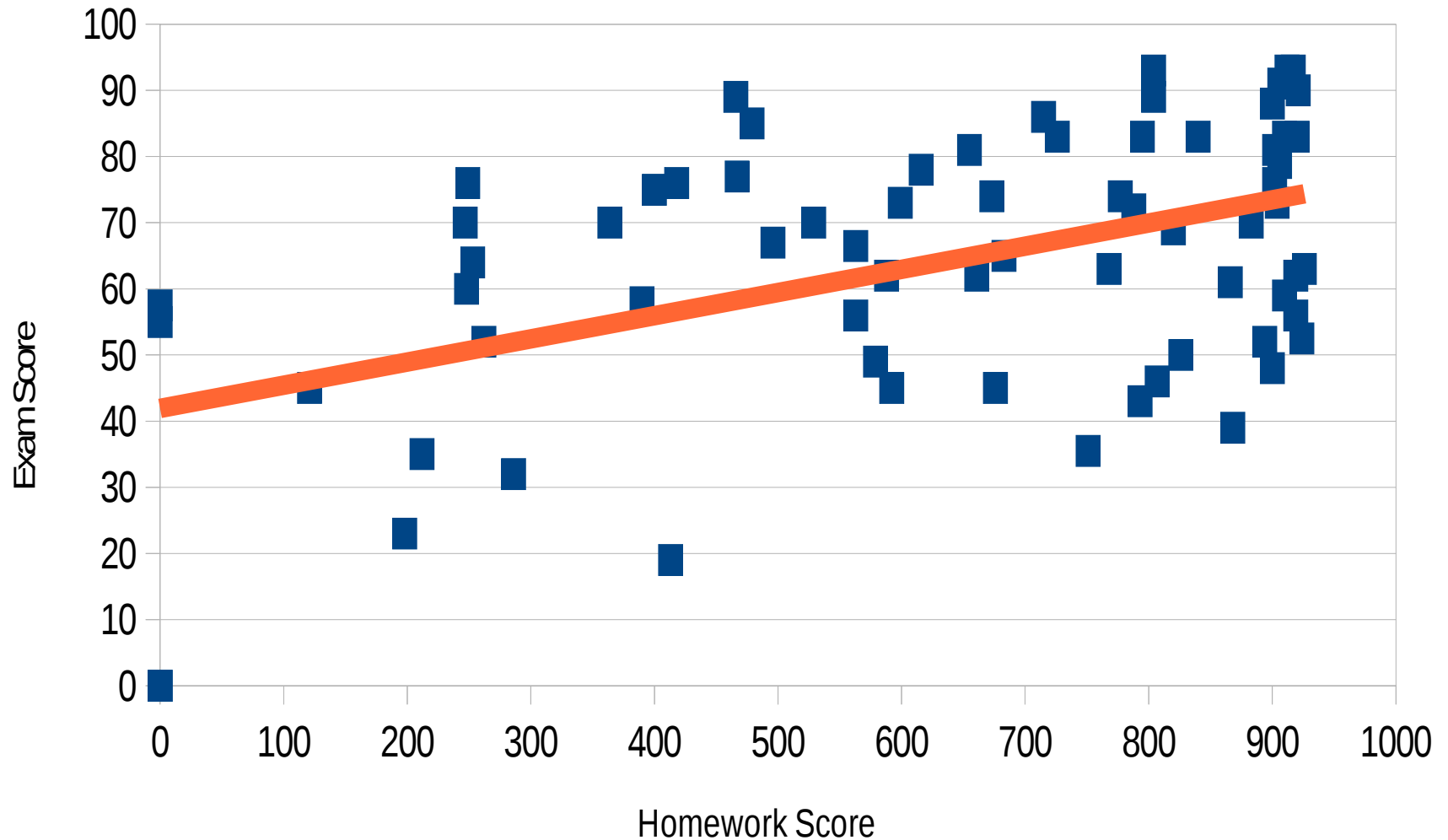


Physics 122 – Class #15 – Outline

- About Exam #1 (and #2)
- Electric Field lines
- Effect of Electric Field on motion
- Field of continuous distributions
- Derivation of field of a line

Do homework ... increase test score

Relation between Homework and uncurved test



High Homework but Low Test Score?

