

# **Physics 122 – Class #20 – (3/26/15)**

- **Homework/Readings**
- Chapter 29, section by section.

# PHYSICS DROP-IN (HELP) SESSIONS WORKMAN 110

<b>Monday:</b>	<b>10:00am-12:00pm</b> <b>12:00pm-2:00pm</b>	<b>Dana Baylis</b> <b>Gareth (Indy) Jones</b>
<b>Tuesday:</b>	9:00am-11:00am 11:00am-12:00pm	Virginie Montes Tina Gueth
<b>Wednesday:</b>	10:00am-11:00pm 11:00am-12:00pm 1:00pm-2:00pm 2:00pm-3:00pm	Jose Martinez James Price Jose Martinez Heather Bloemhard
<b>Thursday:</b>	11:00am-12:00pm 1:00pm-2:00pm <b>4:00pm-6:00pm</b>	Tina Gueth Brandon Gray <b>Ryen Lapham</b>
<b>Friday:</b>	<b>12:00am-1:00pm</b>	<b>Brandon Gray</b>

# Homework

## Mastering Physics

29.17, 29.18, 29.19, 29.20, 29.21, 29.25,  
29.51, 29.53, 29.54

[Due Tuesday 3/31/2015 at 11:59 pm]

HW-WR-07 29.56, 29.57, 29.17

(due next Tuesday in class)

## MP Assignment 9a

29.1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 15, 25, 28, 29,  
64, 65

[due Saturday night 4/4]



# Reworked Exams

- Reworked exams due next Tuesday (1/3 points back)
- Everyone qualifies
- If you missed last class ... come get your exam after class

# Reading Assignments

*This week* – Chapter 29 – Relation between electric potential and electric field.

Combining capacitors.

*Next week* – Chapter 30 – Currents. Read all of it (it's less mathematical than most), but you may skip pages 873-874.

Lab next week is on series/parallel and RC circuits (Ch. 31).

## Chapter 29 – Summary

- 29.1 You can integrate  $E(x)$  to get  $V(x)$   
get  $E(x)$  from  $dV/dx$ .

This allows understanding the formula for a parallel plate capacitor.

- 29.2 You “manufacture” potential with a battery, or a Van de Graaf ... or a power plant!

- 29.3  $E$  is the “gradient” of potential  
AND Potentials add in series.

- 29.4 Every point in a conductor is at the same potential.



# Chapter 29 – Summary

- 29.5  $Q=CV$

Capacitances in Parallel Add.

You need a reciprocal formula for capacitances in series.

- 29.6 Capacitors store energy and charge

- 29.7 Dielectric materials let you store more energy and charge in the same space than using air or a vacuum.

# Electrical Units

Potential Energy = Charge x Potential ( $U = Q V$ )

Power = Energy/time =  $QV/t = (Q/t) V = I V$

Charge – Coulombs

Charge/time – Coulombs/second = Current  
(Amperes)

Electric Field – Newtons/Coulomb or Volts/meter

Electric Potential – Joules/Coulomb (or Volts)

Power = Joules/second =

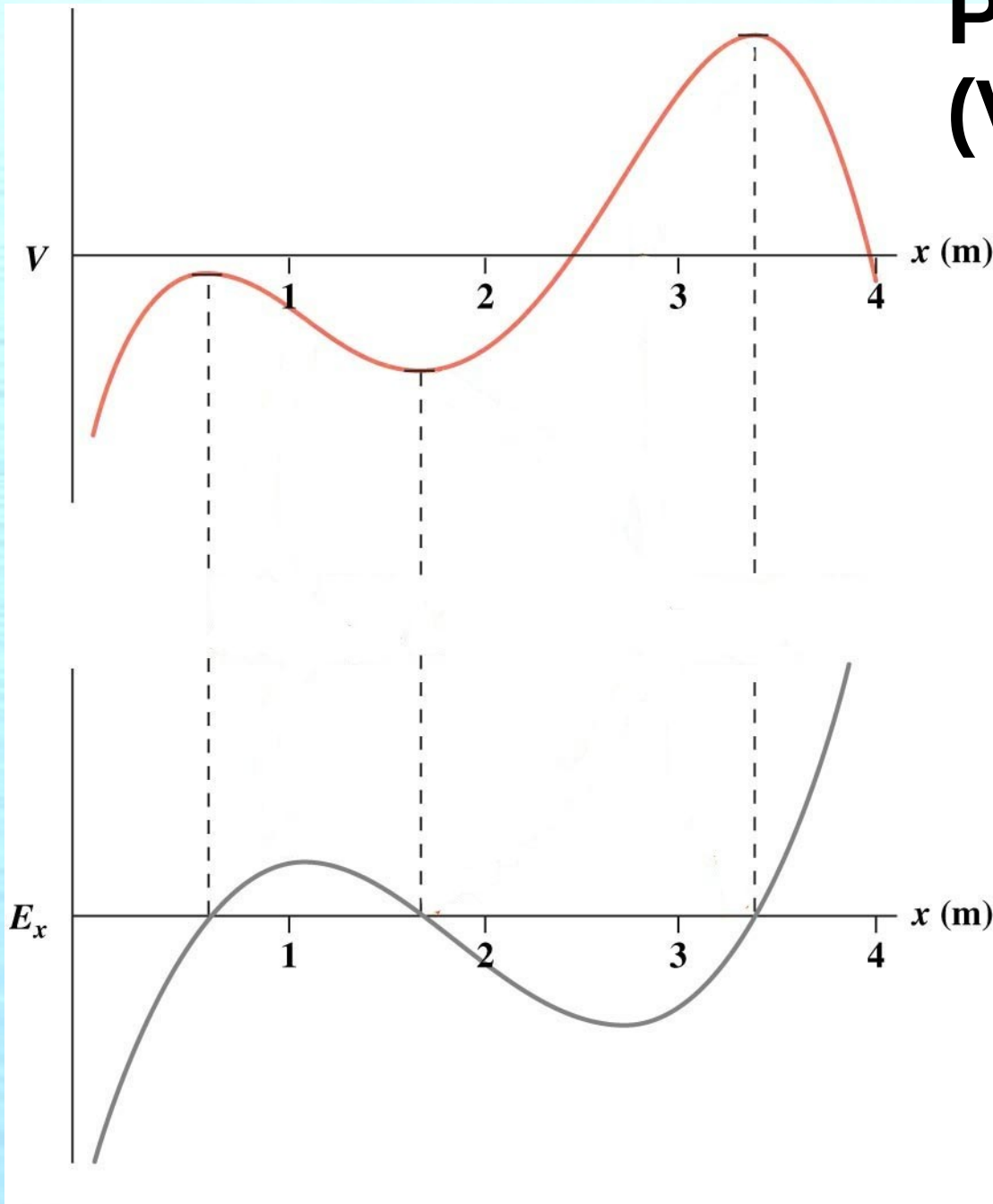
Coulomb/sec x Joules/Coulomb =  $I V$



## Chapter 29 – Summary

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get  $E(x)$  from  $dV/dx$ .
- This allows understanding the formula  
for a parallel plate capacitor.

