

# Physics 122 – Class #19 – (3/24/15)

- **Announcements**
- Exam Review
- Connections
  - Blitz summary of Chapter 28
  - Blitz summary of Chapter 29
  - Where does potential really come from?
- Capacitance
  - Parallel Plates
  - Energy in a capacitor
  - Of circuits – “Equivalent capacitance”
  - Of cylinders

# Exam Grades

- 13 A's
  - 13 B's
  - 14 C's
  - 9 D's
  - 19 F's
- 
- Mean 73
  - Median 77
  - Max 100
  - Min 10

# Midterm Grades

- 7 A's
  - 17 B's
  - 20 C's
  - 12 D's
  - 19 F's
- 
- Details on Canvas.
  - Clickers not included yet
  - “A” on exams, “C” on HW, – “B”
  - “D” on exams, “A” on HW, – “C”

# Midterm Grades – What do I do?

- Numerical grade below 55% ... drop course (Deadline 4/1) – 7 people
- Do old (MP) homeworks for 50% credit or more.
- Rework exam.
- Read book!
- Find more hours!
- Talk to advisor
- See tutors (OSS)
- See tutors (Physics grad students)

# PHYSICS DROP-IN (HELP) SESSIONS WORKMAN 110

Monday:	<b>10:00am-12:00pm</b> <b>12:00pm-2:00pm</b>	<b>Dana Baylis</b> <b>Gareth (Indy) Jones</b>
Tuesday:	9:00am-11:00am 11:00am-12:00pm	Virginie Montes Tina Gueth
Wednesday:	10:00am-11:00pm 11:00am-12:00pm 1:00pm-2:00pm 2:00pm-3:00pm	Jose Martinez James Price Jose Martinez Heather Bloemhard
Thursday:	11:00am-12:00pm 1:00pm-2:00pm <b>4:00pm-6:00pm</b>	Tina Gueth Brandon Gray <b>Ryen Lapham</b>
Friday:	<b>12:00am-1:00pm</b>	<b>Brandon Gray</b>

# Physics 122 – Class #19 –

- Homeworks due next Tuesday
- Reworked exams due next Tuesday  
(1/3 points back)
- Problems 4, 5, 10 in recitation

# Reading Assignments

*This week* – Chapter 29 – Relation between electric potential and electric field.  
Combining capacitors.

*Next week* – Chapter 30 – Currents. Read all of it (it's less mathematical than most), but you may skip pages 873-874.

Lab next week is on series/parallel and RC circuits (Ch. 31).

# Chapter 28 – Summary

- 28.1 Potential energy is calculated from work just like in Physics I.

- For constant field  $U = -\vec{F} \cdot \Delta \vec{r}$

$$U_{\text{grav}} = m g y \qquad U_{\text{elec}} = q E s$$

- 28.2 For a varying field

$$U(x) = -\int_0^x F(x') dx'$$

- For a point mass/charge,

$$U_{\text{grav}} = -G \frac{m_1 m_2}{r} \qquad U_{\text{elec}} = k \frac{q_1 q_2}{r}$$



# Chapter 28 – Summary

- 28.3 Dipoles ... nevermind
- 28.4 Electric potential (Volts) is Potential energy (Joules) over  $q$ .

$$V = U/q$$

- 28.5 In a parallel-plate capacitor

$$U_{\text{elec}} = q E s \rightarrow V = U/q = E s$$

- 28.6 For a point charge

$$V = U_{\text{elec}}/q_2 = k \frac{q_1 q_2}{r q_2} = k \frac{q_1}{r}$$

- 28.7 Got more charges? Sum potentials!

# **Exam Review (all except 4, 5, 10)**

-

A



B



C

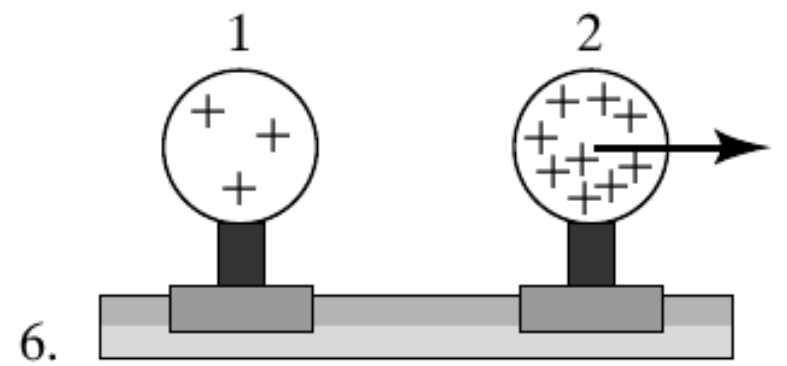
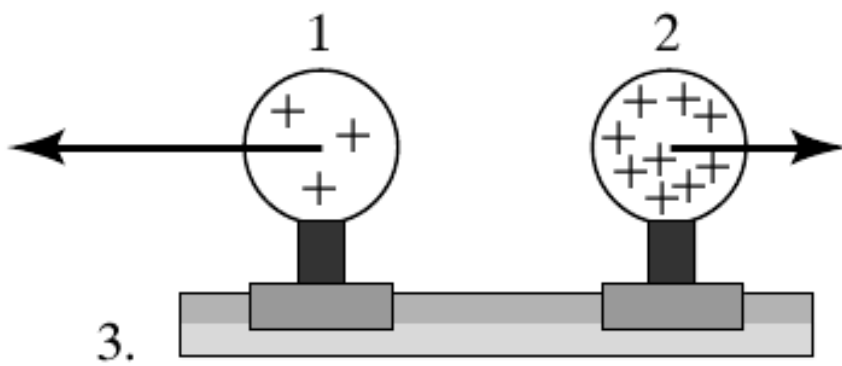
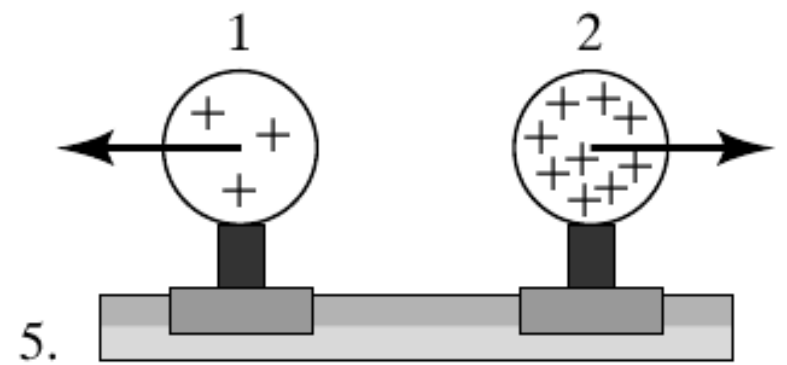
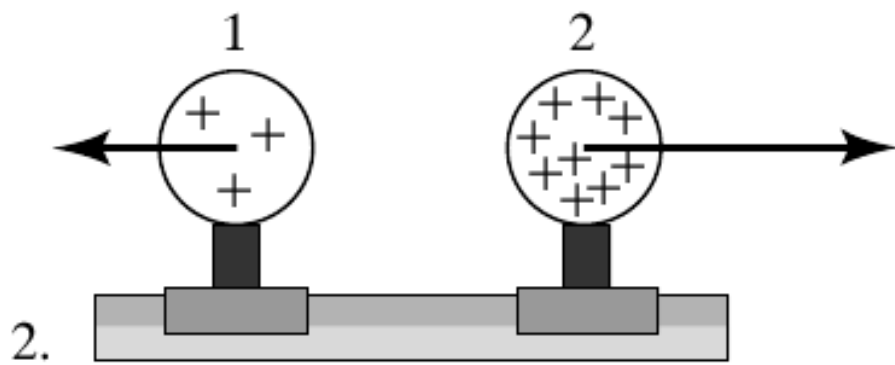
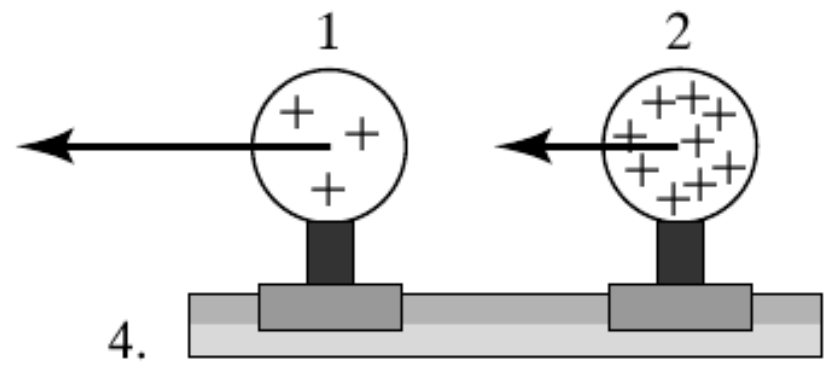
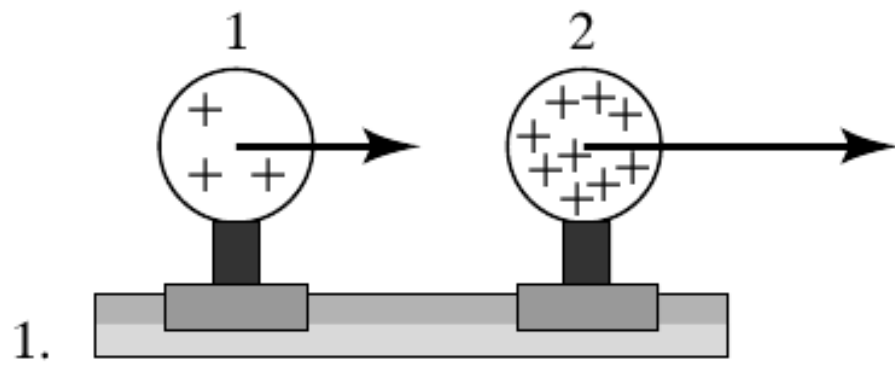