- Working with a group but not understanding the result?
- Taking too many short cuts by Googling?
- What else? ... Come see me.

Educational and Life Philosophy

- Don't be like Cleopatra



Educational and Life Philosophy

- Don't be like Cleopatra
- “I will try harder” ... does not work if there is some reason that you cannot.
 - Holes in background?
 - Difficult personal life?
 - Too many classes?
 - Disability?
- Don't do the same thing which did not work well and expect a different result.
- A 2-4 points extra credit for a reflective essay on what did not work on exam (by Friday) (mpsonnenfeld@gmail.com)

Ask Cleo ...

- Make your index card as you do your home work.
- You will see what equations you needed.
- Those are the same ones you will probably need on the test.



Ask Cleo ...

- Read book before lecture
(or at least read the book)
- Take notes on content
(if you like) but
- **ALSO** work the green sections of the book with pencil and paper.
- This is called “active reading” and prevents ...

Ask Cleo ...

- Read book before lecture (or at least read the book)
- Take notes on content (if you like) but
- ALSO work the green sections of the book with pencil and paper.
- This is called “active reading” and prevents ...



Starfish ...

I will report all D's and F's on "Starfish"

You are not "in trouble". The theory is tutors etc. are supposed to contact you an offer to help.

Let me know if it helps or DOES NOT help. I do not have to report these grades, and I won't if it bothers you.

Test #2 ... before or after break?

Chapters 25, 26 ... if next week

All vectors ... all the time.

Chapter 25, 26, 27 ... if after ... more time to do homework.

What did we learn from the discussion Of empirical electrostatics?

[A] Only electrical conductors may be charged

[B] Only electrical insulators may be charged

[C] Both conductors and insulators may be charged

[D] You can't charge anything, only polarize it.

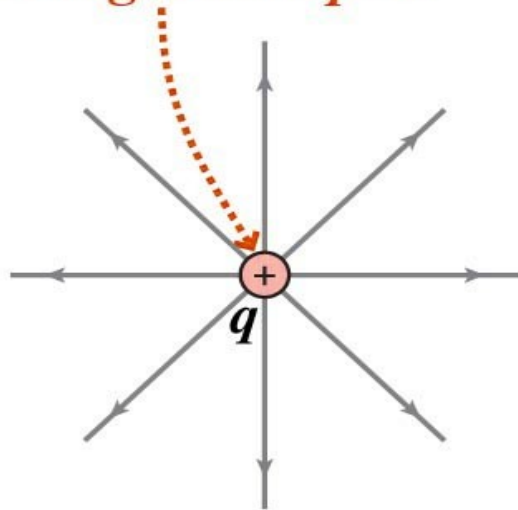
Physics 122 – Class #15 – Outline

- About Exam #1 (and #2)
- **Electric Field lines**
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Electric Field Lines

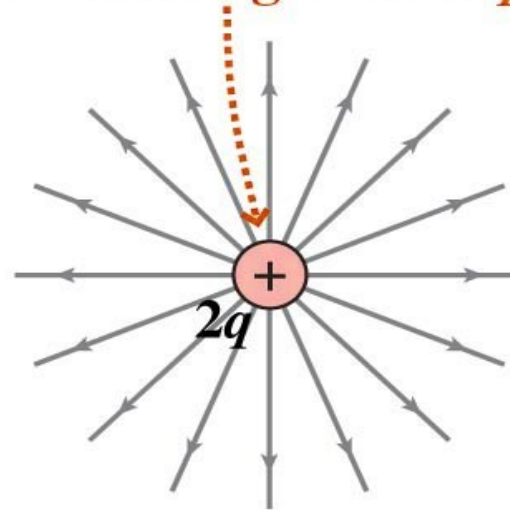
- ♦ A way of getting intuition for the fields caused by a few charges (without calculating)
- ♦ Positive charges “emit” field lines.
- ♦ Negative charges “absorb” field lines.
- ♦ Field lines begin at + charge and end at infinity or negative charge.
- ♦ The tangent to an electric field line gives direction of force
- ♦ Electric field lines do not cross