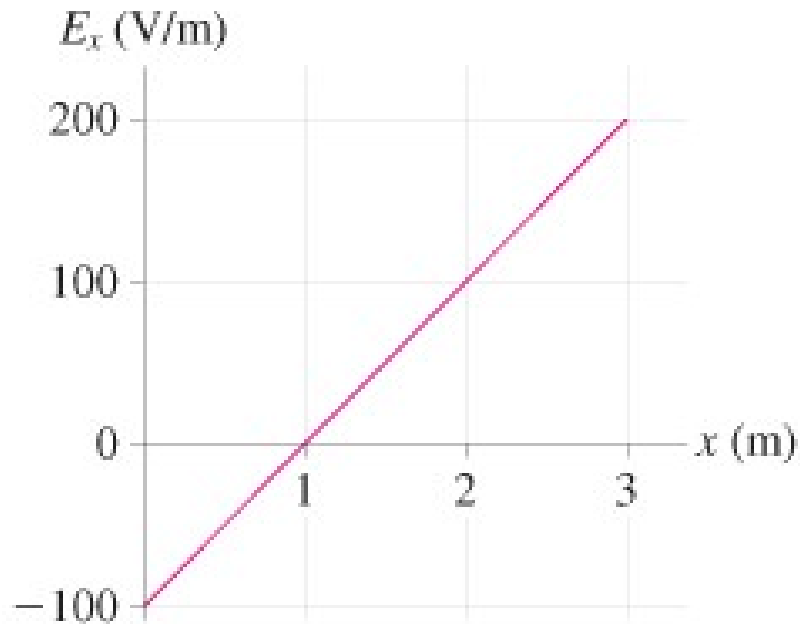
# Potential (Voltage) in 1-D



$$V(x) = -\int E_x dx$$

$$E_x = -\frac{dV}{dx}$$

## Problem 29.3



## Potential (Voltage) in 1-D

$$V(x) = -\int E_x dx$$

Given  $E_x$  as at left, what is potential Difference between 2 and 3 meters?

$$y = mx + b$$

$$E_x = 100x - 100$$

$$V_{23} = -\int_2^3 E_x dx = -\int_2^3 (100x - 100) dx$$

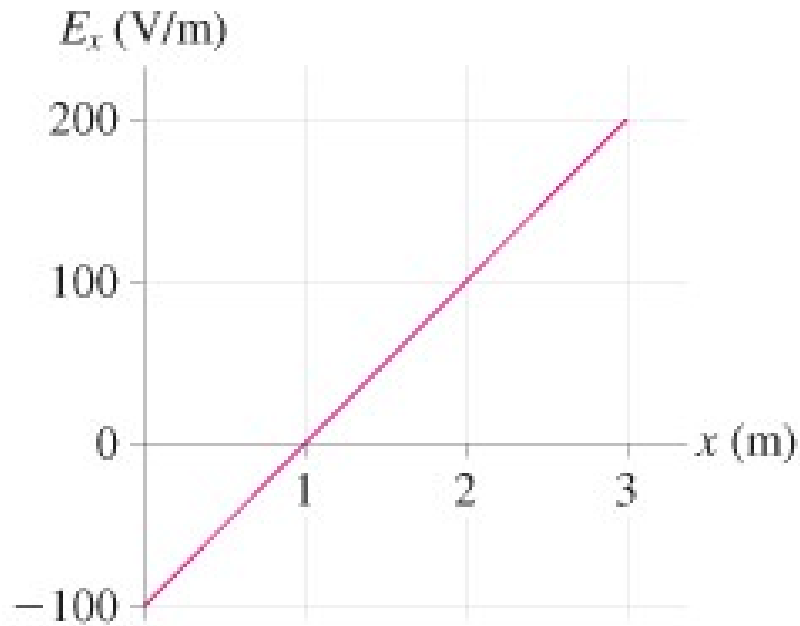
$$V_{23} = -\int_2^3 (100x - 100) dx = -50x^2 + 100x$$

$$V_{23} = -50x^2 + 100x \Big|_2^3$$

$$V_{23} = -(50)(9) + (100)(3) + (50)(4) - (100)(2) = -150 \text{ Volts}$$



## Problem 29.3



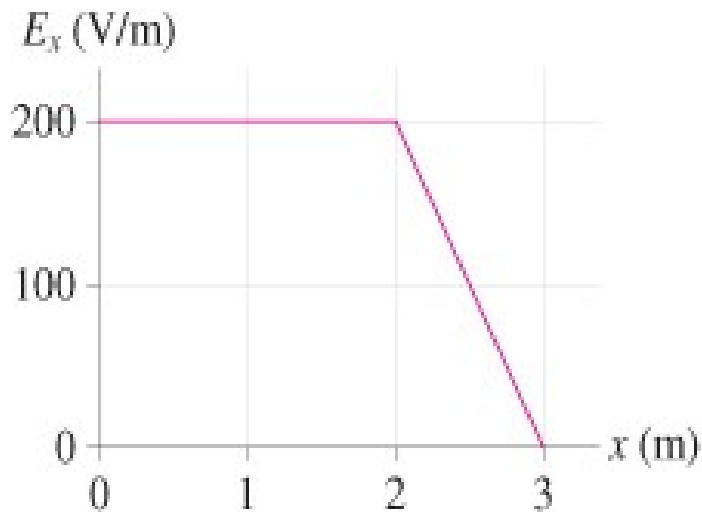
## Potential (Voltage) in 1-D

$$V(x) = -\int E_x dx$$

Given  $E_x$  as at left, what is potential Difference between 2 and 3 meters?

Can more easily do this problem  
By remembering the integral  
Is area under a curve.

## Problem 29.4



## Potential (Voltage) in 1-D

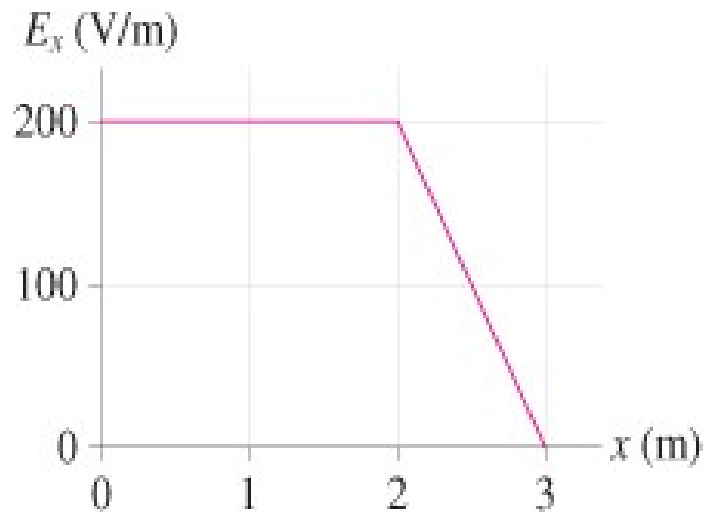
$$V(x) = -\int E_x dx$$

If the potential of the origin is  $V(0) = 100$  Volts, what is  $V(1)$ ?  
What is  $V(2)$ ?

What is  $V(3)$ ?

- [A] 0 V
- [B] -100 V
- [C] -300 V
- [D] -400 V
- [E] -450 V
- [F] -500 V

## Problem 29.4



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# Electric field from voltage

**Given**  $V(x) = 8x^2 - 7$

**what is the**

**Electric field at  $x=1$  m?**

- [A] 1 V
- [B] -1 V
- [C] -9 V
- [D] 16 V
- [E] -16 V

**You are told that the electric potential is zero  
At some point “P”. Which statement is correct?**

- A. A charge placed at  $P$  would feel no electric force
- B. The electric field at  $P$  is also zero.
- C. The electric field at  $P$  is negative
- D. Both A and B
- E. not enough information given to decide

# Chapter 29 – Summary

- 29.2 You “manufacture” potential with a battery, or a Van de Graaf ... or a power plant!



# Van de Graaf Generator

- Charges are literally carried up on a belt from the base (ground) to the sphere on top of generator.
- Since there are already charges on top, there is an electric field and work must be done to move the charges toward the field
- Whenever you have a voltage source, work was done against electric field.

# Potential Energy to Power

If you let a charge move through a potential, it acquires kinetic energy. You can create a potential by supplying either kinetic energy or some non-electrical energy.

In our lives, we pay money for potential, either by paying for batteries (chemical energy) or by paying a power company and plugging in.

How does this potential get there?

In practice lots of chemical energy (coal, oil) is converted into electric potential ... and we love it!