D



E





7. none of the above

(a)

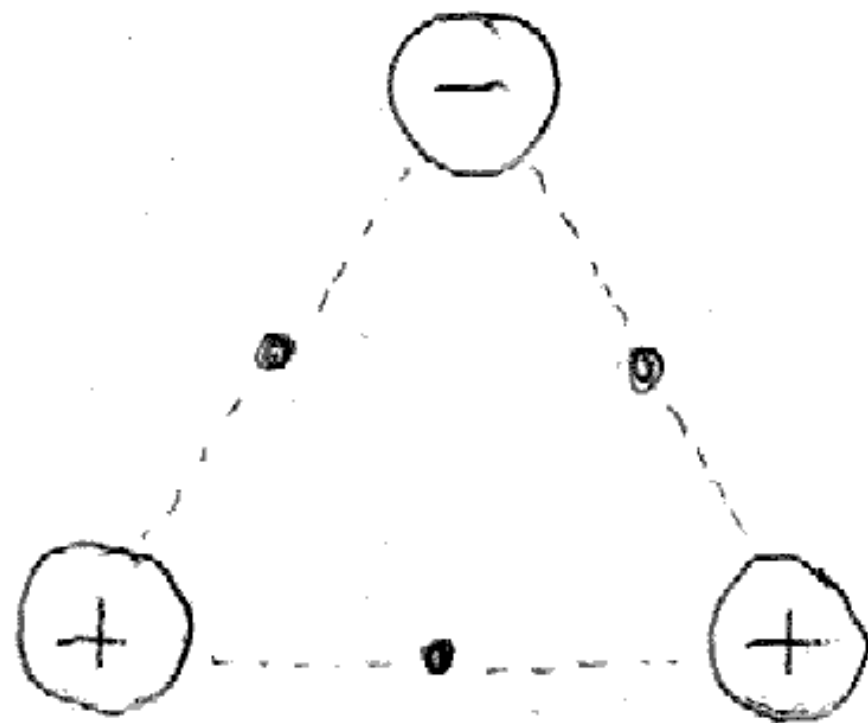
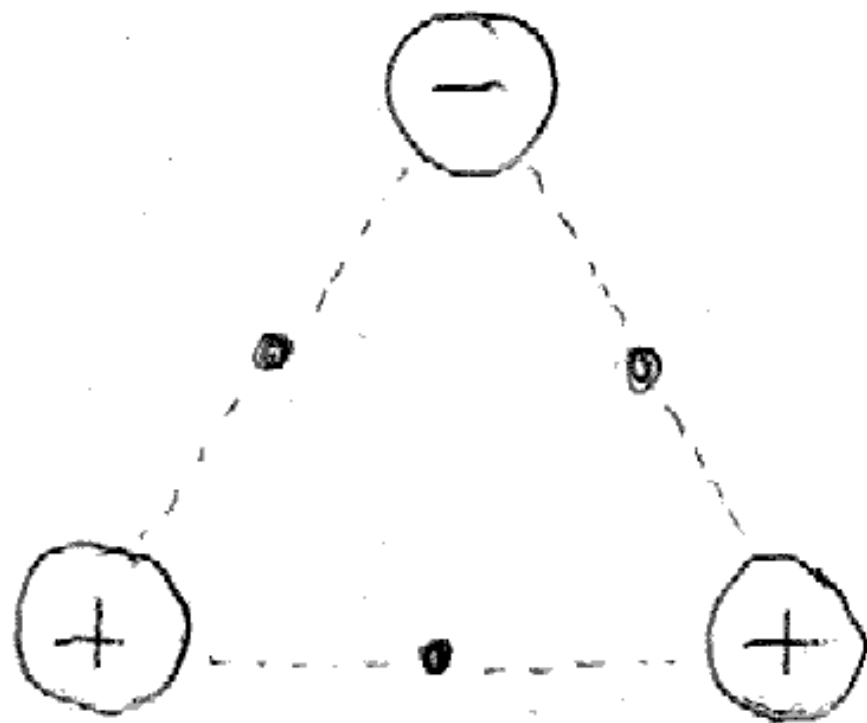
"A"

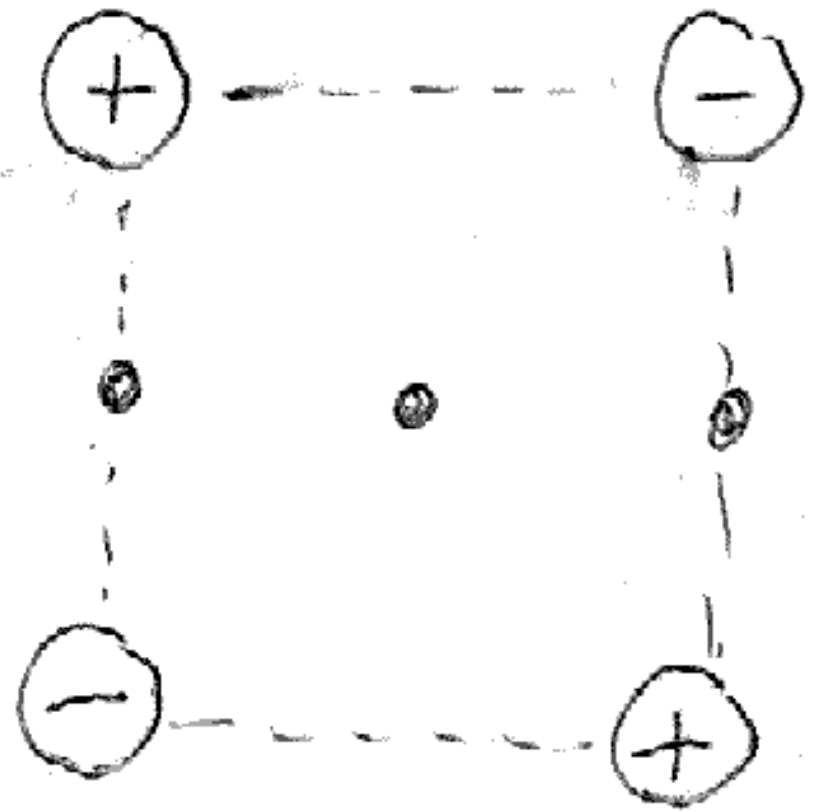
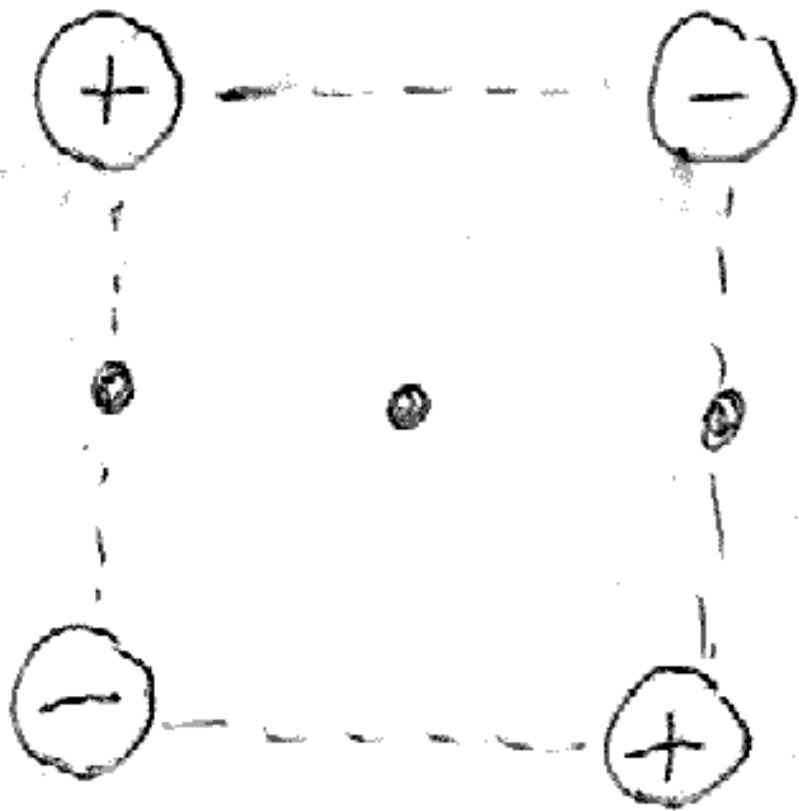
"B"



(b)







## Chapter 29 – Summary

- 29.1 You can integrate  $E(x)$  to get  $V(x)$   
get  $E(x)$  from  $dV/dx$ .

This allows understanding the formula for a parallel plate capacitor.

- 29.2 You “manufacture” potential with a battery, or a Van de Graaf ... or a power plant!

- 29.3  $E$  is the “gradient” of potential  
AND Potentials add in series.

- 29.4 Every point in a conductor is at the same potential.