Eight lines begin on $+q \dots$



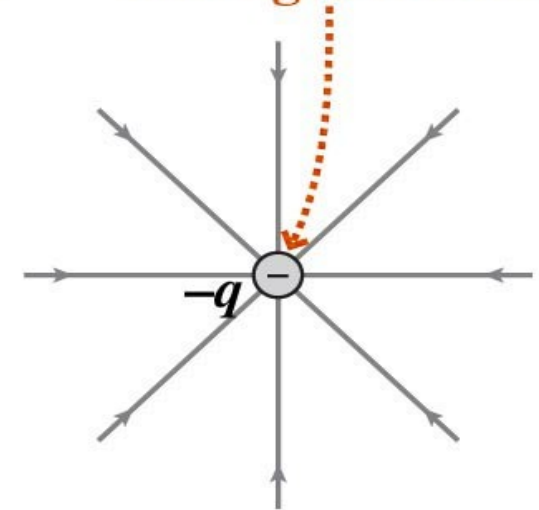
(a)

so 16 lines begin on $+2q \dots$



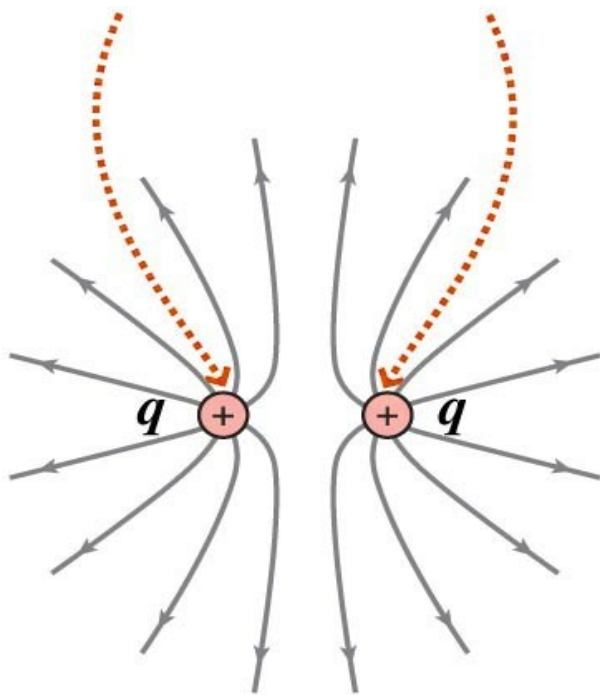
(b)

and eight end on $-q$.



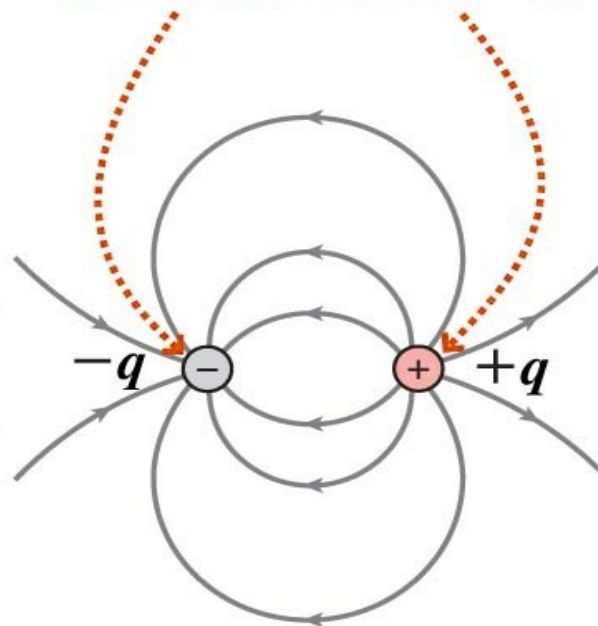
(c)

Eight lines begin on each $+q$.