# Electric Power Plants

[Tinyurl.com/fourcornerspowerplant](http://tinyurl.com/fourcornerspowerplant)

<http://tinyurl.com/feedingacoalfiredplant>

Chapter 33 –  
How electrical  
generators  
work

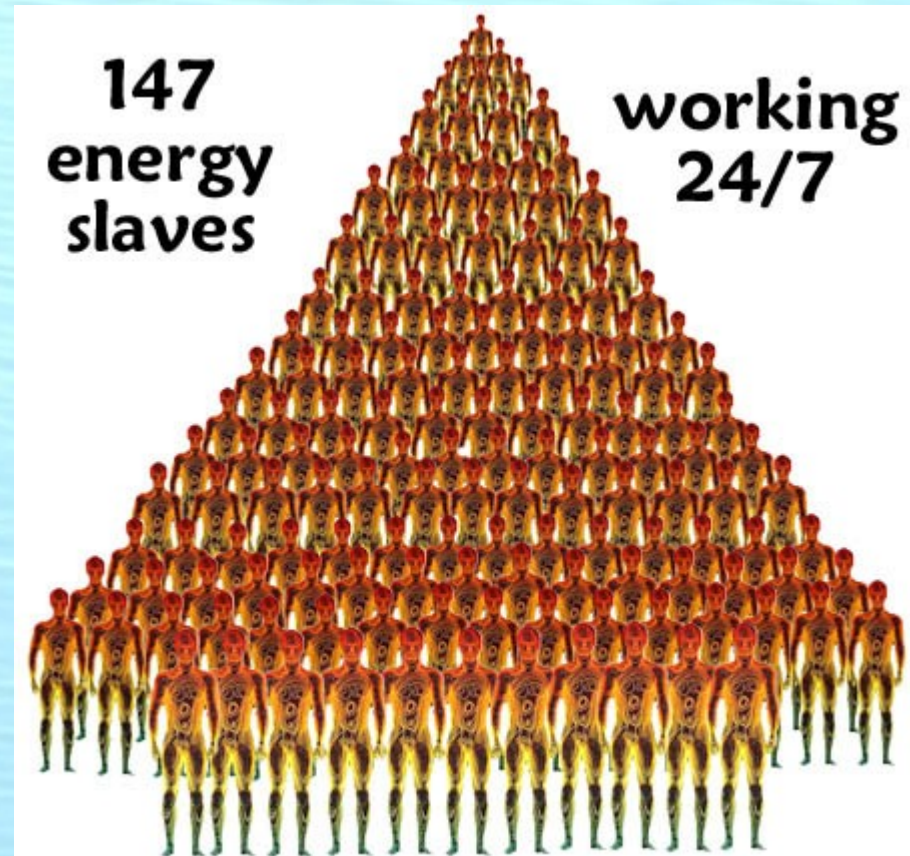




# We burn fossil fuel to generate electricity

One gallon of gasoline is about 100 million joules  
= 40 kiloWatt Hours, is 600 people working as hard as  
they can for an hour.

Our wonderful lifestyle is  
Sustained by “energy slaves”



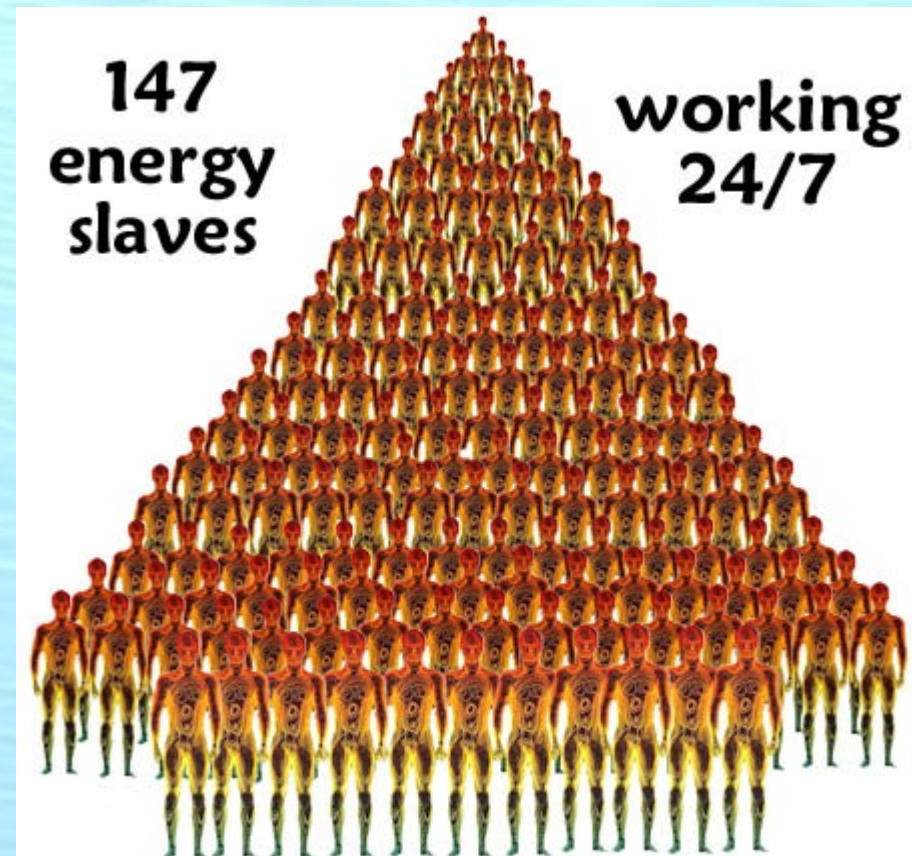


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You are all Pharoahs.



# Chapter 29 – Summary

- 29.3  $E$  is the “gradient” of potential  
AND Potentials add in series.
- 29.4 Every point in a conductor is at  
the same potential.



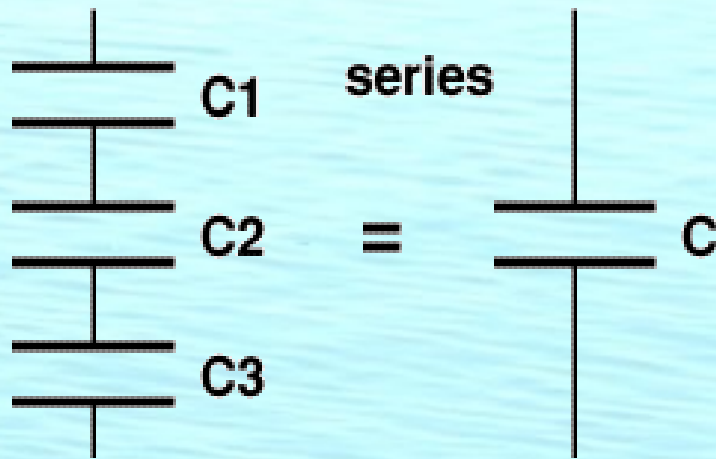
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Capacitances in Parallel Add.

- You need a reciprocal formula for capacitances in series.

# Capacitors in Series and Parallel

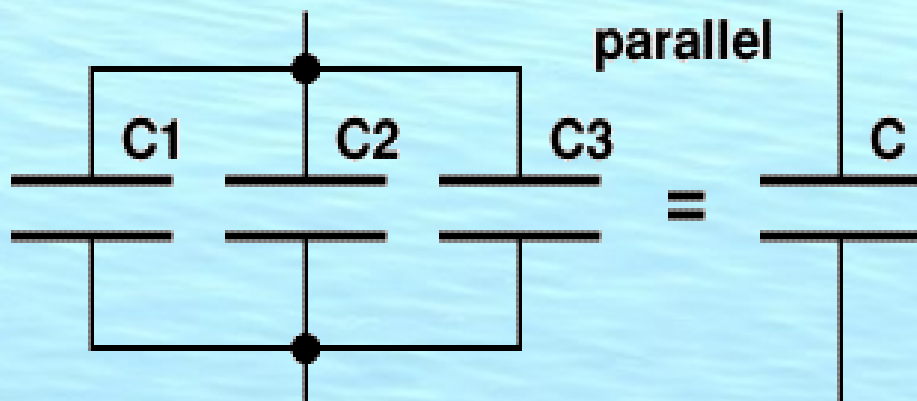


Caps in series have the

“bottom wire” or one

Connected to the “top wire”

Of the next.