# Chapter 29 – Summary

- 29.5  $Q=CV$

Capacitances in Parallel Add.

You need a reciprocal formula for capacitances in series.

- 29.6 Capacitors store energy and charge

- 29.7 Dielectric materials let you store more energy and charge in the same space than using air or a vacuum.

# Potential Energy to Power

If you let a charge move through a potential, it acquires kinetic energy. You can create a potential by supplying either kinetic energy or some non-electrical energy.

In our lives, we pay money for potential, either by paying for batteries (chemical energy) or by paying a power company and plugging in.

How does this potential get there?

In practice lots of chemical energy (coal, oil) is converted into electric potential ... and we love it!

# Electrical Units

Potential Energy = Charge x Potential ( $U = Q V$ )

Power = Energy/time =  $QV/t = (Q/t) V = I V$

Charge – Coulombs

Charge/time – Coulombs/second = Current  
(Amperes)

Electric Field – Newtons/Coulomb or Volts/meter

Electric Potential – Joules/Coulomb (or Volts)

Power = Joules/second =

Coulomb/sec x Joules/Coulomb =  $I V$

# Electric Power Plants

“How Power Plants Work Fisk and Crawford”

[Tinyurl.com/fourcornerspowerplant](http://tinyurl.com/fourcornerspowerplant)

<http://tinyurl.com/feedingacoalfiredplant>

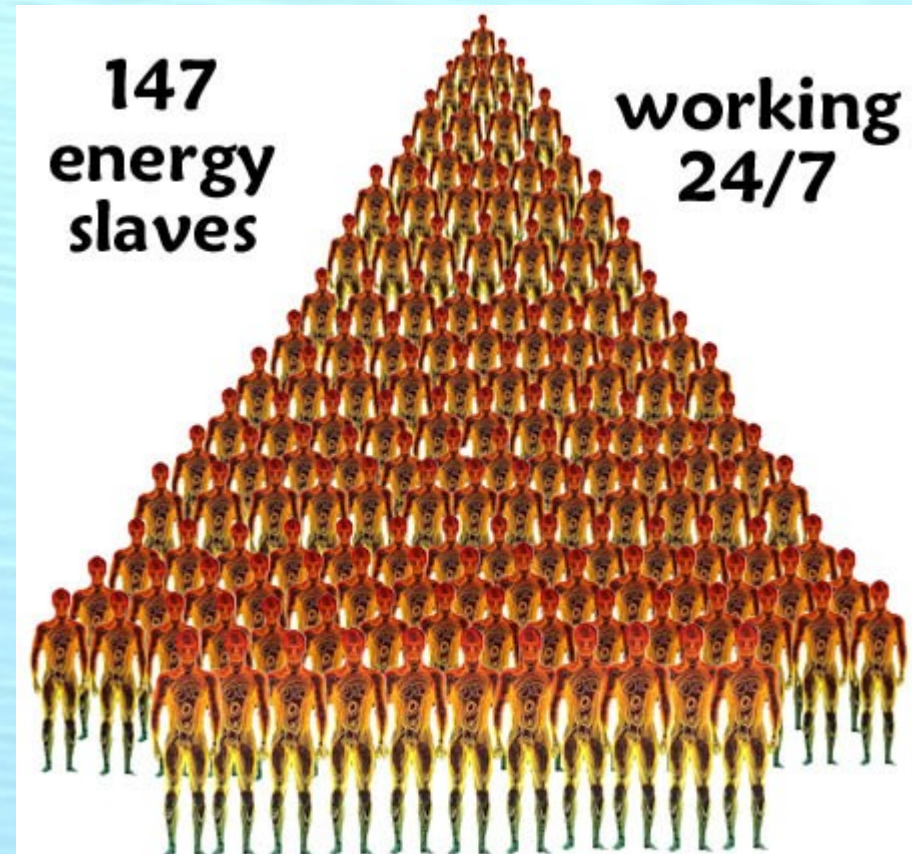
Chapter 33 –  
How electrical  
generators  
work



# We burn fossil fuel to generate electricity

One gallon of gasoline is about 100 million joules  
= 40 kiloWatt Hours, is 600 people working as hard as  
they can for an hour.

Our wonderful lifestyle is  
Sustained by “energy slaves”

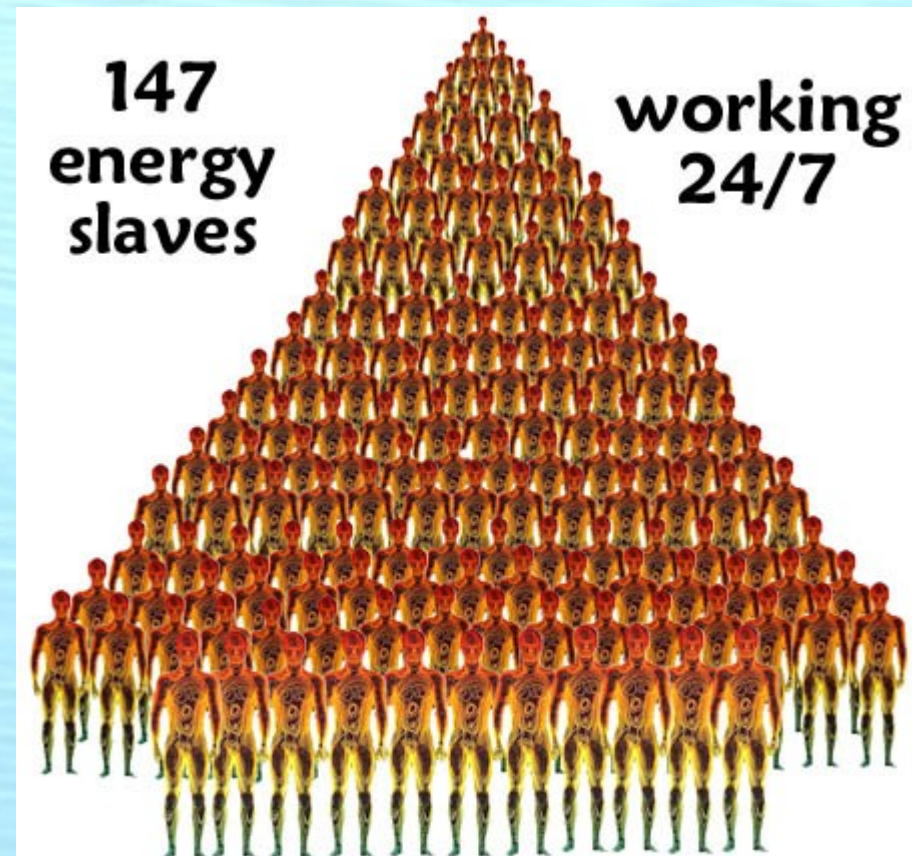


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Sustained by “energy slaves”

You are all Pharoahs.



# Chapter 29

Big Idea: All electric fields represent stored energy. And capacitors are convenient containers for electric fields.

Definition: Capacitance relates Voltage to stored charge. Generally voltage is easier to measure than charge.

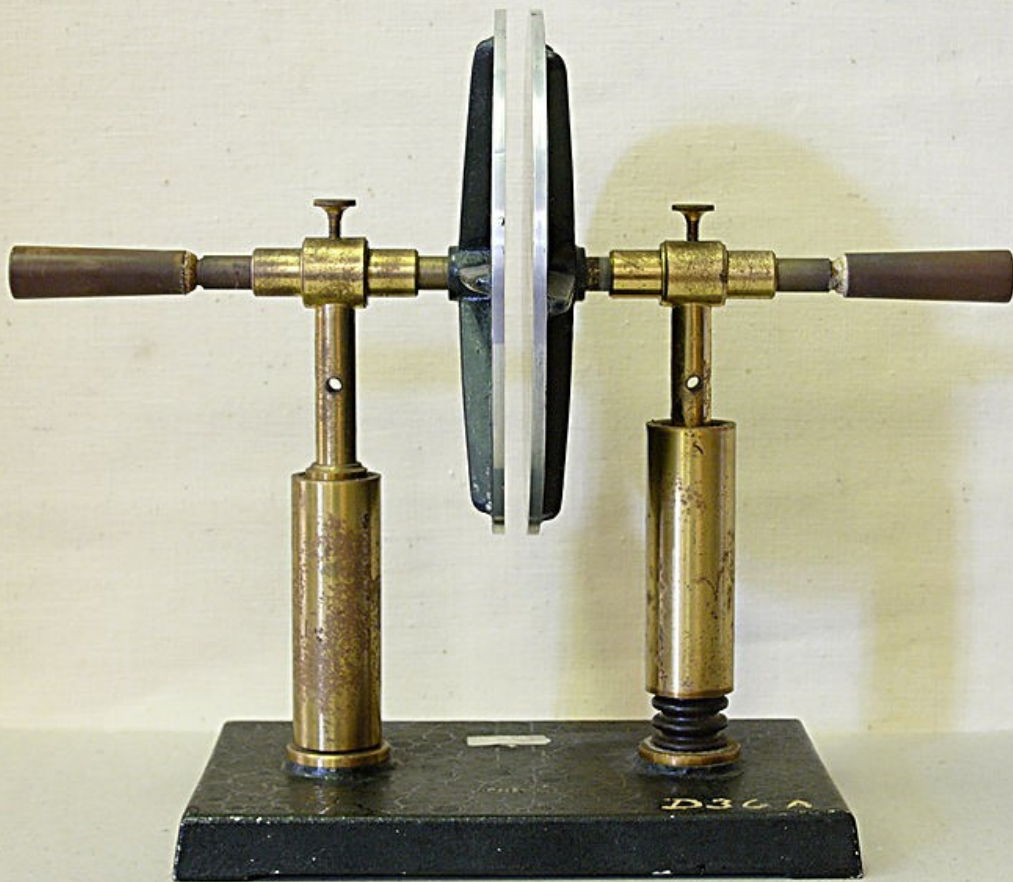
$$C = \frac{Q}{V} \quad Q = C V$$

New SI Unit: “Farad”.  $[C] = [F][V]$   
(Coulomb = Farad x Volt)

It takes ever higher pressure to force more water into a full tank, and ever higher voltage to force more charge onto a charged capacitor.

$$Q = \frac{\epsilon_0}{d} A V$$

$$M_{\text{water}} = \frac{1}{g} A P$$



A water tank gets deeper as you increase pressure, but the plates of a capacitor don't get further apart as you increase voltage.



