Lecture 04: 01/25/2024

- Announcements
  - Written HW#1 due midnight tonight
  - Written HW#2 date corrected (next Thursday)
  - Online HW#2 next Tuesday

- Last Time
  - Types of charge
  - Tribocharging
  - Insulators and Conductors

- Today
  - Coulomb's Law
    - Coulomb vector form and r-hat
    - Superposition

iClicker

- We had 45 clickers last time. There are 51 students.
- Has everyone got a clicker? Please see me if have issues.

Coulomb's Law

$$F = k \frac{q_1 q_2}{r^2}$$

$$k = 8.99 \times 10^9 \frac{N\,m^2}{C^2}$$

Forces in Hydrogen atom

A hydrogen atom is composed of a proton and an electron with equal charges. The proton has roughly 1800 times the electron mass.
Compare the forces on electron and proton.

(A) The electron feels a greater force because it orbits the nucleus.

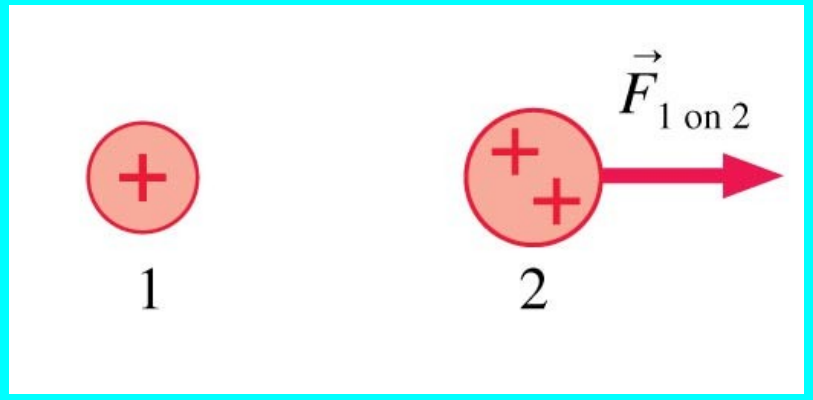
(B) The proton feels a greater force because it is larger and has a larger surface area.

(C) Depends on whether the atom is in a molecule.

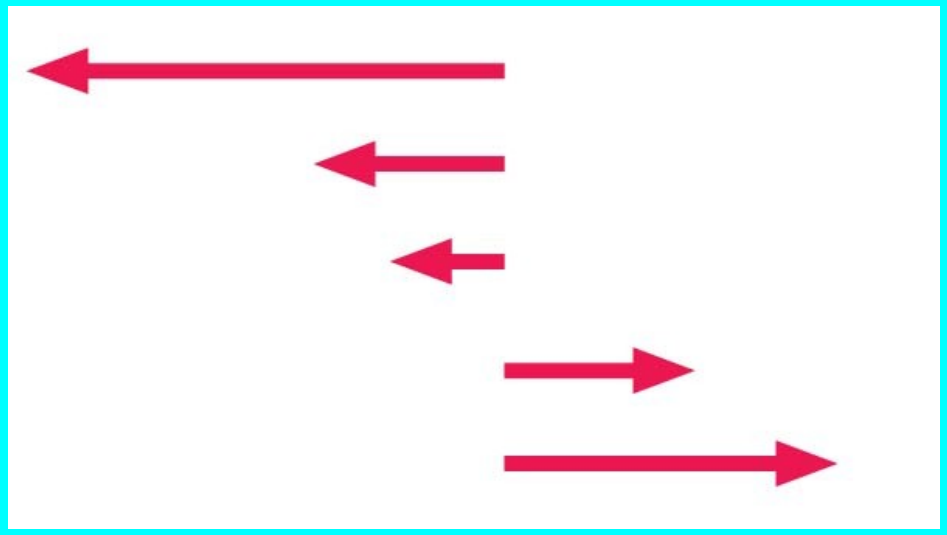
(D) The electron and proton feel the same force because coulomb's law is symmetrical.

Coulomb's Law for Unequal charges

The charge of sphere 2 is twice that of sphere 1. Which vector below shows the force of 2 on 1?