Caps in parallel have all

Their tops connected to

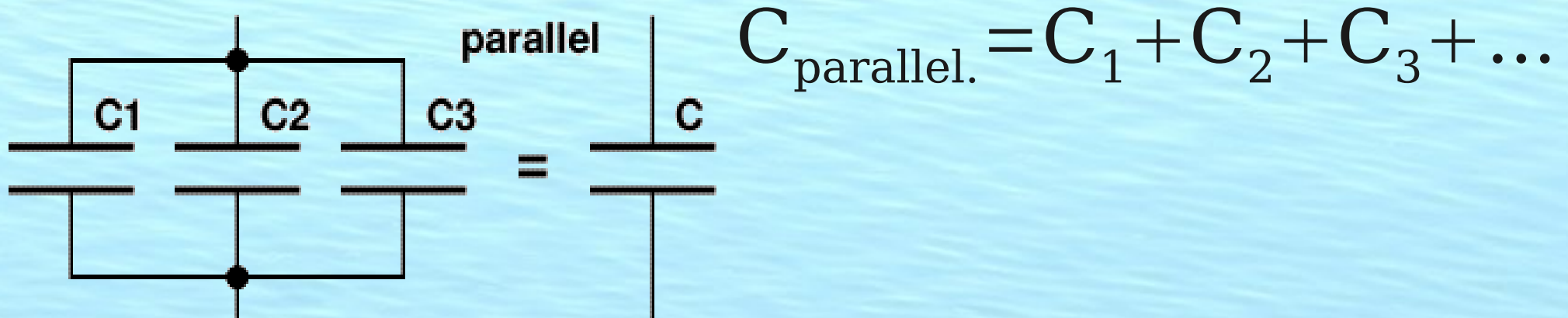
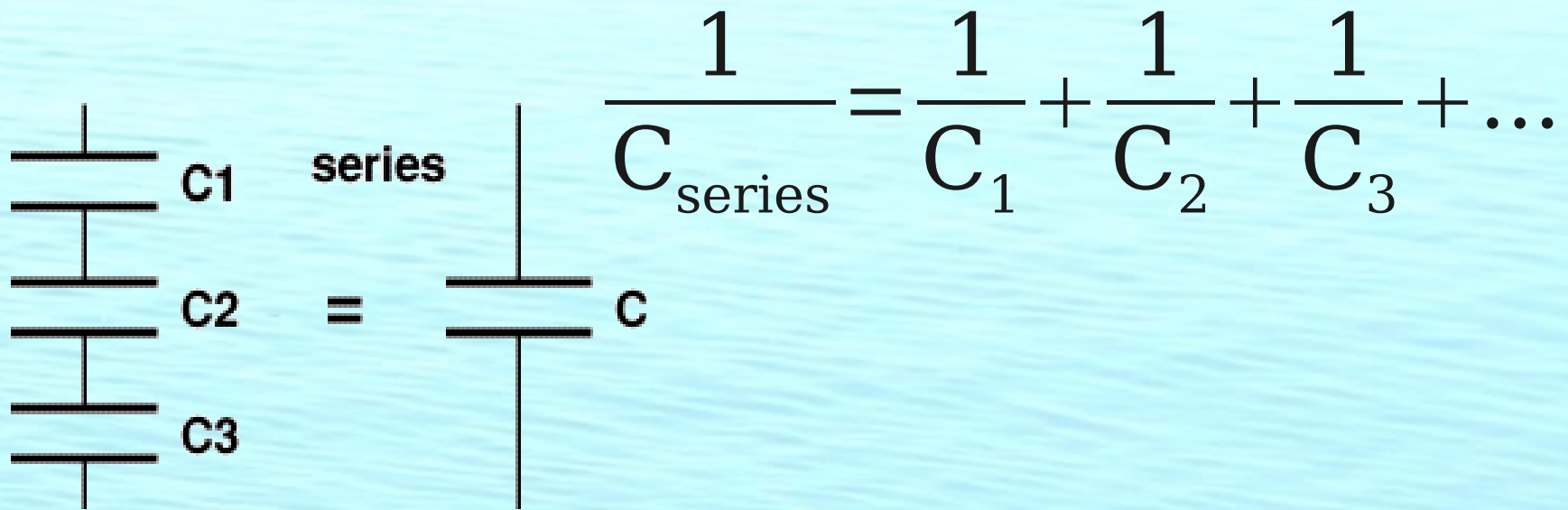
One wire and all their

Bottoms also connected to

A second wire.

Caps in series have equal charges

# Capacitors in Series and Parallel



Caps in parallel have equal voltages.

Caps in series have equal charges.



A 12 microfarad capacitor is connected with a 6 microfarad capacitor as shown. The equivalent capacitance of this combination is:

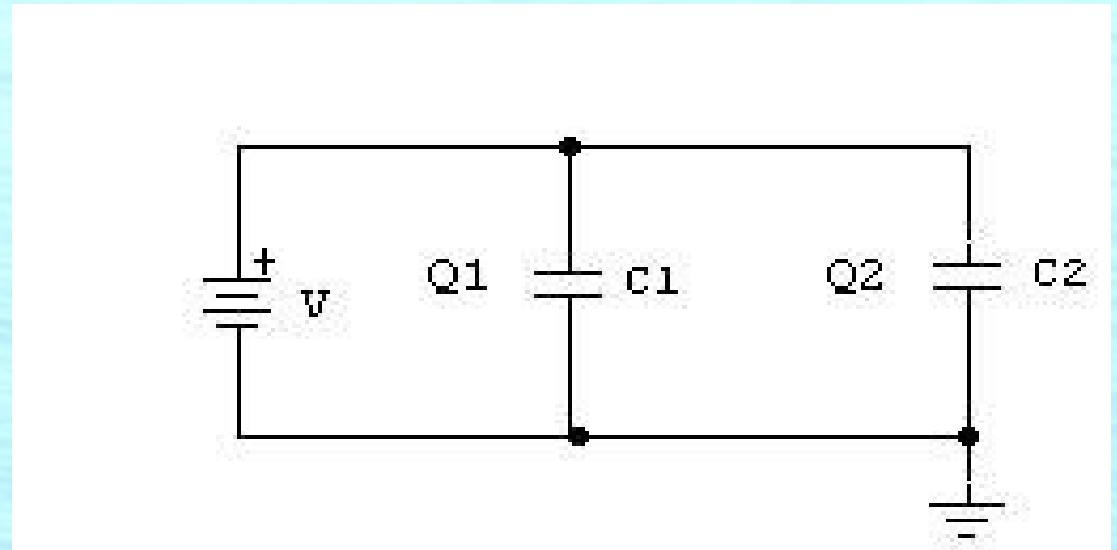
A.  $C_{eq} = 18 \mu\text{F}$

B.  $C_{eq} = 9 \mu\text{F}$

C.  $C_{eq} = 6 \mu\text{F}$

D.  $C_{eq} = 4 \mu\text{F}$

E.  $C_{eq} = 2 \mu\text{F}$



Two capacitors are connected together as shown. What is the equivalent capacitance of the two capacitors as a unit?