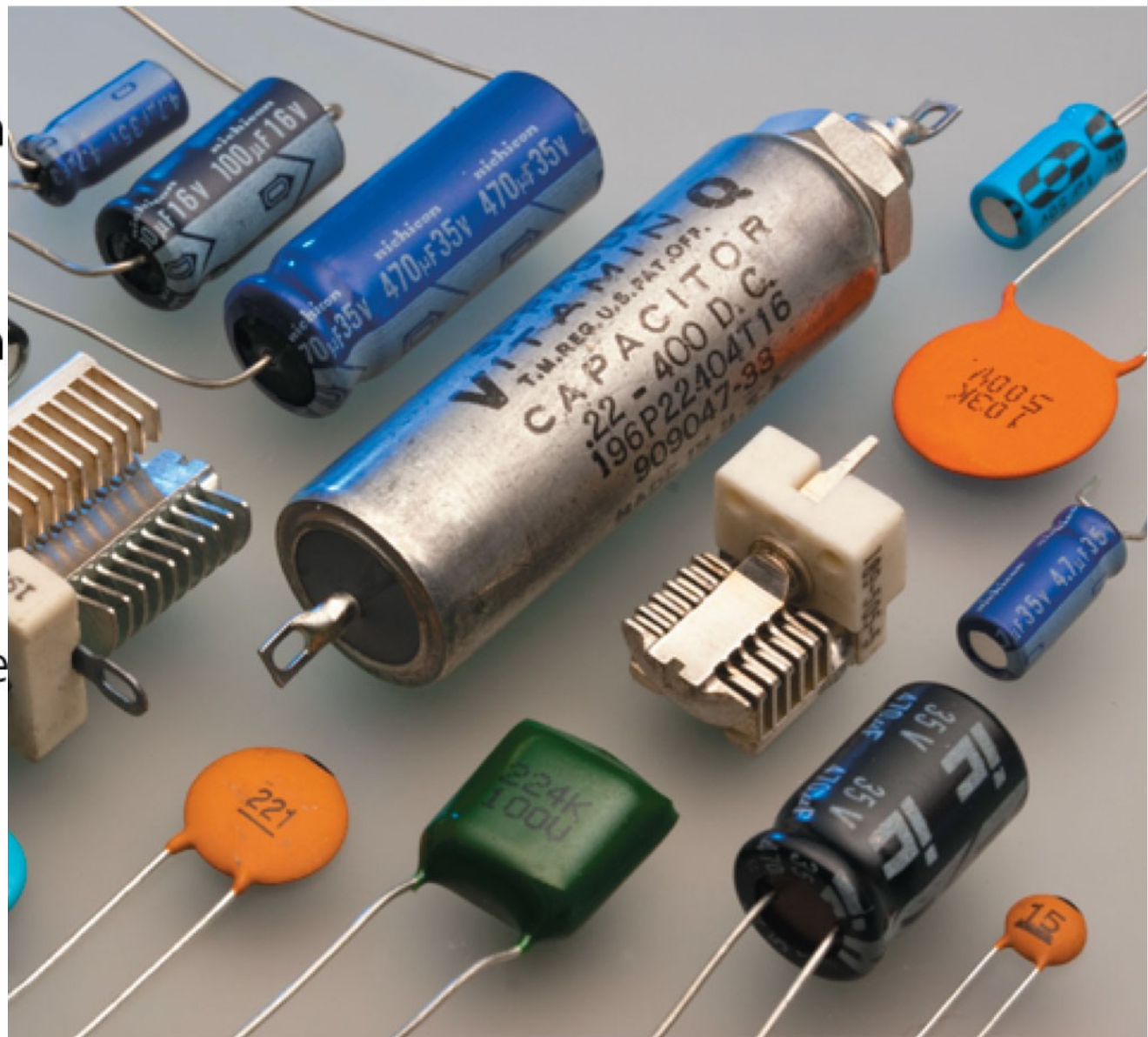
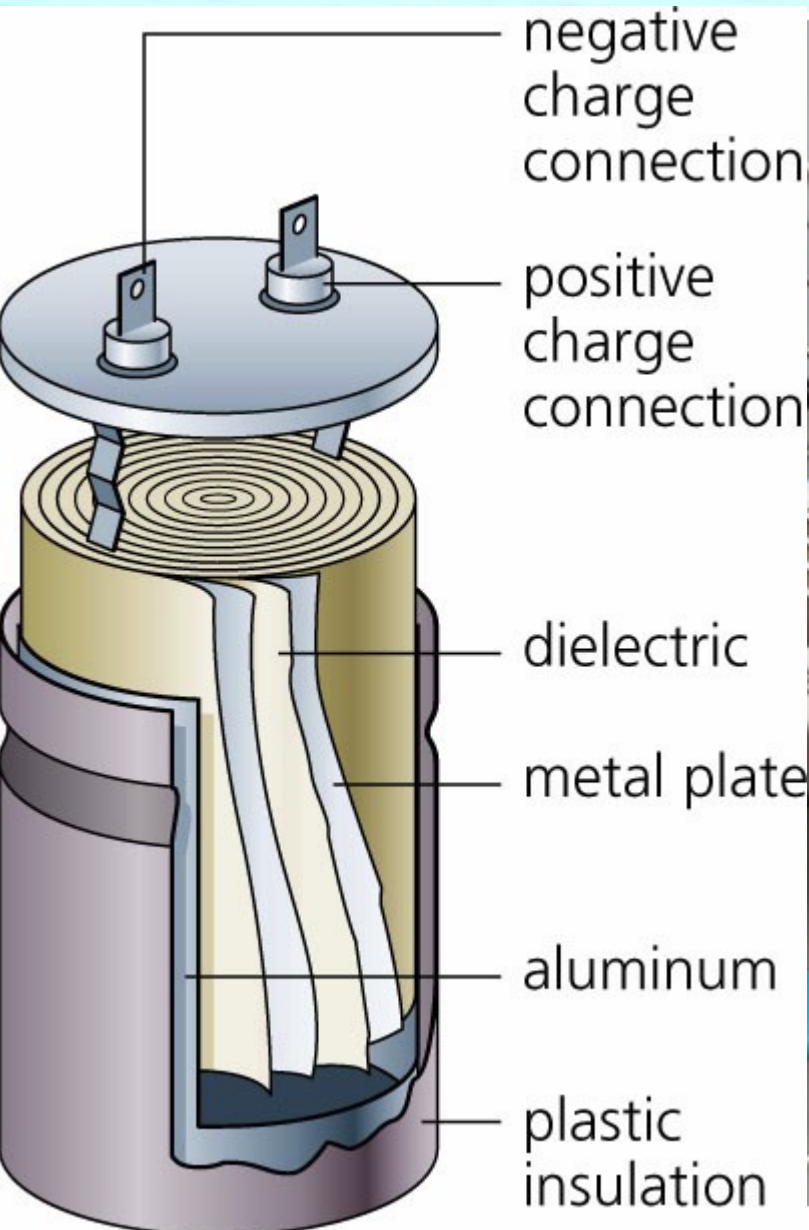
“Capacitance”, sounds like “Capacity”, and it is related. A large bottomed tank has a larger fluid capacity at given pressure than a small tank. “Voltage” is like “Pressure”