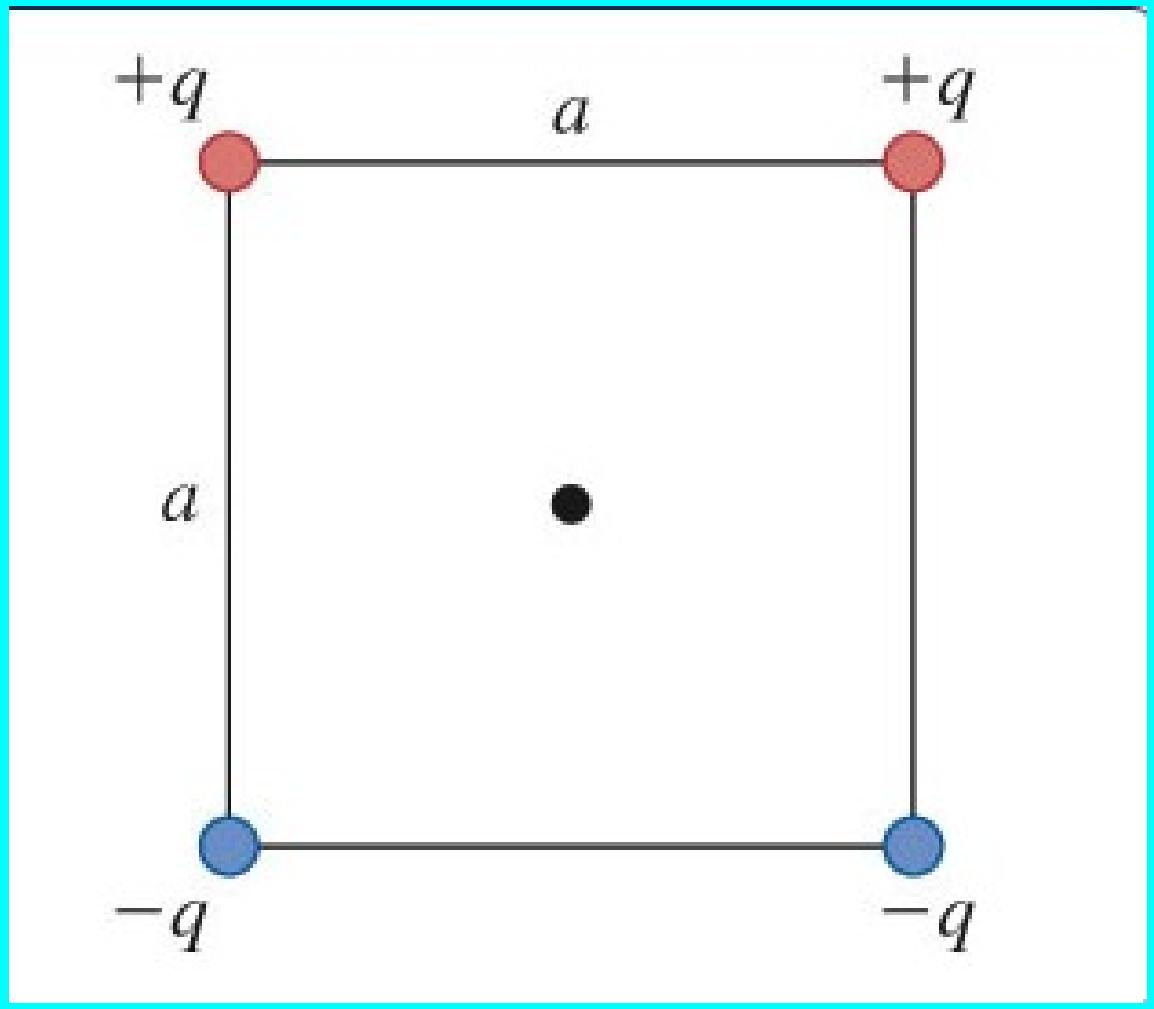


A.
B.
C.
D.
E.



$$\vec{F}_{12} = k \frac{q_1 q_2}{r_{12}^2} \hat{r}_{12}$$

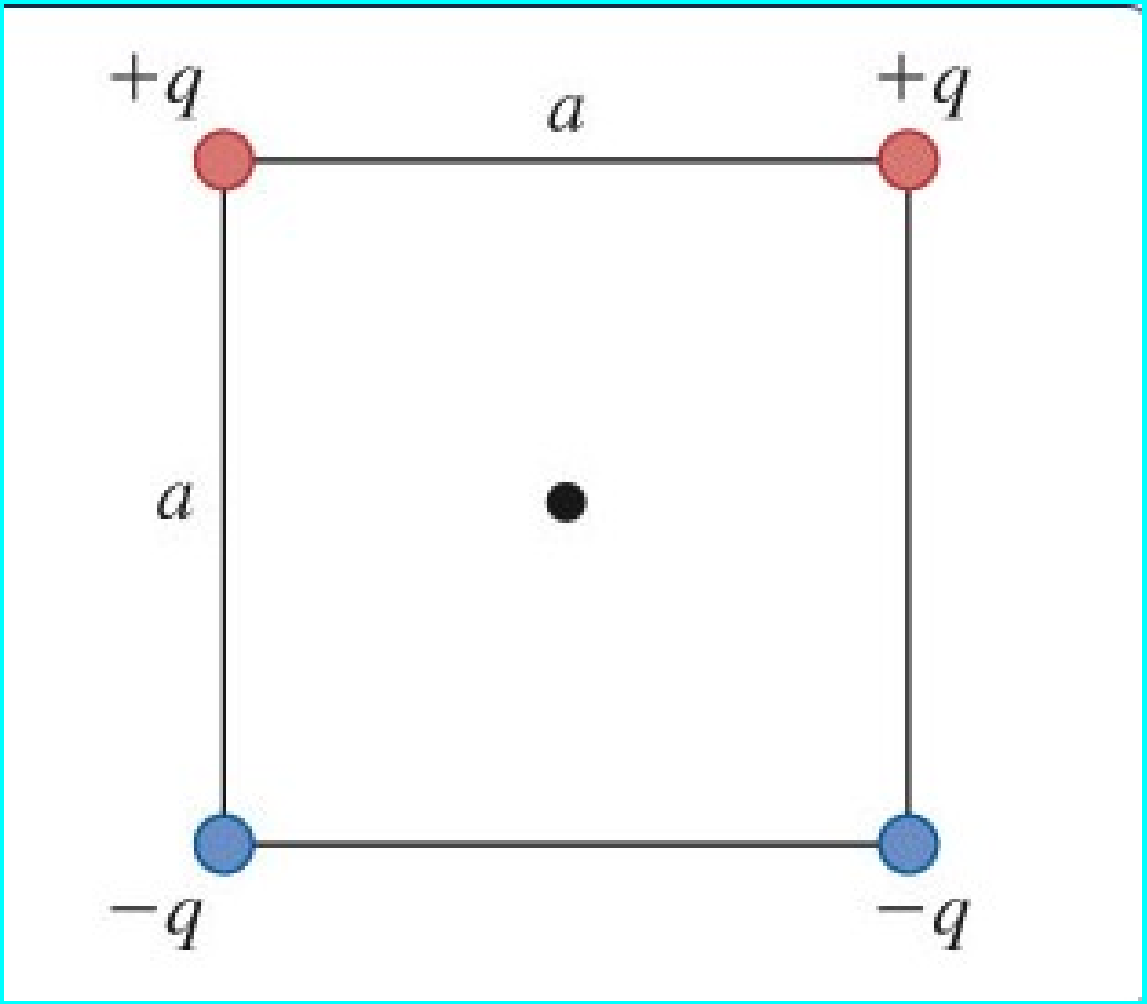
Electric Field Superposition



Charges are arranged on the corners of a square. The magnitude of all ‘q’s is the same.

Find the direction of the force on a positive charge in the center of the square.

Electric Field Superposition



For charges arranged as in previous question, find direction of force on a positive charge in the middle of a side.