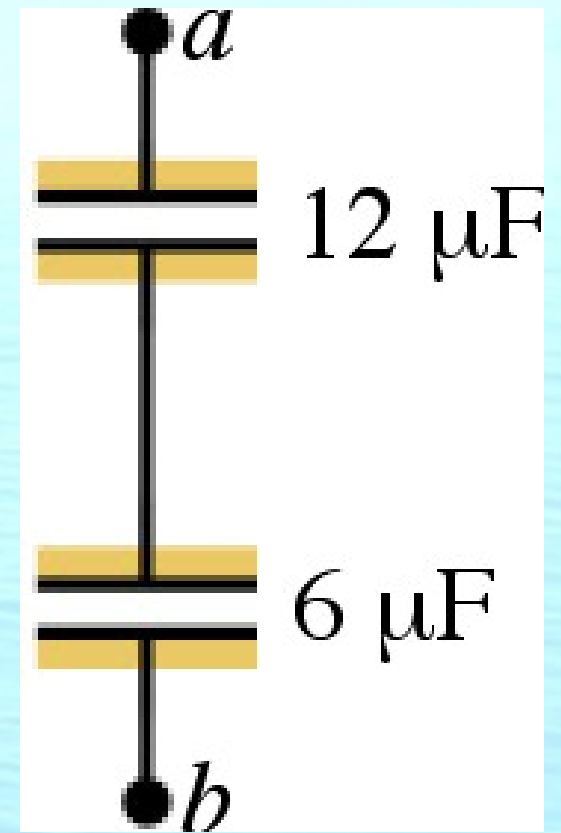
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- 29.7 Dielectric materials let you store more energy and charge in the same space than using air or a vacuum.

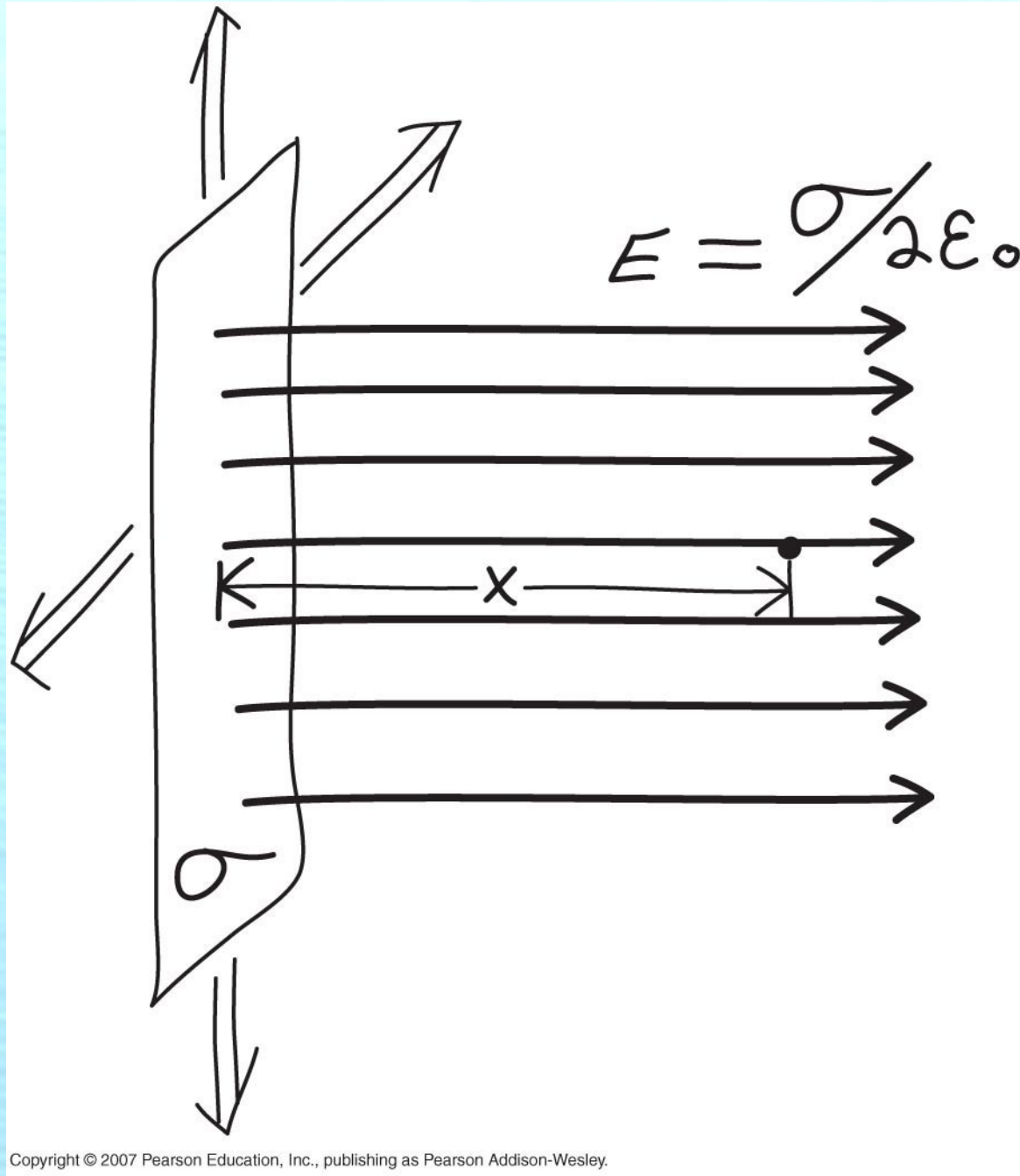


All electric fields represent stored energy.  
And capacitors are convenient containers for electric fields.

Capacitance relates Voltage to stored charge. Generally voltage is easier to measure than charge.

$$C = \frac{Q}{V} \quad Q = C V$$

New SI Unit: “Farad”.  $[C]=[F][V]$   
(Coulomb=Farad x Volt)



## E-Field of a “large” charged plate:

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{i}$$

$$\sigma = \frac{Q}{A}$$

$$V = -\int_0^x E \cdot dx'$$

## **E-Field of an infinite charged plate:**

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{i} \quad V = \frac{U}{q} = -\int_0^x E \cdot dx'$$

## **Electric Potential of an infinite plate:**

$$[A] \quad V = \frac{\sigma^2}{4\epsilon_0}$$

$$[B] \quad V = -\frac{\sigma^2}{4\epsilon_0}$$

$$[C] \quad V = \frac{\sigma}{2\epsilon_0} x$$

$$[D] \quad V = -\frac{\sigma}{2\epsilon_0} x$$



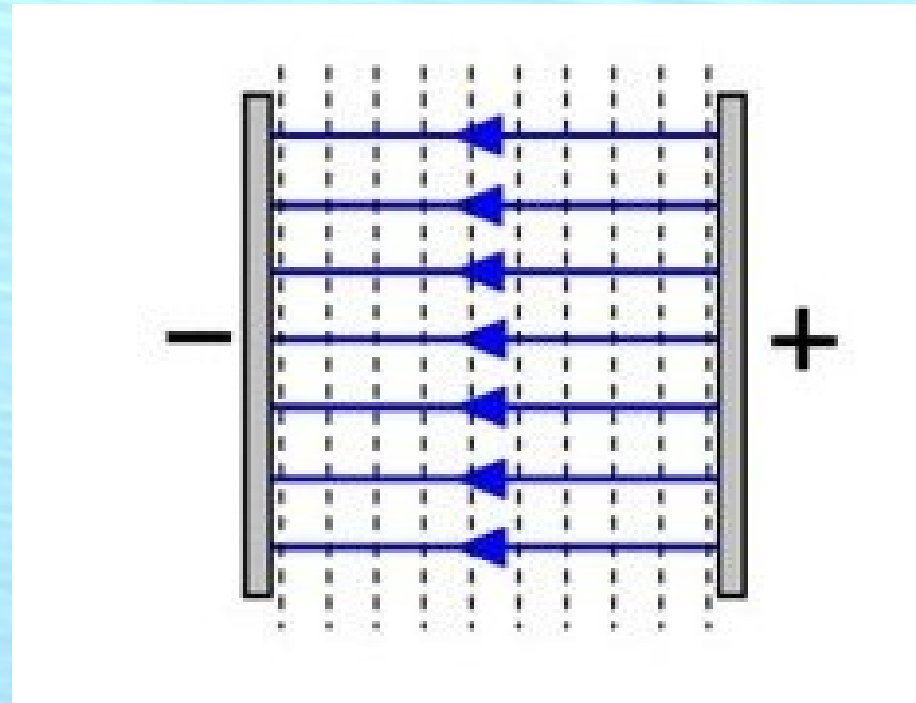
Electric potential of TWO large plates  
(Area “A” separation “d”) ...