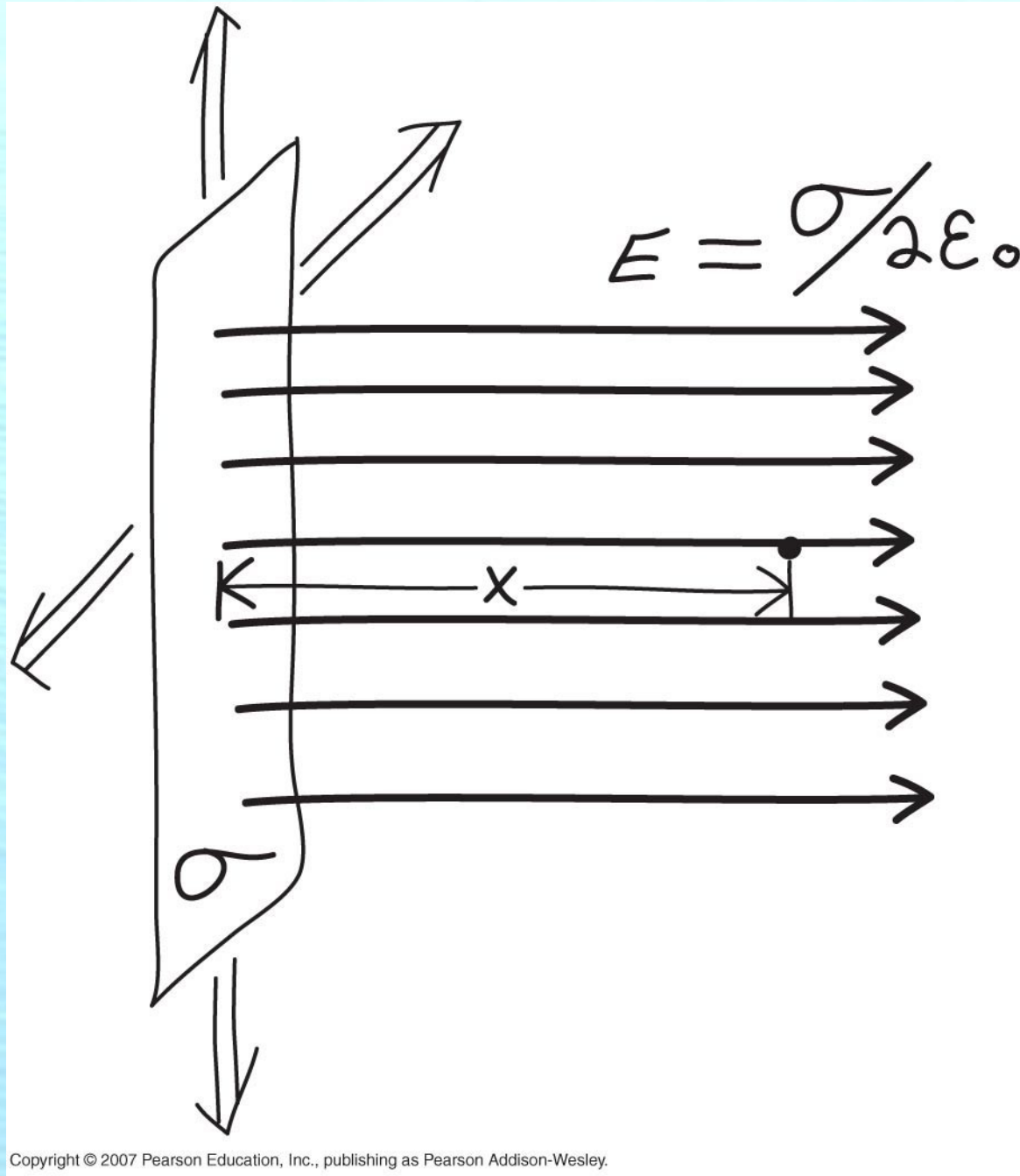
A large area capacitor has a larger charge capacity at given voltage than a small area capacitor.

$$Q = \frac{\epsilon_0}{d} A V \qquad \text{Mass} = \frac{1}{g} A P$$

$$\epsilon_0 = 8.86 \times 10^{-12} \text{ F/m}, \quad (\text{C/V m}), \quad (\text{J/V}^2)$$

# What Commercial Capacitors Look like





## **E-Field of a “large” charged plate:**

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{i}$$

$$\sigma = \frac{Q}{A}$$

$$V = -\int_0^x E \cdot dx'$$

## **E-Field of an infinite charged plate:**

$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{i} \quad V = \frac{U}{q} = -\int_0^x E \cdot dx'$$

## **Electric Potential of an infinite plate:**

$$[A] \quad V = \frac{\sigma^2}{4\epsilon_0}$$

$$[B] \quad V = -\frac{\sigma^2}{4\epsilon_0}$$

$$[C] \quad V = \frac{\sigma}{2\epsilon_0} x$$

$$[D] \quad V = -\frac{\sigma}{2\epsilon_0} x$$

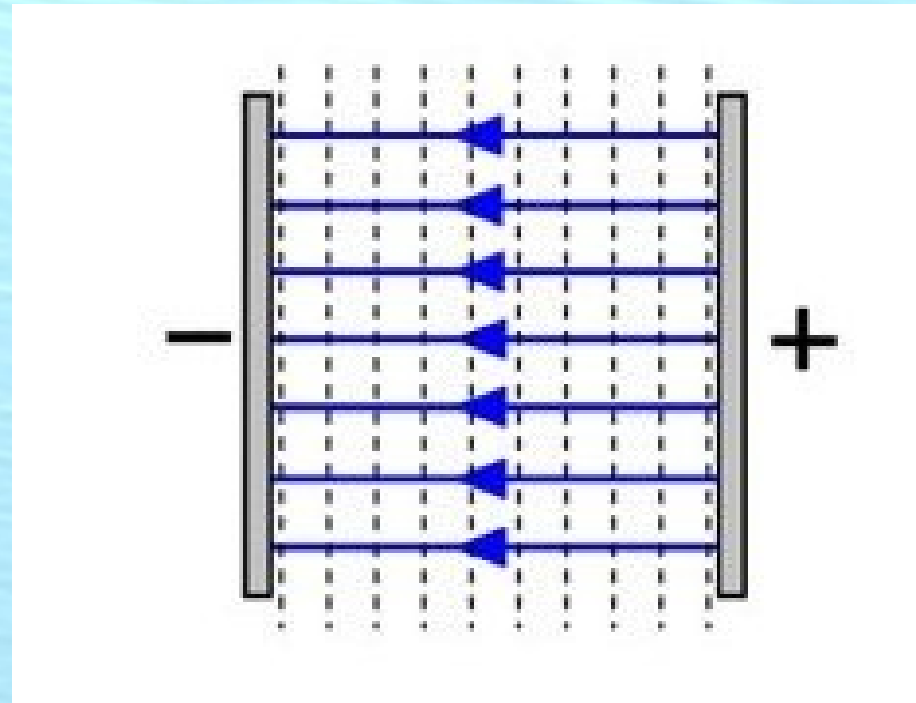
Electric potential of TWO large plates  
(Area “A” separation “d”) ...

Electric field is doubled because two charged  
plates of opposite sign.

$$\vec{E} = \frac{-\sigma}{\epsilon_0} \hat{i}$$

$$V = -\vec{E} \cdot \Delta \vec{r} = E d$$

$$V = \frac{\sigma}{\epsilon_0} x = \frac{\sigma}{\epsilon_0} d$$



# Deriving Parallel Plate Formula

$$[1] Q = C V$$

Definition of Capacitance

$$[2] V = \frac{\sigma}{\epsilon_0} d$$

Shown on last page

$$[3] \sigma = \frac{Q}{A}$$

Definition of surface charge density

$$[4] V = \frac{Q}{\epsilon_0 A} d$$

Plug 3 into 2

$$[5] Q = \frac{\epsilon_0 A}{d} V$$

Solve for Q

$$[6] C = \frac{\epsilon_0 A}{d}$$

**How many capacitors are in your dorm room or house?**

**(A) None – I do not own a time machine or a DeLorean.**



**(B) About a dozen – Capacitors are energy storage and signal filtering devices used in power supplies for all electronics.**

**(C) Billions**

**How many capacitors are in your dorm room or house?**

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**(B) About a dozen – Capacitors are energy storage and signal filtering devices used in power supplies for all electronics.**

**(C) Billions – Capacitors store energy and are also elements of the memory cell in digital devices.**



Note that the parallel plate formula only has “geometric” variables. Capacitance is a property of a set of conductors and does not depend on charge or voltage (or any other electric variables)

$$C = \frac{\epsilon_0 A}{d}$$

**[Ex. 1] Find the capacitance of a parallel plate capacitor consisting of circular plates 10 cm in radius separated by 1.5 mm.**

$$\epsilon_0 = 8.86 \times 10^{-12} \text{ F/m}$$

$$C = \epsilon_0 \frac{A}{d}$$

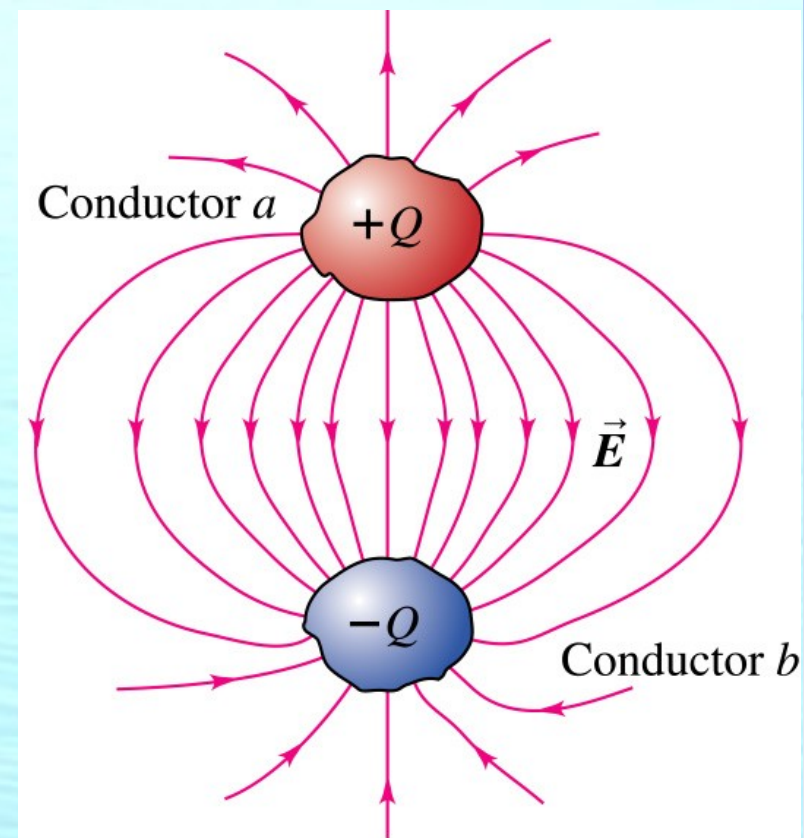
$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

The two conductors  $a$  and  $b$  are insulated from each other, forming a capacitor. You increase the charge on  $a$  to  $+2Q$  and increase the charge on  $b$  to  $-2Q$ , while keeping the conductors in the same positions.