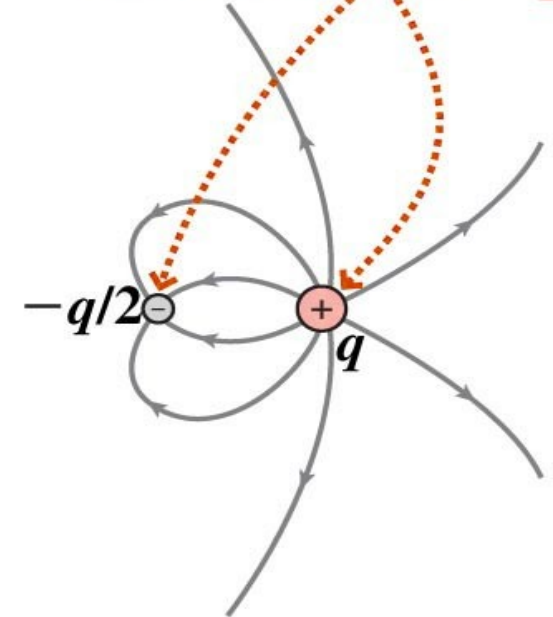
(d)

Eight lines begin on $+q$ and eight end on $-q$.



(e)

Eight lines begin on $+q$.
Four go to infinity and four end on $-q/2$.



(f)

PheT ...

