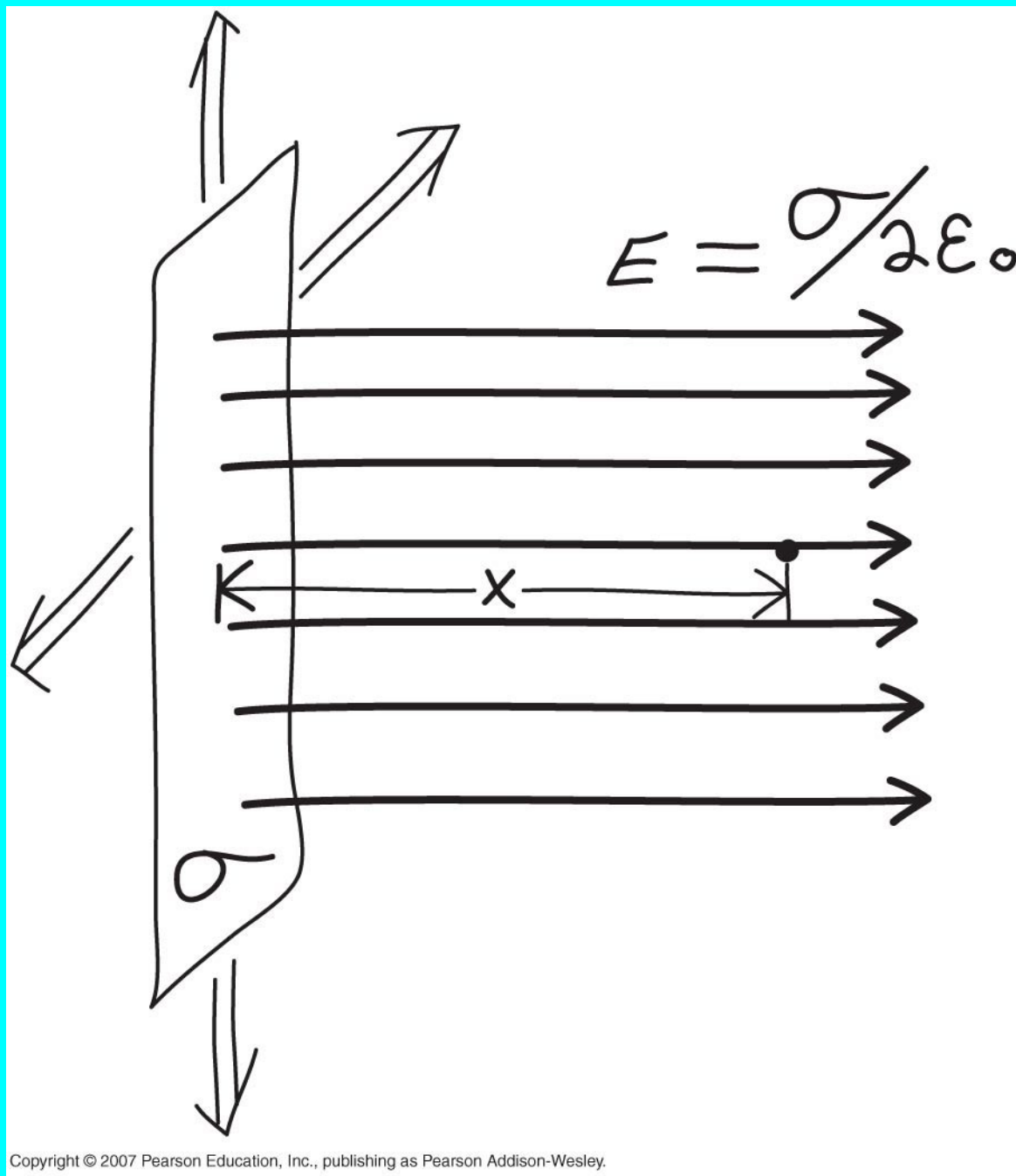
Infinite Plane

A square plate is 10 meters on a side and has a total charge of 8.85 mC. You are 1 cm away from its middle. What is the electric field magnitude?

- (A) 8.85×10^{-5} N/C
- (B) 4.43×10^{-5} N/C
- (C) 5.00×10^6 N/C
- (D) 1.00×10^7 N/C
- (E) 1.00×10^8 N/C

Infinite Plane

A square plate is 10 meters on a side and has a total charge of 8.85 mC. You are 1 cm away from its middle. What is the electric field magnitude?