What effect does this have on the capacitance  $C$ ?

- A.  $C$  is multiplied by a factor of 4
- B.  $C$  is multiplied by a factor of 2
- C.  $C$  is unchanged
- D.  $C$  is multiplied by a factor of  $1/2$
- E.  $C$  is multiplied by a factor of  $1/4$



**[Ex. 2] A capacitor's plates hold  $1.3 \mu\text{C}$  when it is charged to  $80\text{ V}$ . What is its capacitance?**

$$C = \epsilon_0 \frac{A}{d}$$

$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

**[Ex. 3] A stereo receiver contains a 2500  $\mu\text{F}$  capacitor charged to 35 V.**

**How much energy does it store?**

$$C = \epsilon_0 \frac{A}{d}$$

$$C = \frac{Q}{V}$$

$$U = \frac{1}{2} C V^2$$

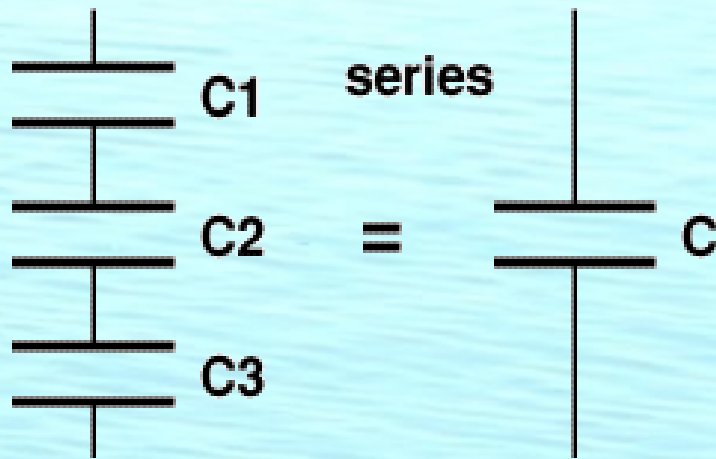
You reposition the two plates of a capacitor so that the capacitance doubles.

If the charges  $+Q$  and  $-Q$  on the two plates are kept constant in this process, what happens to the potential difference  $V_{ab}$  between the two plates?

- A.  $V_{ab}$  is multiplied by a factor of 4
- B.  $V_{ab}$  is multiplied by a factor of 2
- C.  $V_{ab}$  is unchanged
- D.  $V_{ab}$  is multiplied by a factor of  $1/2$
- E.  $V_{ab}$  is multiplied by a factor of  $1/4$

$$Q = CV$$

# Capacitors in Series and Parallel

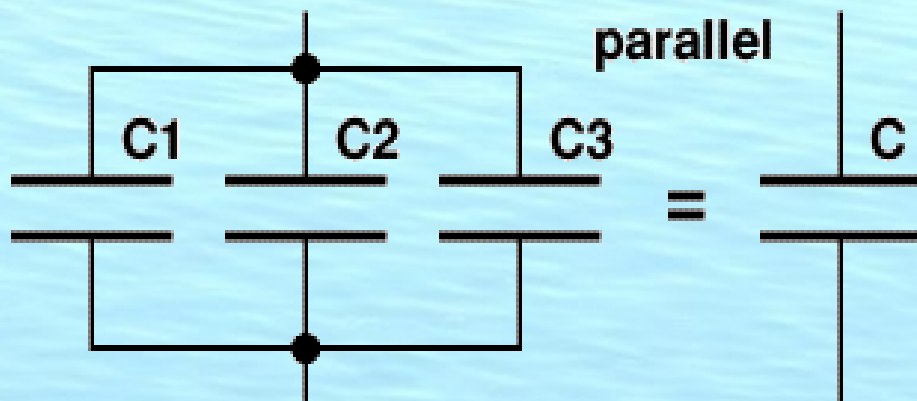


Caps in series have the

“bottom wire” or one

Connected to the “top wire”

Of the next.



Caps in parallel have all

Their tops connected to

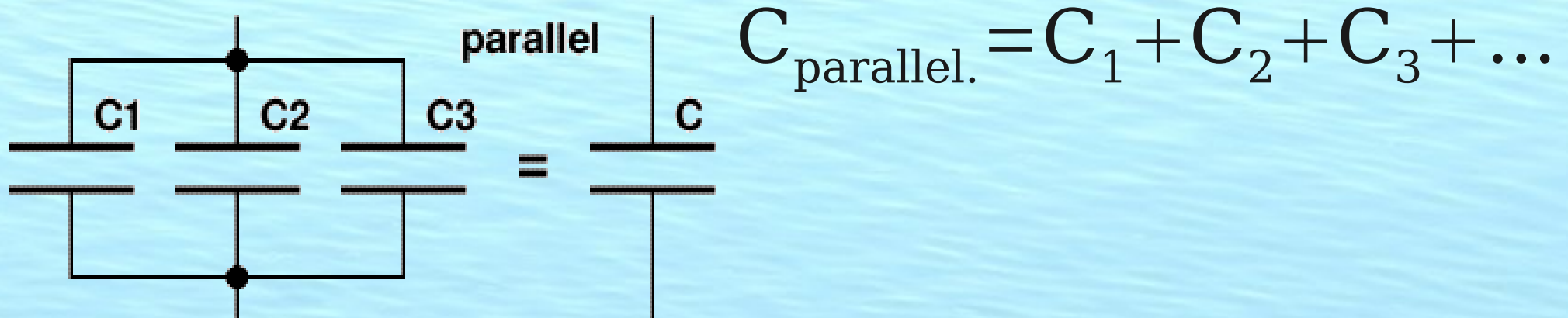
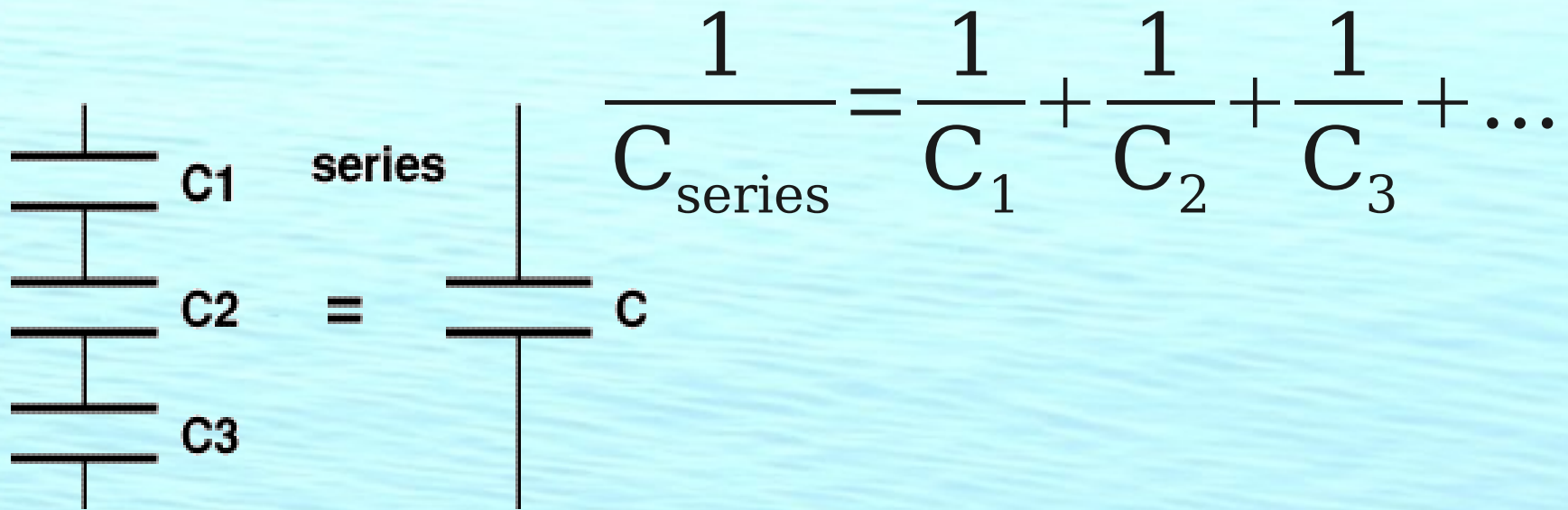
One wire and all their

Bottoms also connected to

A second wire.

Caps in series have equal charges

# Capacitors in Series and Parallel



Caps in parallel have equal voltages.

Caps in series have equal charges.