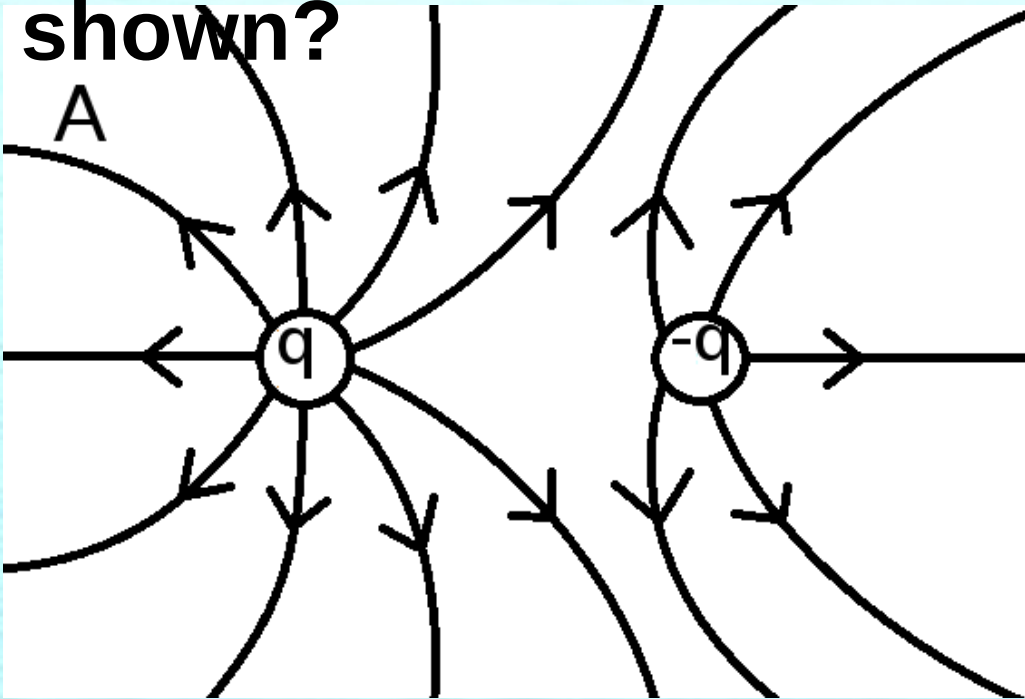
Charges and fields

Electric field of dreams

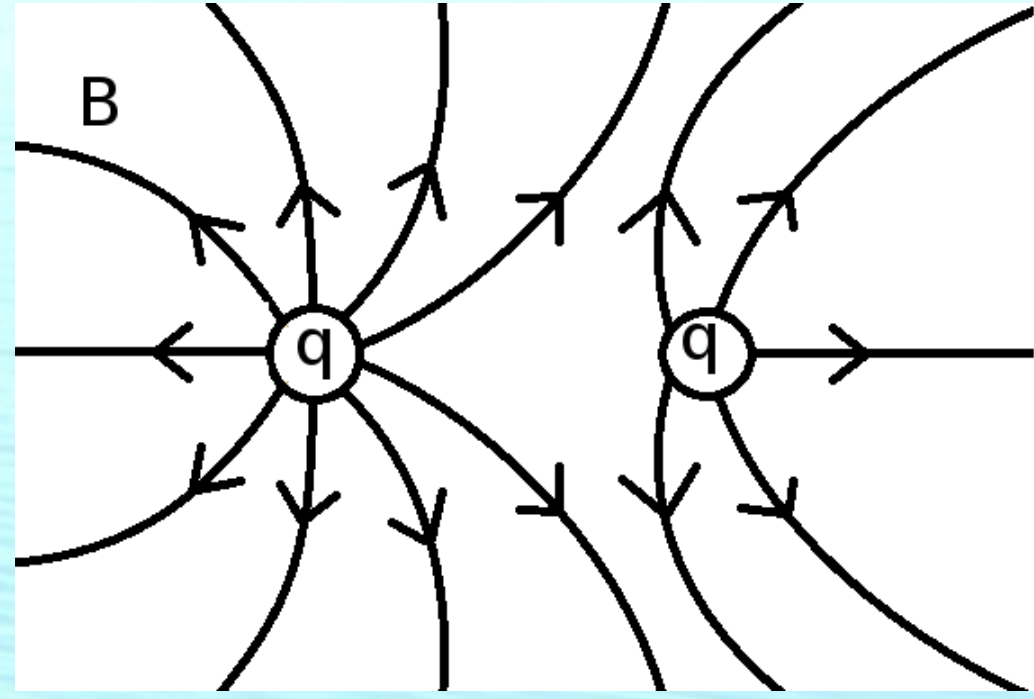
Which set of field lines corresponds to charges

shown?