Electric field is doubled because two charged  
plates of opposite sign.

$$\vec{E} = \frac{-\sigma}{\epsilon_0} \hat{i}$$

$$V = -\vec{E} \cdot \Delta \vec{r} = E d$$

$$V = \frac{\sigma}{\epsilon_0} x = \frac{\sigma}{\epsilon_0} d$$



# Deriving Parallel Plate Formula

$$[1] Q = C V$$

Definition of Capacitance

$$[2] V = \frac{\sigma}{\epsilon_0} d$$

Shown on last page

$$[3] \sigma = \frac{Q}{A}$$

Definition of surface charge density

$$[4] V = \frac{Q}{\epsilon_0 A} d$$

Plug 3 into 2

$$[5] Q = \frac{\epsilon_0 A}{d} V$$

Solve for Q

$$[6] C = \frac{\epsilon_0 A}{d}$$

**How many capacitors are in your dorm room or house?**

**(A) None – I do not own a time machine or a DeLorean.**



**(B) About a dozen – Capacitors are energy storage and signal filtering devices used in power supplies for all electronics.**

**(C) Billions**



Note that the parallel plate formula only has “geometric” variables. Capacitance is a property of a set of conductors and does not depend on charge or voltage (or any other electric variables)

$$C = \frac{\epsilon_0 A}{d}$$

**[Ex. 1] Find the capacitance of a parallel plate capacitor consisting of circular plates 10 cm in radius separated by 1.5 mm.**

$$\epsilon_0 = 8.86 \times 10^{-12} \text{ F/m}$$

$$C = \epsilon_0 \frac{A}{d}$$

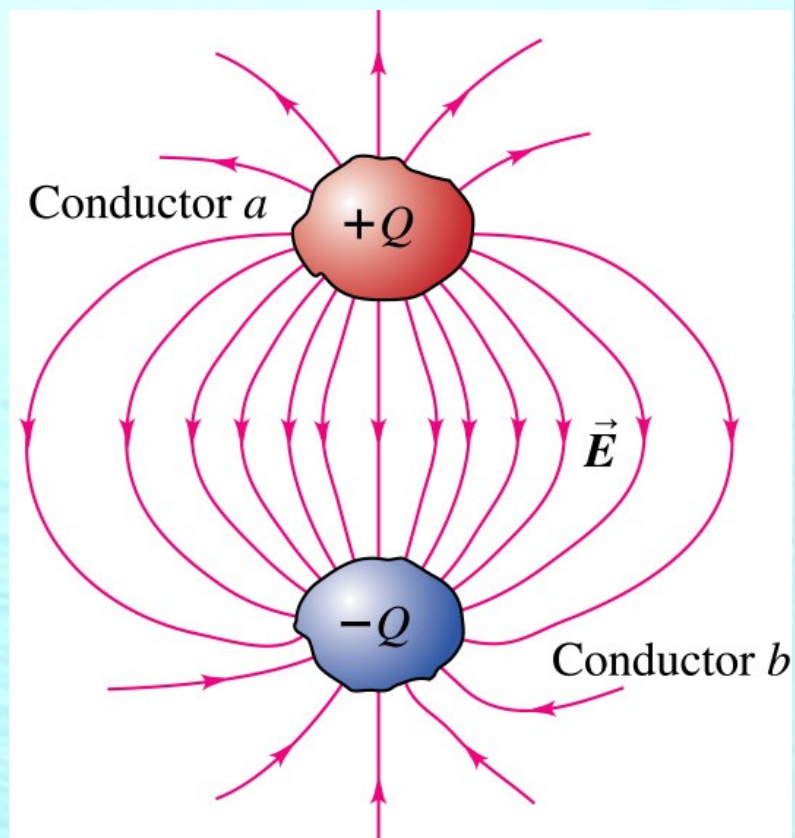
$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

The two conductors  $a$  and  $b$  are insulated from each other, forming a capacitor. You increase the charge on  $a$  to  $+2Q$  and increase the charge on  $b$  to  $-2Q$ , while keeping the conductors in the same positions.

What effect does this have on the capacitance  $C$ ?

- A.  $C$  is multiplied by a factor of 4
- B.  $C$  is multiplied by a factor of 2
- C.  $C$  is unchanged
- D.  $C$  is multiplied by a factor of  $1/2$
- E.  $C$  is multiplied by a factor of  $1/4$





**[Ex. 2] A capacitor's plates hold  $1.3 \mu\text{C}$  when it is charged to  $80\text{ V}$ . What is its capacitance?**

$$C = \epsilon_0 \frac{A}{d}$$

$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

**[Ex. 3] A stereo receiver contains a 2500  $\mu\text{F}$  capacitor charged to 35 V.**

**How much energy does it store?**

$$C = \epsilon_0 \frac{A}{d}$$

$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

You reposition the two plates of a capacitor so that the capacitance doubles.

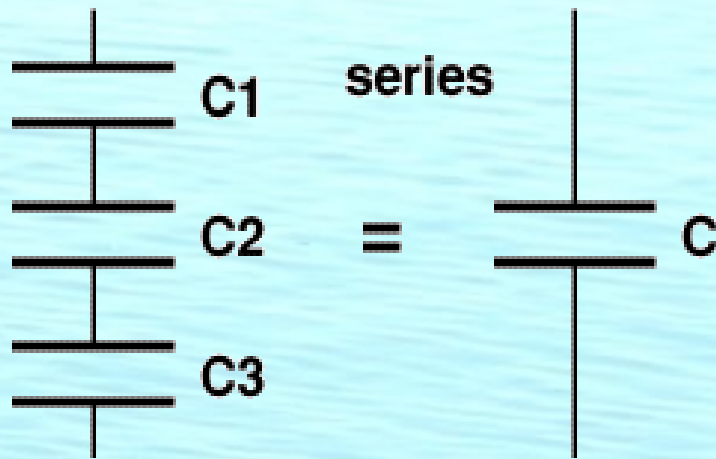
If the charges  $+Q$  and  $-Q$  on the two plates are kept constant in this process, what happens to the potential difference  $V_{ab}$  between the two plates?

- A.  $V_{ab}$  is multiplied by a factor of 4
- B.  $V_{ab}$  is multiplied by a factor of 2
- C.  $V_{ab}$  is unchanged
- D.  $V_{ab}$  is multiplied by a factor of  $1/2$
- E.  $V_{ab}$  is multiplied by a factor of  $1/4$