A 12 microfarad capacitor is connected with a 6 microfarad capacitor as shown. The equivalent capacitance of this combination is:

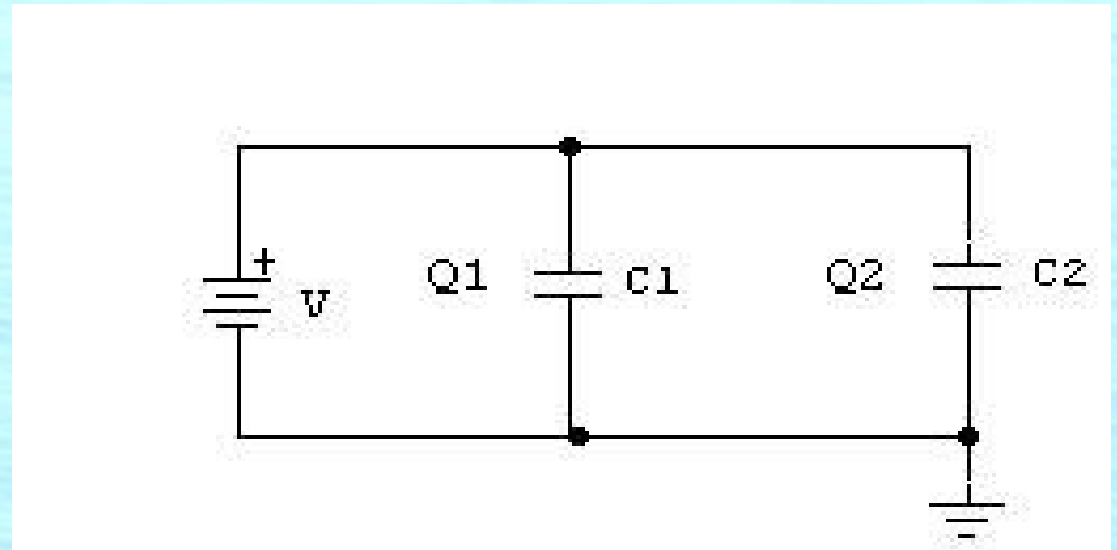
A.  $C_{eq} = 18 \mu\text{F}$

B.  $C_{eq} = 9 \mu\text{F}$

C.  $C_{eq} = 6 \mu\text{F}$

D.  $C_{eq} = 4 \mu\text{F}$

E.  $C_{eq} = 2 \mu\text{F}$



Two capacitors are connected together as shown. What is the equivalent capacitance of the two capacitors as a unit?

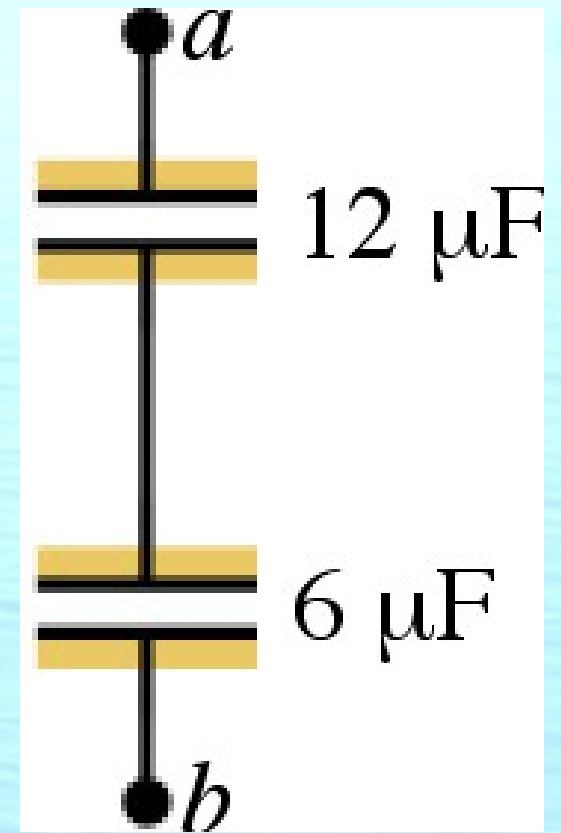
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D.  $C_{eq} = 4 \mu\text{F}$

E.  $C_{eq} = 2 \mu\text{F}$



Network of capacitors:

Replace parallel elements with an equivalent cap. Combine that equivalent cap in series with what is left.

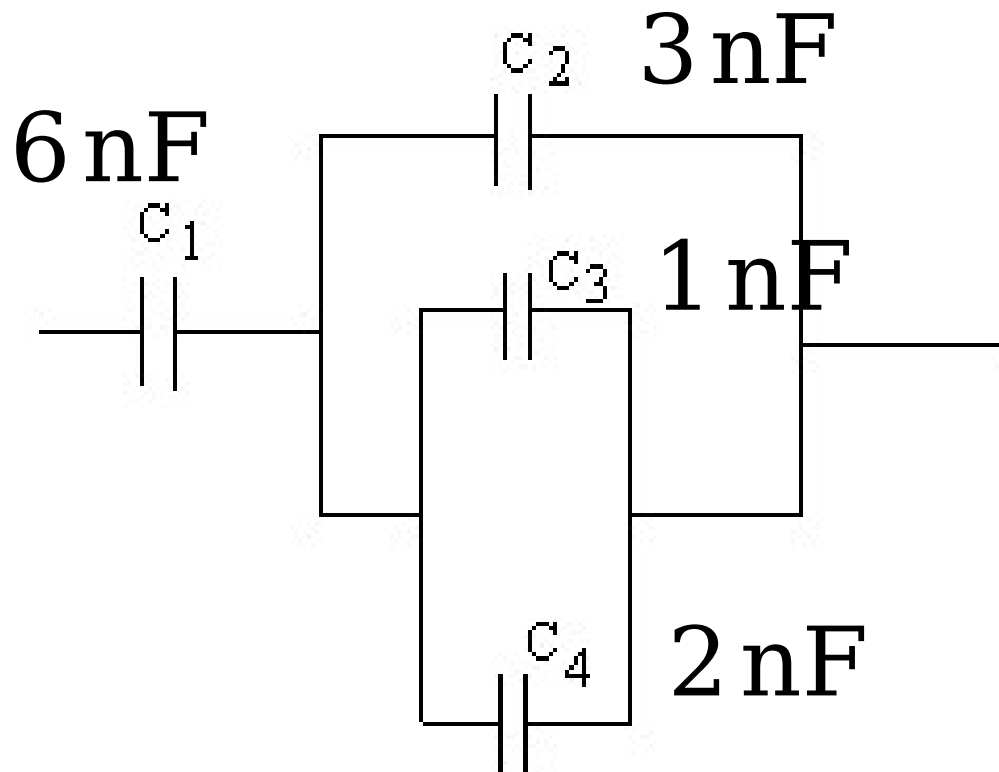
[A] 1 nF

[B] 2 nF

[C] 3 nF

[D] 6 nF

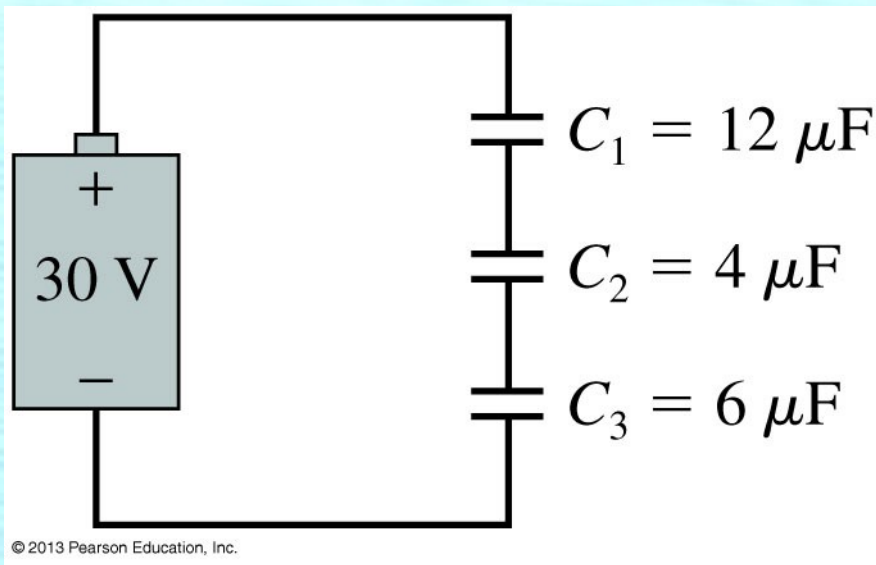
[E] 12 nF



**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

**What is the voltage across each capacitor?**



Caps in parallel have equal voltages.