An infinite sheet of charge creates a field of 10000 V/m.

An electron moves 10 cm in this field.

What is the final speed of the electron?

$$m_e = 9.0 \times 10^{-31} \text{ kg}$$

Electric Potential: What's a volt anyway?



Electric Potential:

Is also called voltage. They are the same thing.

Electric potential is measured in Volts. (SI unit)

The term potential ties back to potential energy because potential IS the potential energy per unit charge.

$$U = QV \quad V = \frac{U}{Q}$$

Electric Potential and Electric field:

We did a similar trick with electric field and force

Electric field ties back to force because field is the force per unit charge.

$$U = QV \qquad V = \frac{U}{Q}$$
$$\vec{F} = Q\vec{E} \qquad \vec{E} = \frac{\vec{F}}{Q}$$

You have a 12.0-V motorcycle battery that can move 5000 C of charge, and a 12.0-V car battery that can move 60,000 C of charge. How much energy does each deliver?

- (A) 60 and 720 kiloJoules
- (B) 5 and 60 kiloJoules
- (C) 417 and 5000 Joules
- (D) 417 and 5000 Watts
- (E) Both the same because both 12 Volts



In a large lightning flash, the potential difference between a cloud and the ground is 100 Million Volts and the quantity of charge transferred is 30 C.

How much potential energy is Released?



To what speed could you accelerate a 2000 kg car with this much energy?

- (A) 1.73 m/s
- (B) 12.2 m/s
- (C) 122 m/s
- (D) 1730 m/s
- (E) Mach 2



Electric potential is usually expressed in Volts, but it can be expressed in terms of other SI Units.

What other units are appropriate for electric potential?

(A) $\frac{\text{N}}{\text{C}}$

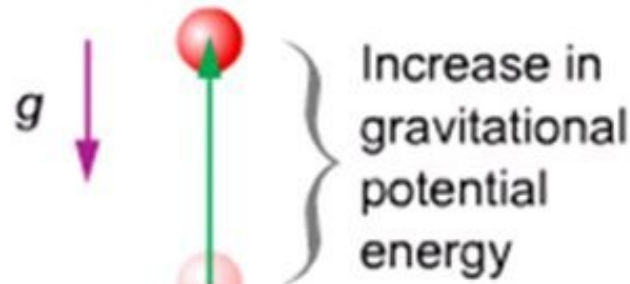
(B) $\frac{\text{V}}{\text{m}}$

(C) $\frac{\text{J}}{\text{C}}$

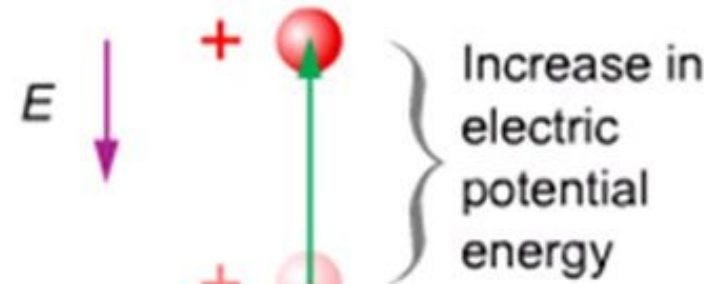
(D) $\text{N}\cdot\text{m}$

Potential Energy

High PE



Low PE

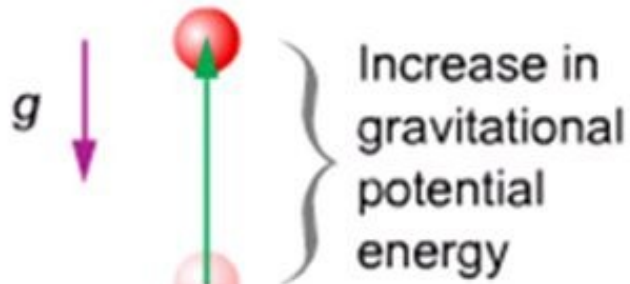


Doing work against a gravity field raises the gravitational potential energy of a mass

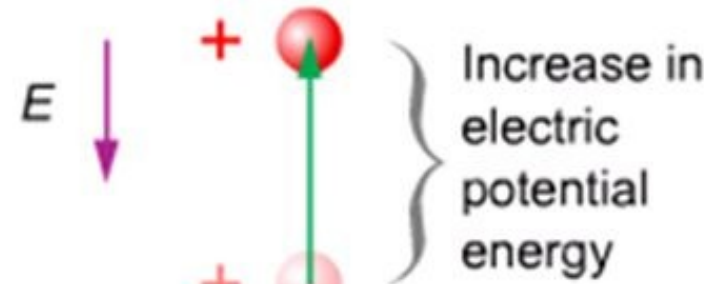
Doing work against an electric field raises the electric potential energy of a charge