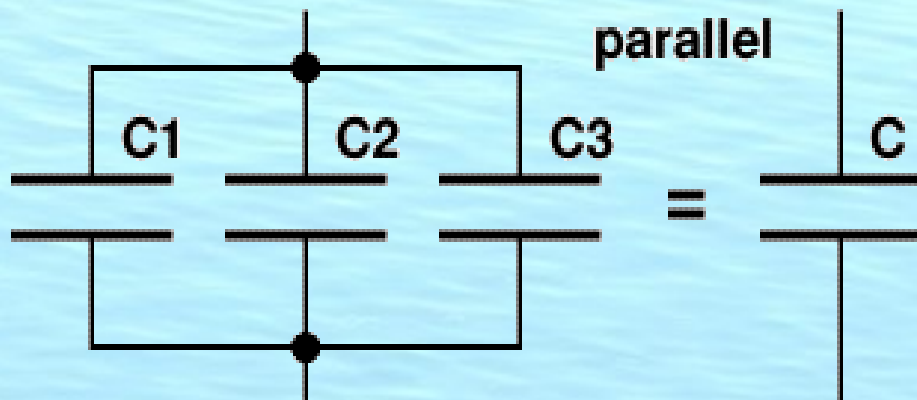
$$Q = CV$$



# Capacitors in Series and Parallel



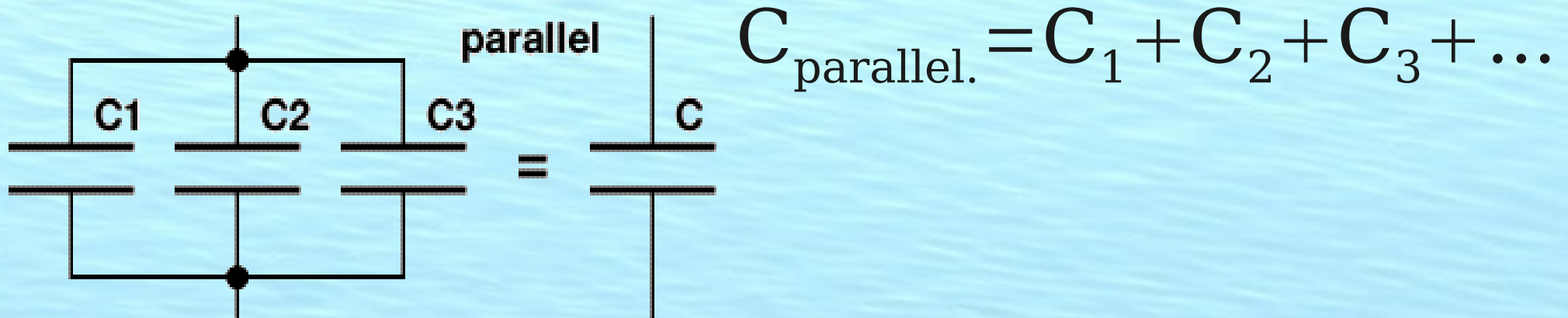
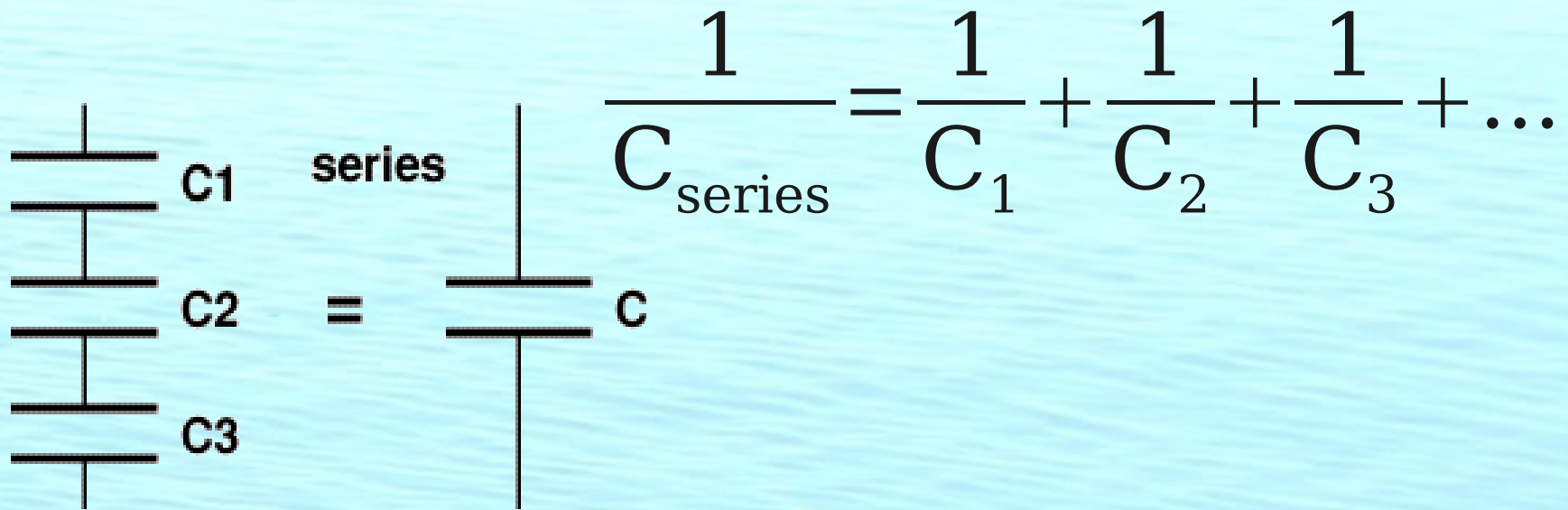
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Their tops connected to  
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Caps in series have equal charges

# Capacitors in Series and Parallel



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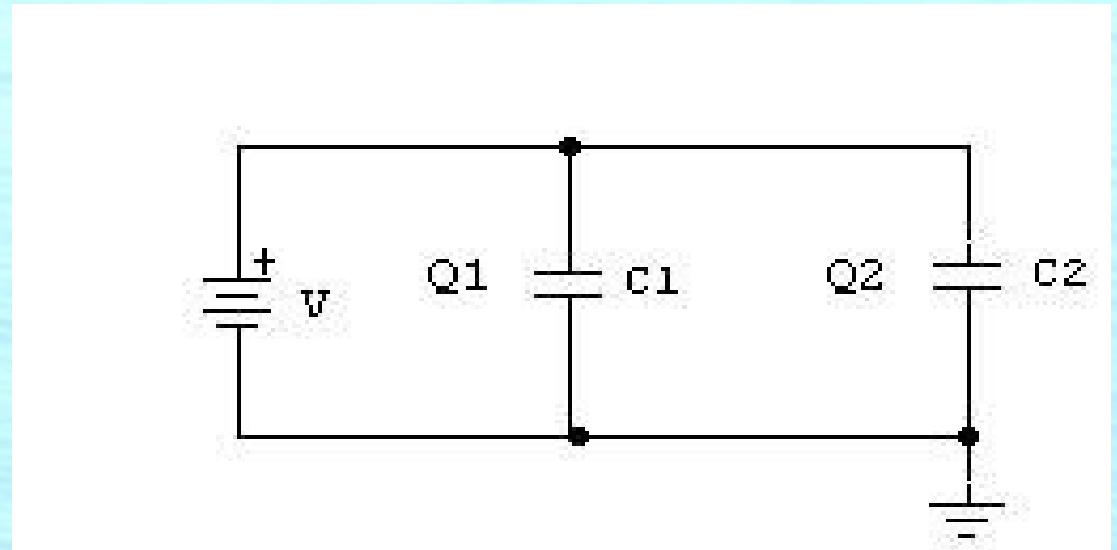
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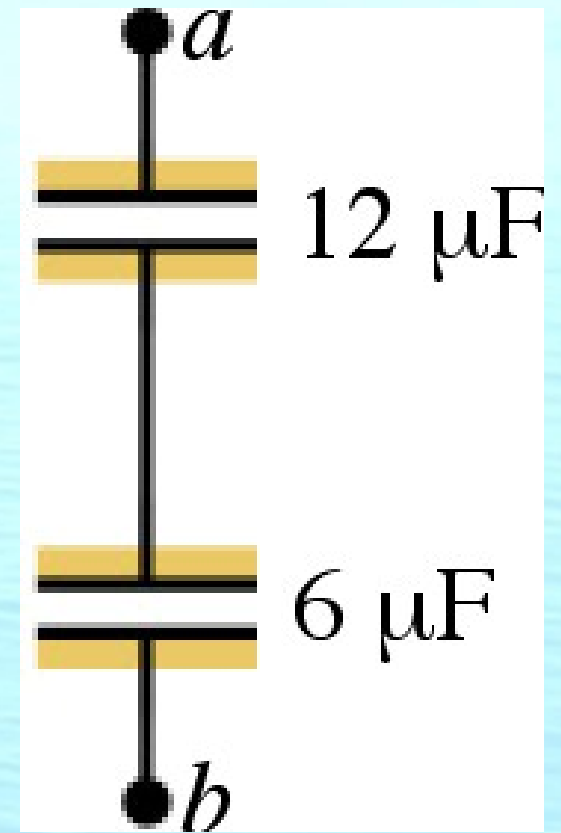
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Network of capacitors:

Replace parallel elements with an equivalent cap. Combine that equivalent cap in series with what is left.