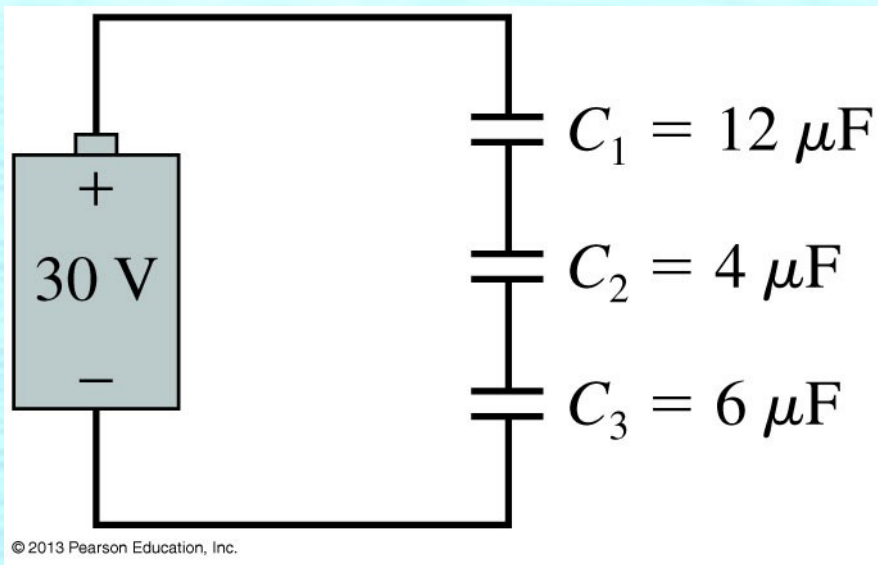
Caps in series have equal charges.

Voltages in series add

**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

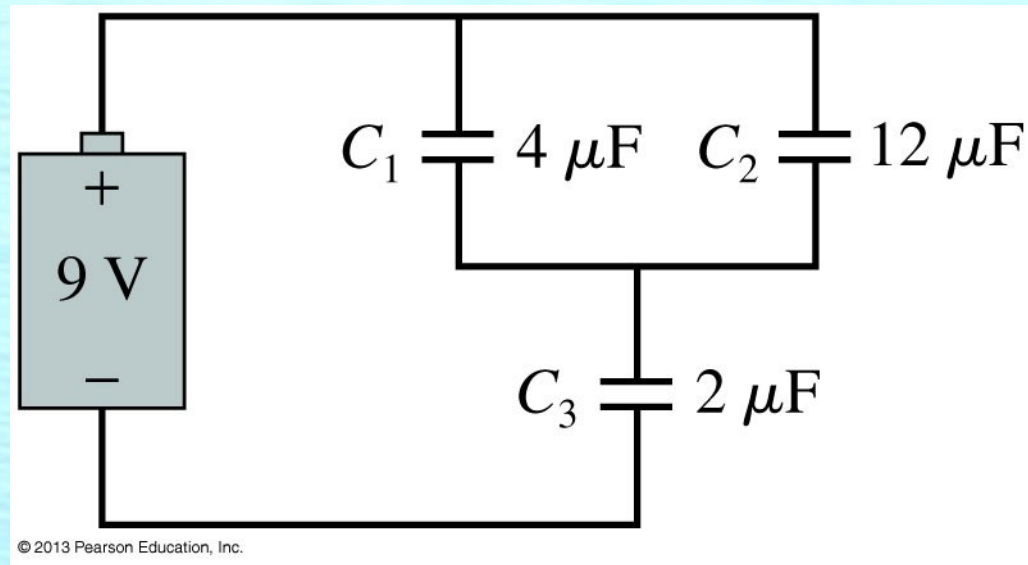
**What is the voltage across each capacitor?**



**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

**What is the voltage across each capacitor?**



Caps in parallel have equal voltages.

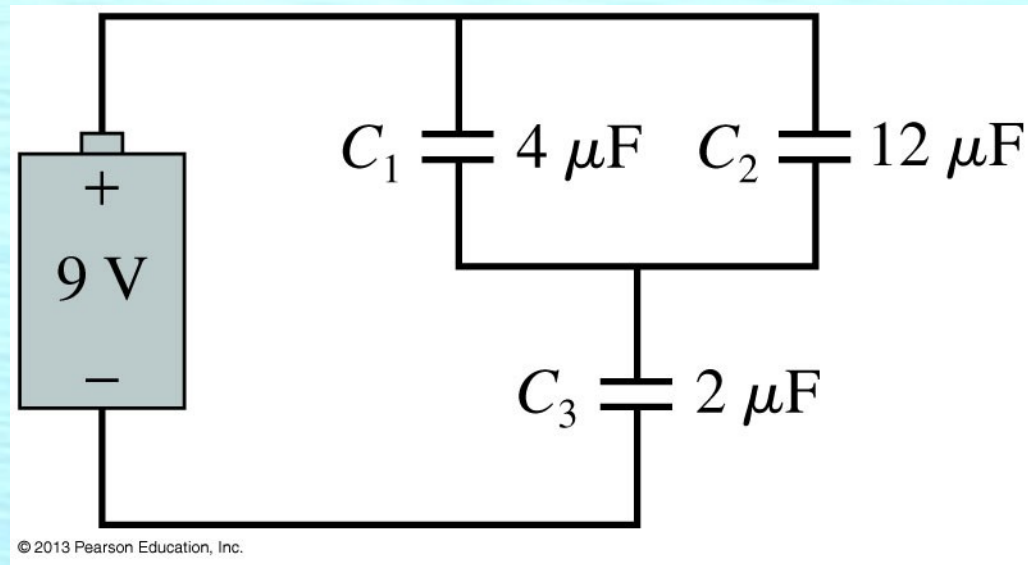
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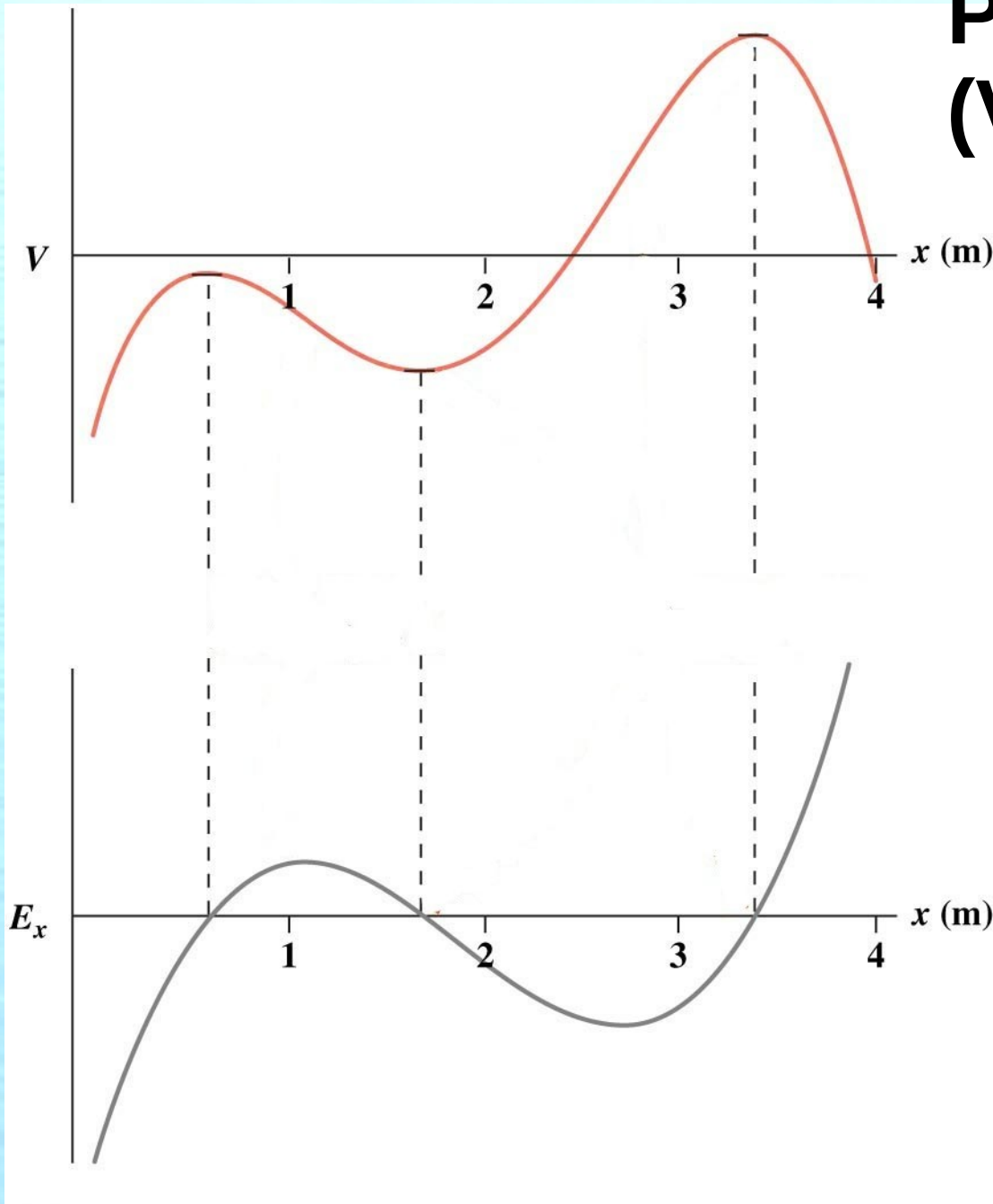
**What is the equivalent capacitance?**

**What is the charge on each capacitor?**

**What is the voltage across each capacitor?**



# Potential (Voltage) in 1-D



$$V(x) = -\int E_x dx$$

$$E_x = -\frac{dV}{dx}$$



Consider a point  $P$  in space where the electric potential is zero. Which statement is correct?

- A. A charge placed at  $P$  would feel no electric force
- B. The electric field near  $P$  is directed toward  $P$
- C. the electric field near  $P$  is directed away from  $P$
- D. none of the above
- E. not enough information given to decide