Steps to solve a superposition problem

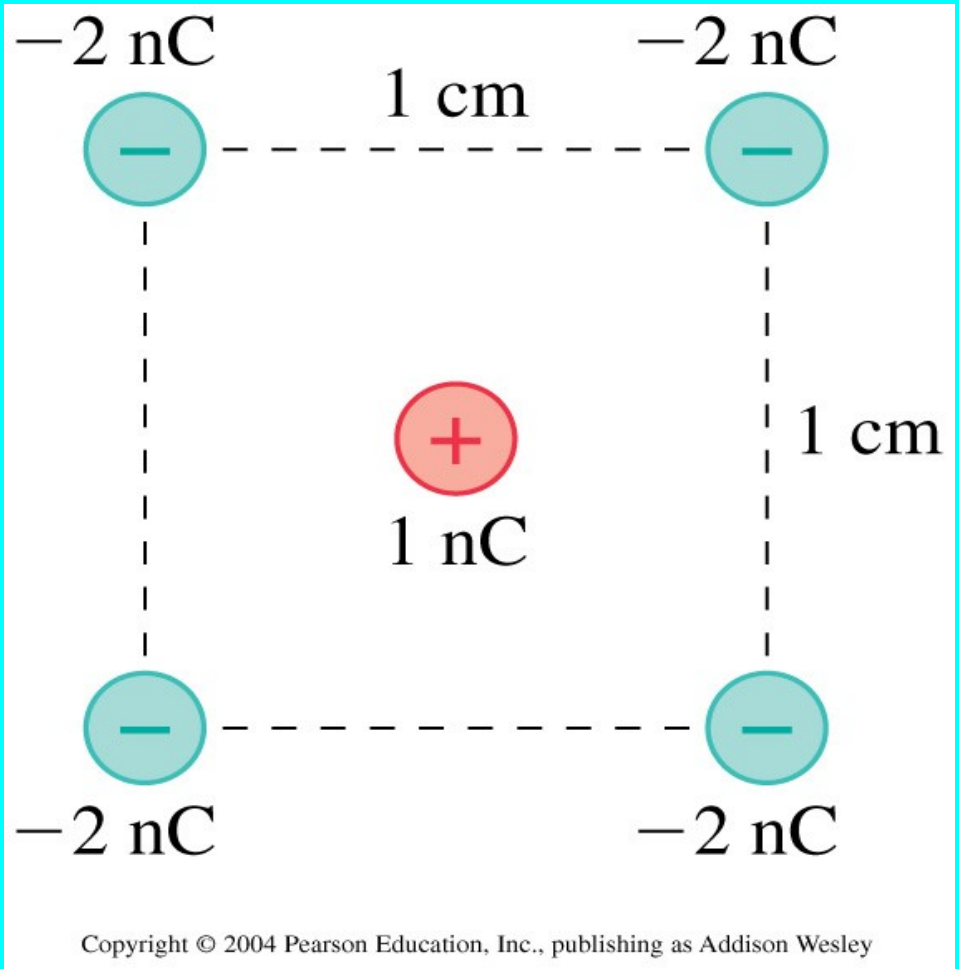
1) Identify the charge (or point P) at which you want to calculate the force (or field).

2) Draw an arrow (a vector) representing the Force Vector (or Field Vector) at the charge along a line joining it with each of the other charges.

3) Make the length of the vectors proportional to the force between the charges (shorter arrows for more distant charges)

4) Add the vectors using the tip to tail method to find the *resultant*.

Superposition problem



Estimate the direction of the NET force on the central charge due to the other four charges.

A) “Up”
B) Along a diagonal
C) “Left”
D) “Right”
E) What net force?

Symmetry

… is the key to easily solving otherwise difficult problems

Coulomb's Law, Vector Form

$$\vec{F}_{12} = k\frac{q_1 q_2}{r_{12}^2}\hat{r}_{12}$$

$$\vec{F}_{net} = \sum_{n=1}^{N} k\frac{q_1 q_n}{r_{1n}^2}\hat{r}_{1n}$$

$$\vec{F}_{net} = Q\sum_{n=1}^{N} k\frac{q_n}{r_n^2}\hat{r}_n$$

Making friends with “r-hat”