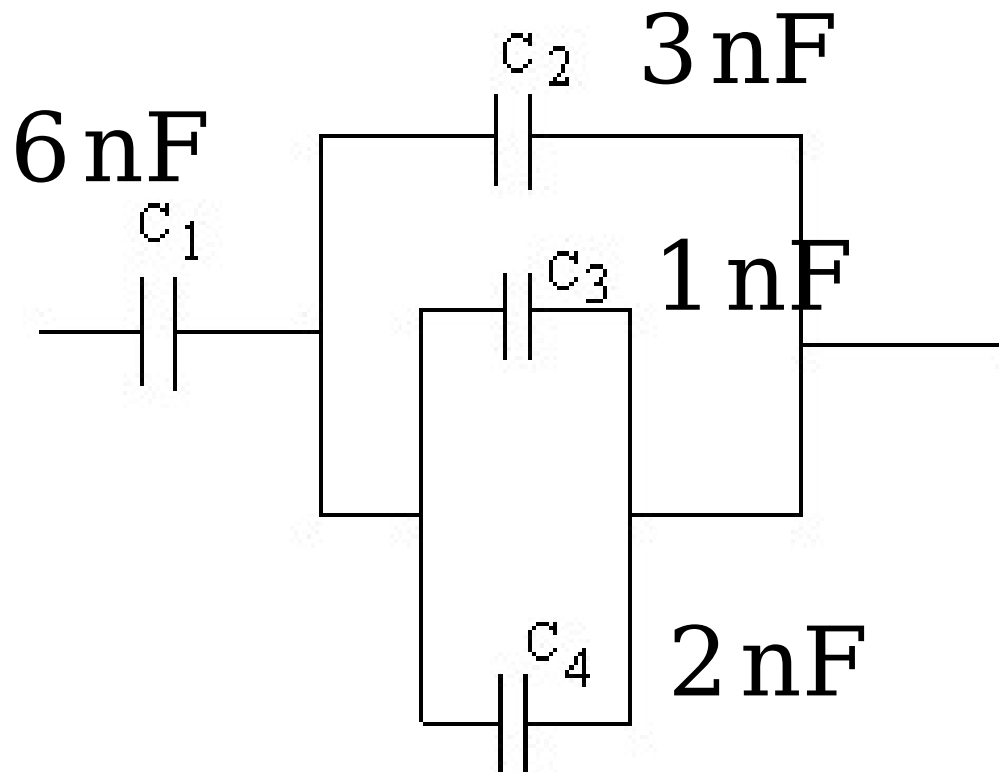
[A] 1 nF

[B] 2 nF

[C] 3 nF

[D] 6 nF

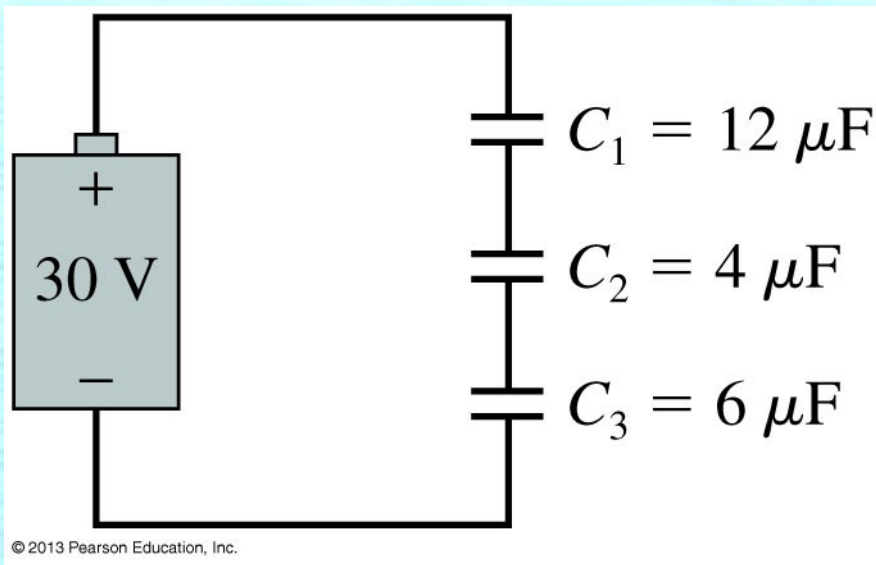
[E] 12 nF



**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

**What is the voltage across each capacitor?**



Caps in parallel have equal voltages.

Caps in series have equal charges.

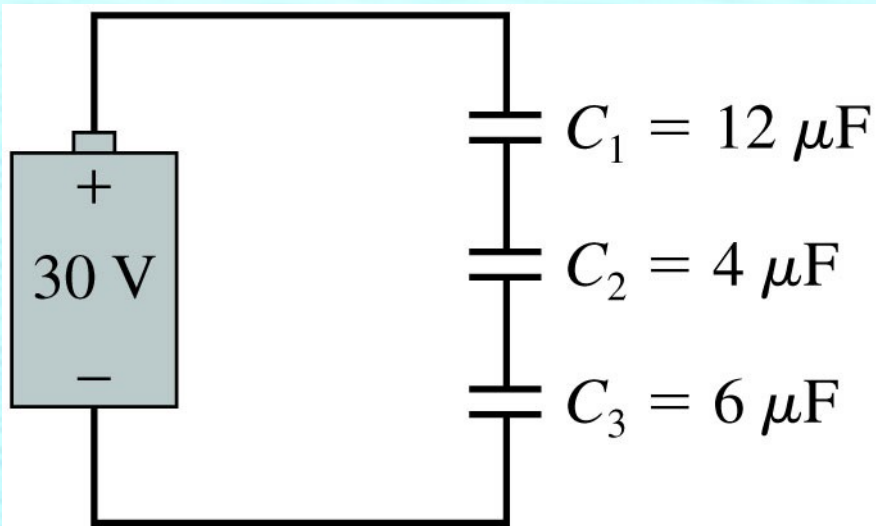
Voltages in series add



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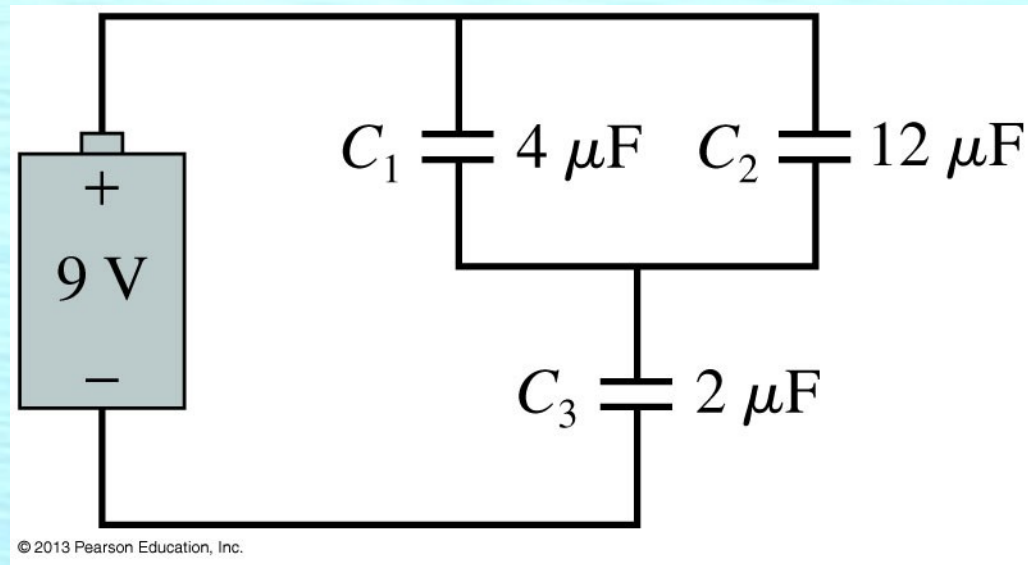
**What is the voltage across each capacitor?**



**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

**What is the voltage across each capacitor?**



Caps in parallel have equal voltages.

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Voltages in series add

**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

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