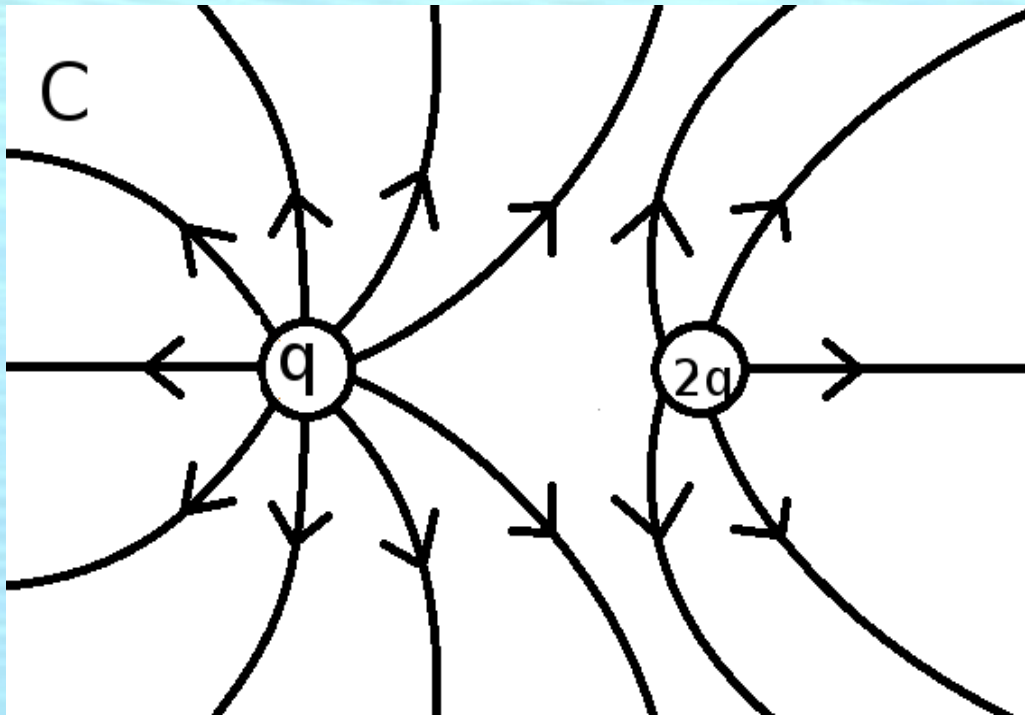
A



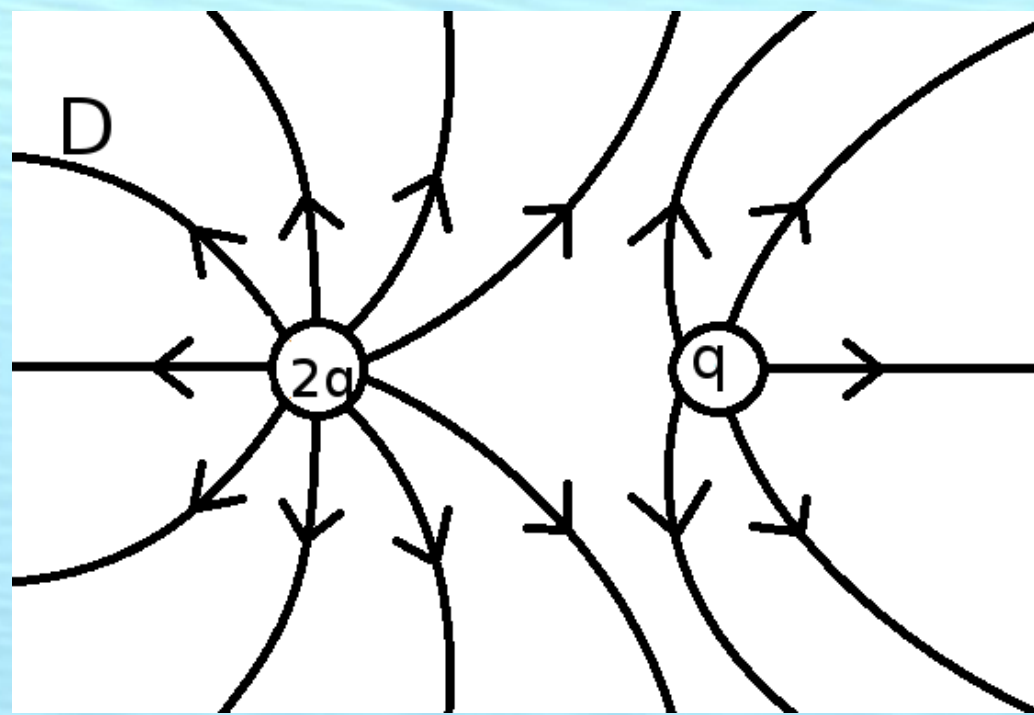
B



C



D



Physics 122 – Class #15 – Outline

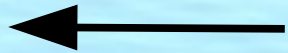
- About Exam #1 (and #2)
- Electric Field lines
- **Effect of Electric Field on motion**
- Field of continuous distributions
- Derivation of field of a line

Clicker



The green arrows represent velocity vectors vs. time for a positively charged particle. Which arrow below represents the Electric field direction causing this?

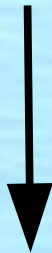
A



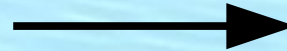
B



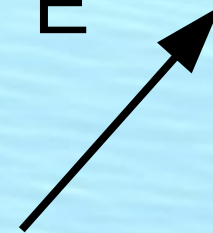
C



D



E

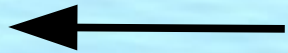


Clicker



The green arrows represent velocity vectors vs. time for a negatively charged particle. Which arrow below represents the Electric field direction causing this?