Potential Energy

High PE



Low PE



$$\vec{F} = m \vec{g}$$

$$U = m g h$$

$$\text{geopotential} = g h$$

$$\vec{F} = Q \vec{E}$$

$$U = Q E h$$

$$V = E h$$

1. If a proton is moved in the same direction as the electric field, what happens to its electric potential energy?

- a. Increases
- b. Decreases
- c. Accelerates
- d. Stays the same

POSITIVE MASS

**GRAVITY
FIELD**

GRAVITATIONAL

1. If a ~~proton~~ is moved in the same direction as the ~~electric field~~, what happens to its ~~electric~~ potential energy?

- a. Increases
- b. Decreases
- c. Accelerates
- d. Stays the same

Work, Potential Energy, and Kinetic Energy

$$W = \vec{F} \cdot \Delta \vec{r} = -\Delta U$$

$$W = \Delta KE = \frac{1}{2} m v_{\text{FINAL}}^2 - \frac{1}{2} m v_{\text{INITIAL}}^2$$

$\Delta U + \Delta KE$ is constant!

Gravity and Electrostatic Force are both CONSERVATIVE

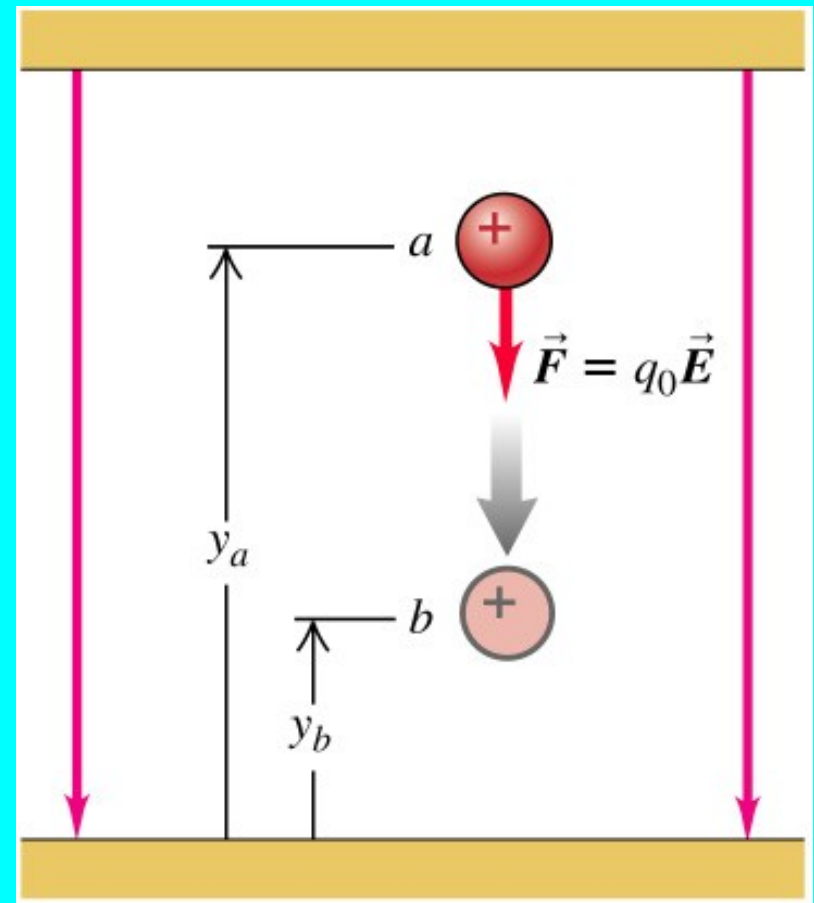
When a positive charge moves in the direction of the electric field,