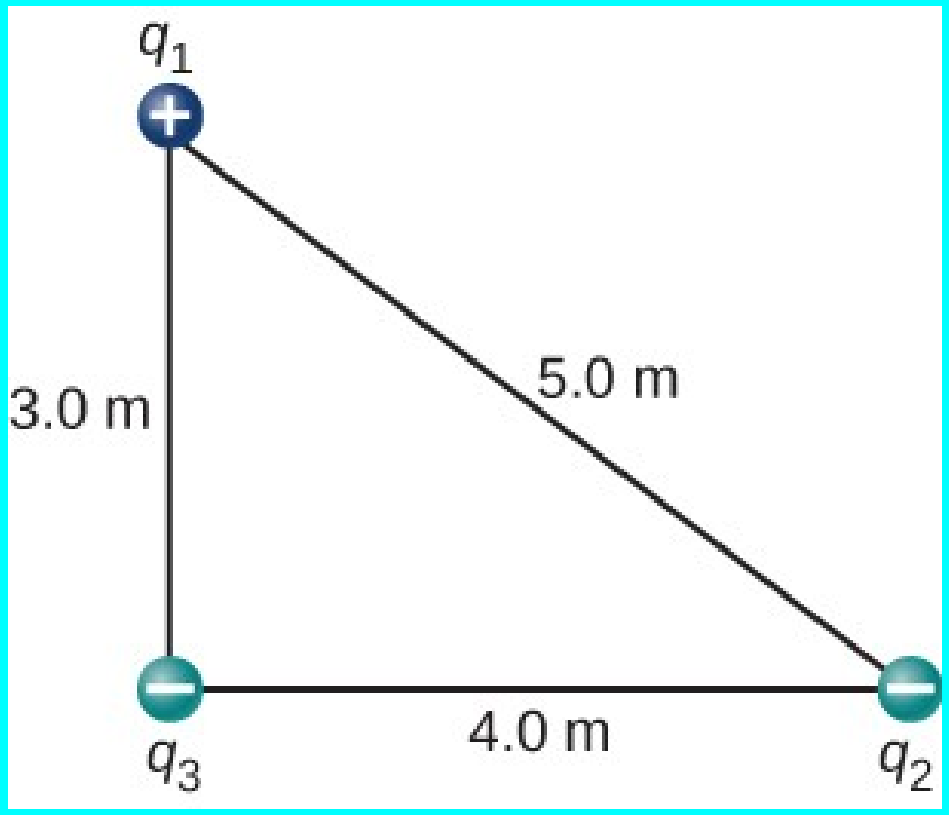
$$\vec{F}_{12} = k\frac{q_1 q_2}{r_{12}^2}\hat{r}_{12}$$

r-hat points from other charges to 'your' charge.