A. the field does positive work on it and the potential energy increases

B. the field does positive work on it and the potential energy decreases

C. the field does negative work on it and the potential energy increases

D. the field does negative work on it and the potential energy decreases



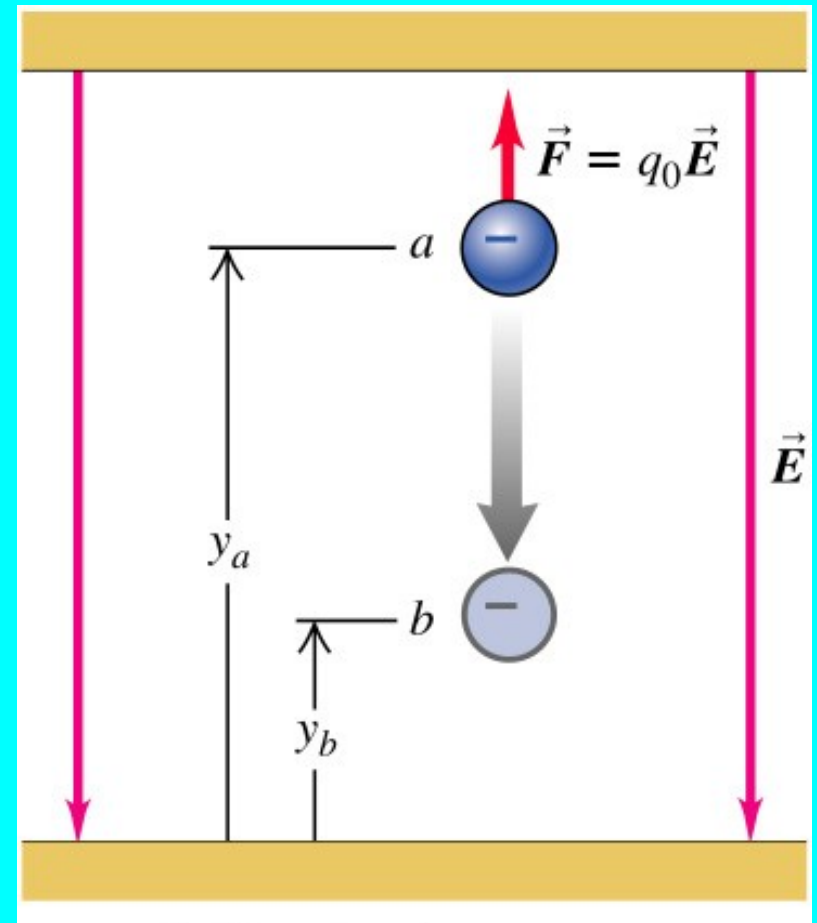
When a negative charge moves in the direction of the electric field,

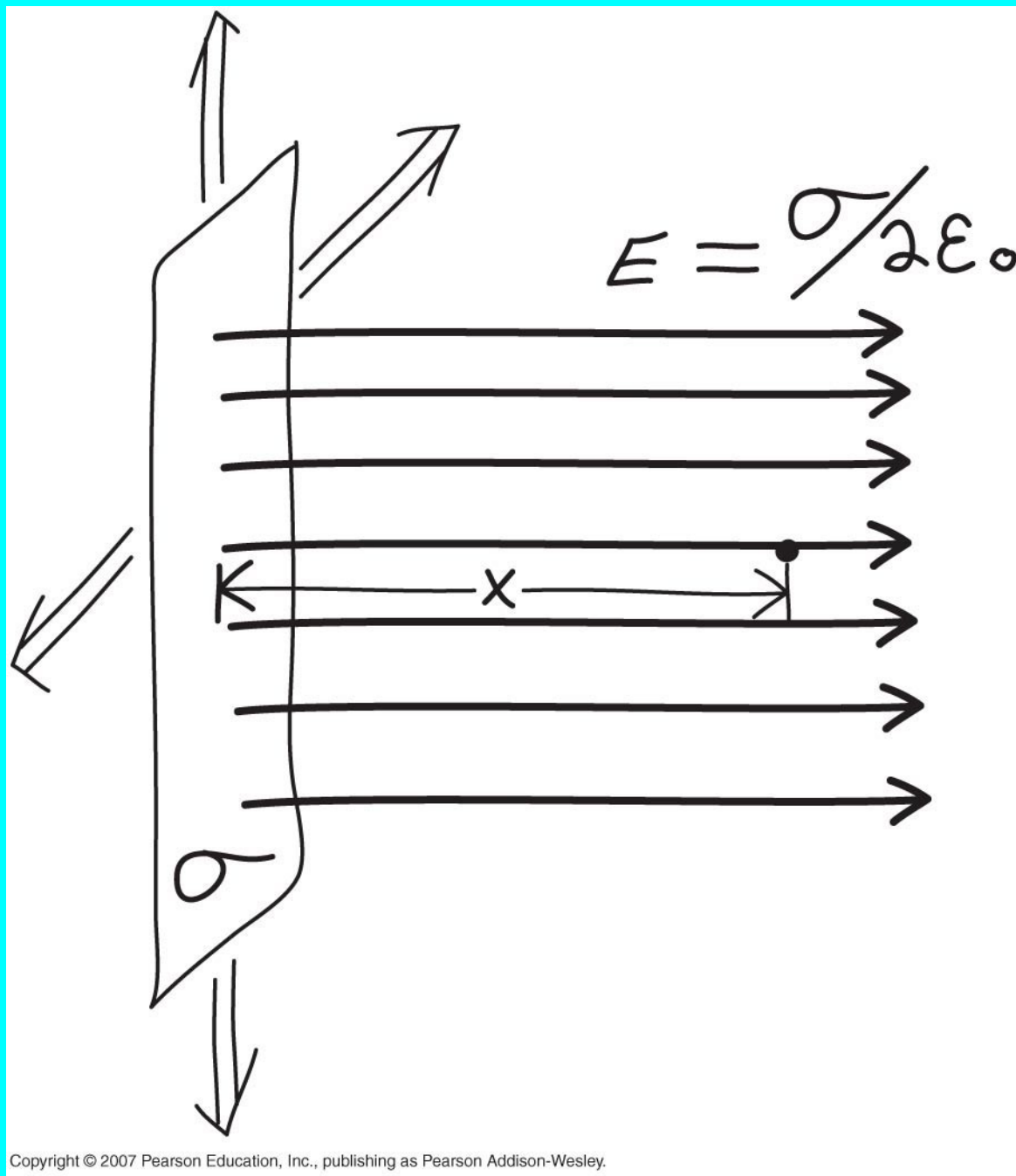
A. the field does positive work on it and the potential energy increases

B. the field does positive work on it and the potential energy decreases

C. the field does negative work on it and the potential energy increases

D. the field does negative work on it and the potential energy decreases





An infinite sheet of charge creates a field of 10000 V/m.

An electron moves 10 cm in this field.

What is the final speed of the electron?

$$m_e = 9.0 \times 10^{-31} \text{ kg}$$

What does work have to do with Electric Potential?

$$W = \vec{F} \cdot \Delta \vec{r} = Q \vec{E} \cdot \Delta \vec{r}$$

What if force or Electric field are not constant?

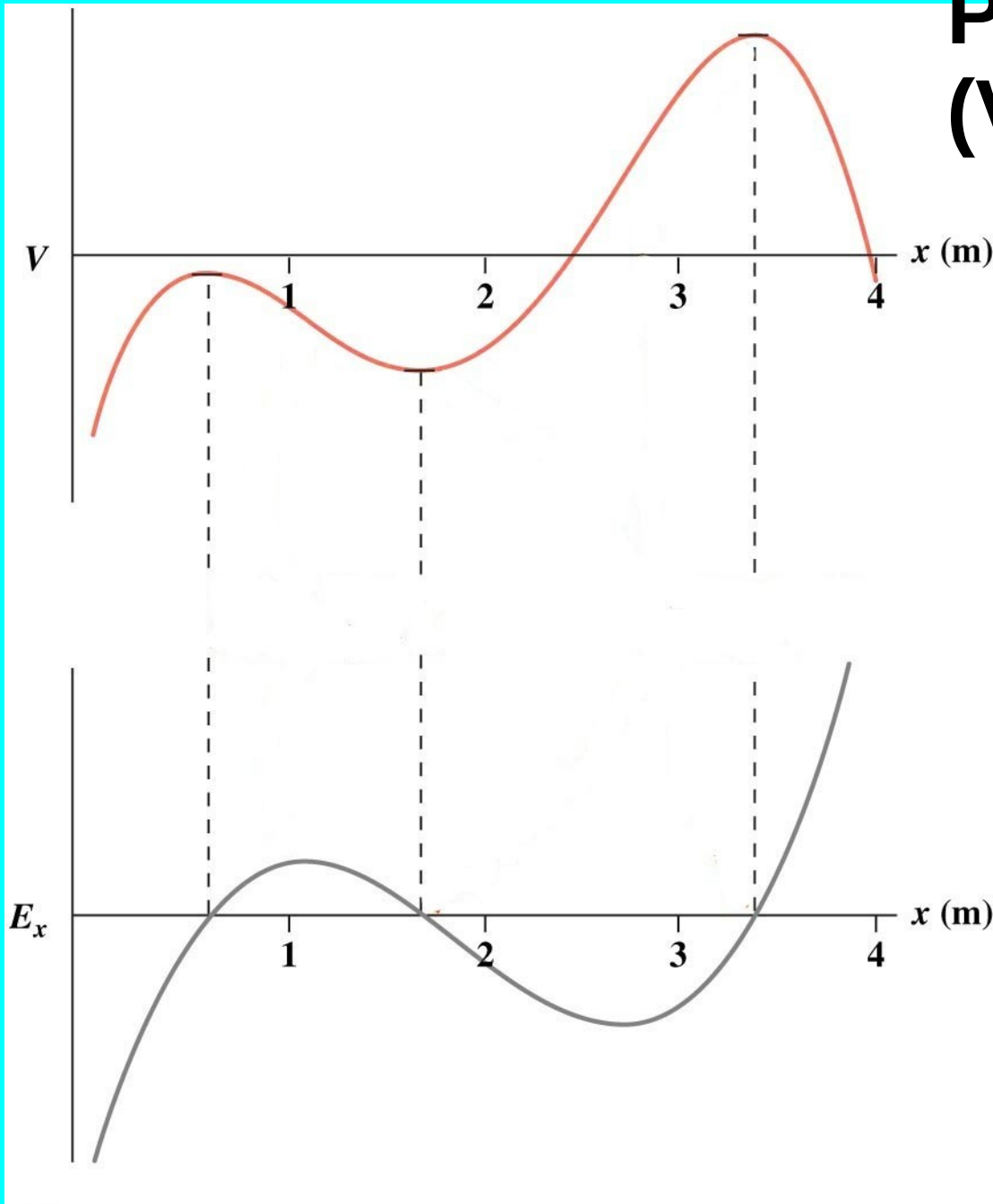
$$W = \int \vec{F} \cdot d\vec{r} = Q \int \vec{E} \cdot d\vec{r}$$

$$\Delta U = -W = QV = -Q \int \vec{E} \cdot d\vec{r}$$

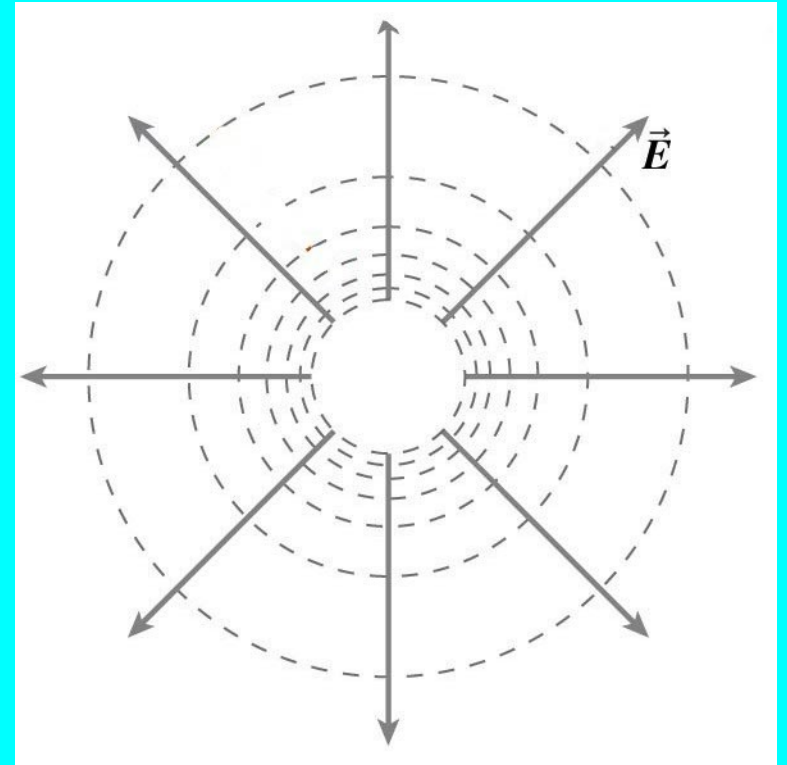
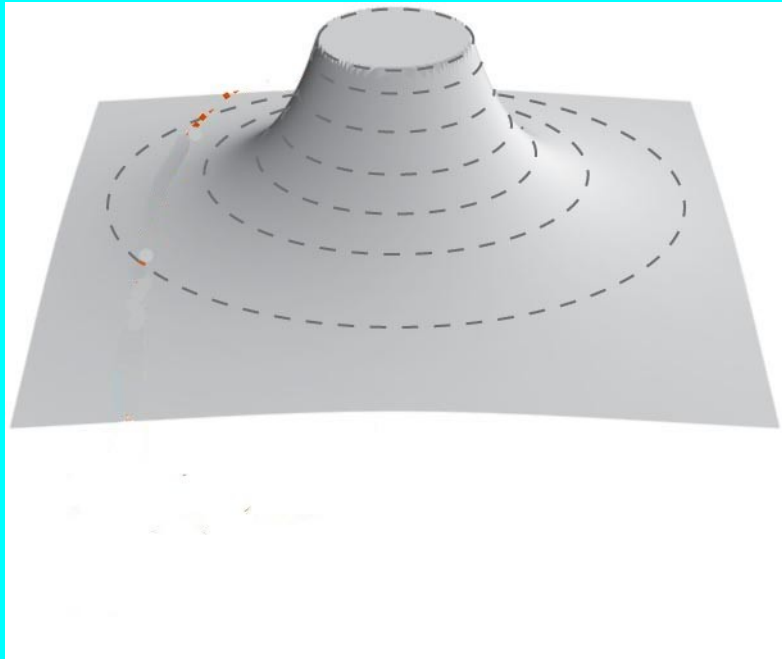
$$\text{therefor } V \stackrel{\text{def}}{=} - \int \vec{E} \cdot d\vec{r}$$