$\hat{r}$ is a unit vector like $\hat{i}$, $\hat{j}$, and $\hat{k}$

$\hat{r}$ points in different directions for different charges

Homework 5-62-ish



$q_1 = 2 \times 10^{-7}$ C

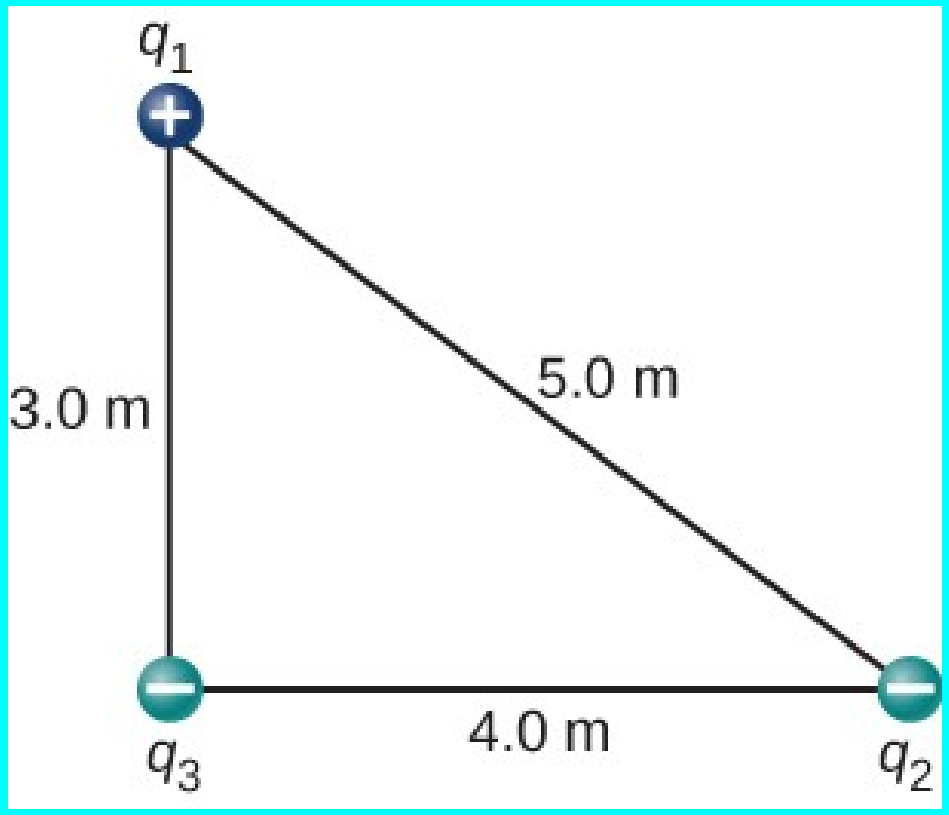
$q_2 = -4 \times 10^{-7}$ C

$q_3 = -1 \times 10^{-7}$ C

Find force on q_3

Homework 5-62-ish

$$\vec{F}_{net} = Q \sum_{n=1}^{N} k \frac{q_n}{r_n^2} \hat{r}_n$$



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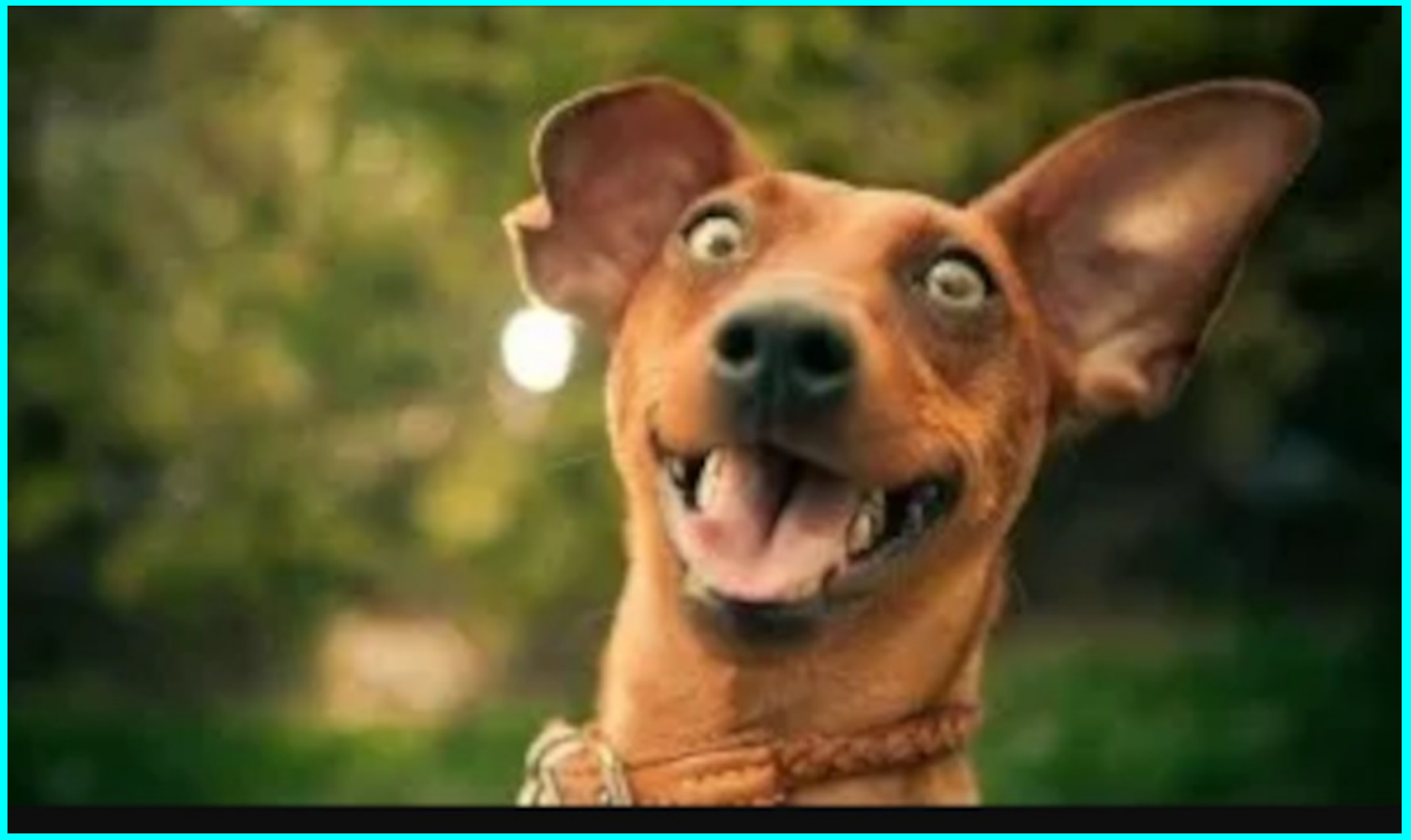
DEMOS!



DEMOS!

Two types of charge

Electric Field

Next Class:

More on Coulomb's law and electric field