Potential (Voltage) in 1-D

$$V(x) = -\int E_x dx$$



$$E_x = -\frac{dV}{dx}$$



Work, Potential Energy, and Kinetic Energy

$$W = \vec{F} \cdot \Delta \mathbf{r} = -\Delta U$$

$$W = \Delta KE = \frac{1}{2} m v_{\text{FINAL}}^2 - \frac{1}{2} m v_{\text{INITIAL}}^2$$

$\Delta U + \Delta KE$ is constant!

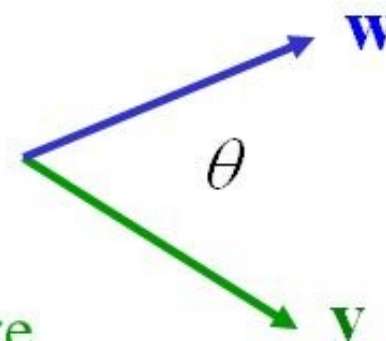
Gravity and Electrostatic Force are both CONSERVATIVE

Dot Products

There are two ways to multiply two vectors

- The dot product produces a scalar quantity
 - It has no direction
 - It can be pretty easily computed from geometry
 - It can be easily computed from components

$$\mathbf{v} \cdot \mathbf{w} = vw \cos \theta = v_x w_x + v_y w_y + v_z w_z$$



- The dot product of two unit vectors is easy to memorize

$$\hat{\mathbf{i}} \cdot \hat{\mathbf{i}} = \hat{\mathbf{j}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{k}} = 1$$

$$\hat{\mathbf{i}} \cdot \hat{\mathbf{j}} = \hat{\mathbf{j}} \cdot \hat{\mathbf{i}} = 0$$

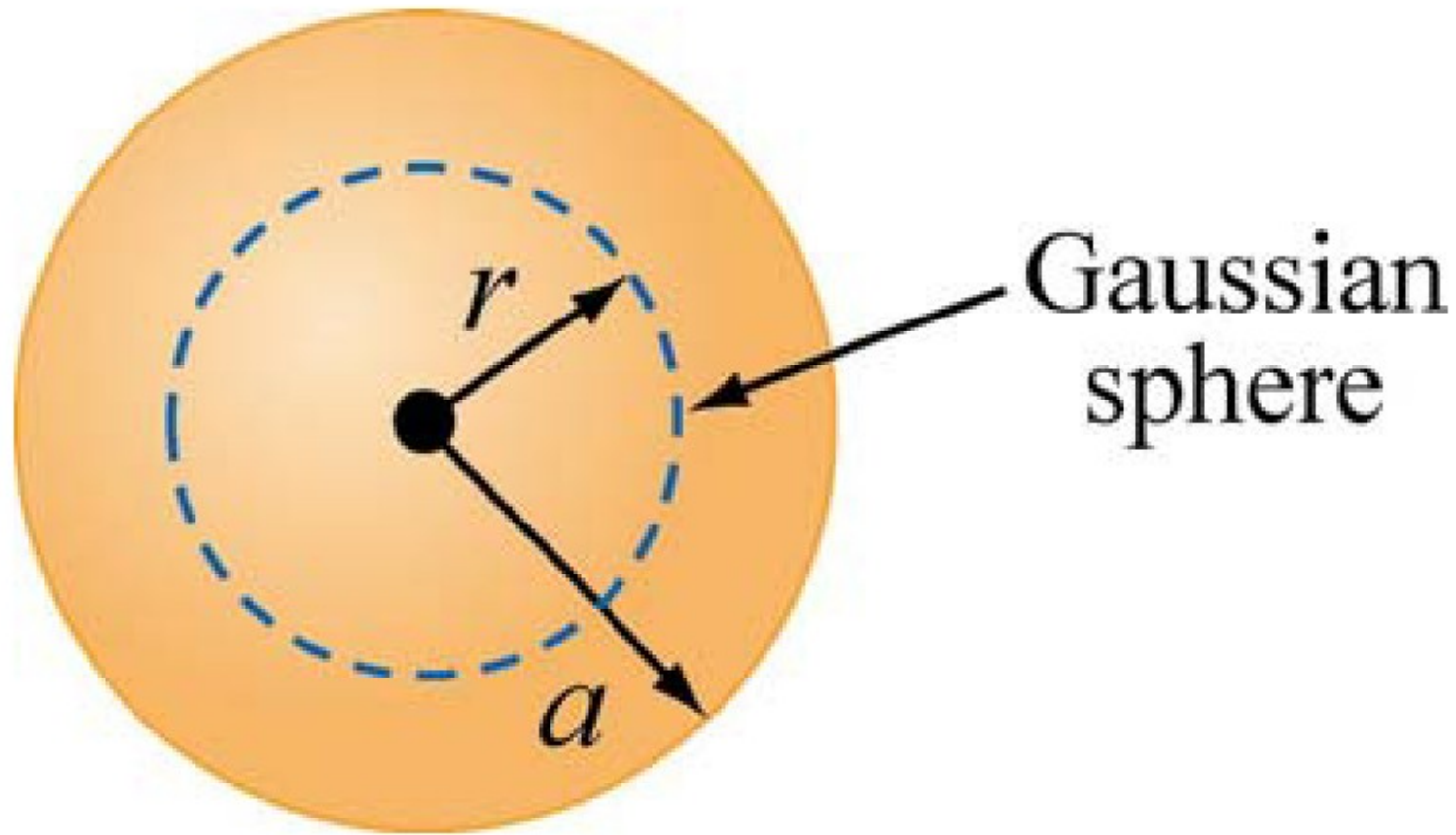
$$\hat{\mathbf{i}} \cdot \hat{\mathbf{k}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{i}} = 0$$

$$\hat{\mathbf{j}} \cdot \hat{\mathbf{k}} = \hat{\mathbf{k}} \cdot \hat{\mathbf{j}} = 0$$

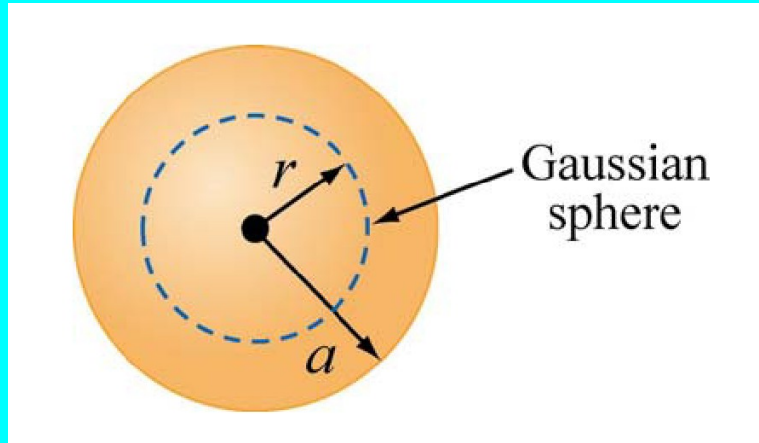
- The dot product is commutative

$$\mathbf{v} \cdot \mathbf{w} = \mathbf{w} \cdot \mathbf{v}$$

What about a solid sphere of charge?



What about a solid sphere of charge?



What about a solid sphere of charge?

What about a solid sphere of charge?