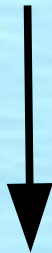
A



B



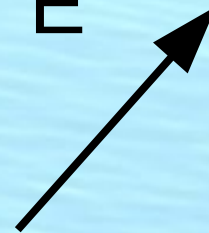
C



D



E



Problems

Electric field needed to accelerate a proton to 1000 km/s from rest in 2 meters?

$$q_p = 1.6 \times 10^{-19} \text{ C} \quad m_p = 1.67 \times 10^{-27} \text{ kg}$$

$$W = \vec{F} \cdot \Delta \vec{r} = K_f - K_i$$

$$v_f^2 - v_i^2 = 2 a \Delta x$$

Electric field needed to accelerate a proton to 1000 km/s from rest in 2 meters?

$$q_p = 1.6 \times 10^{-19} \text{ C}$$

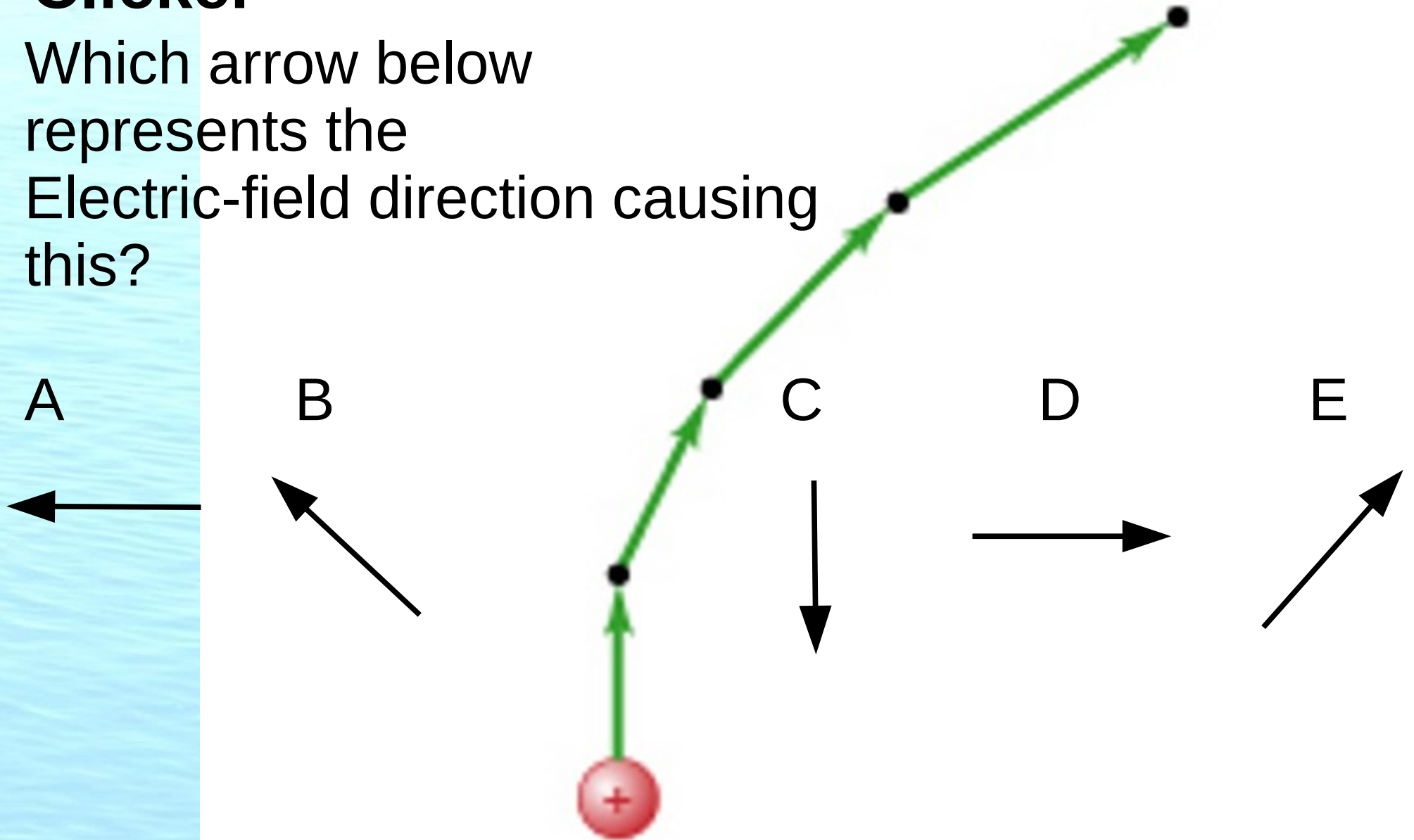
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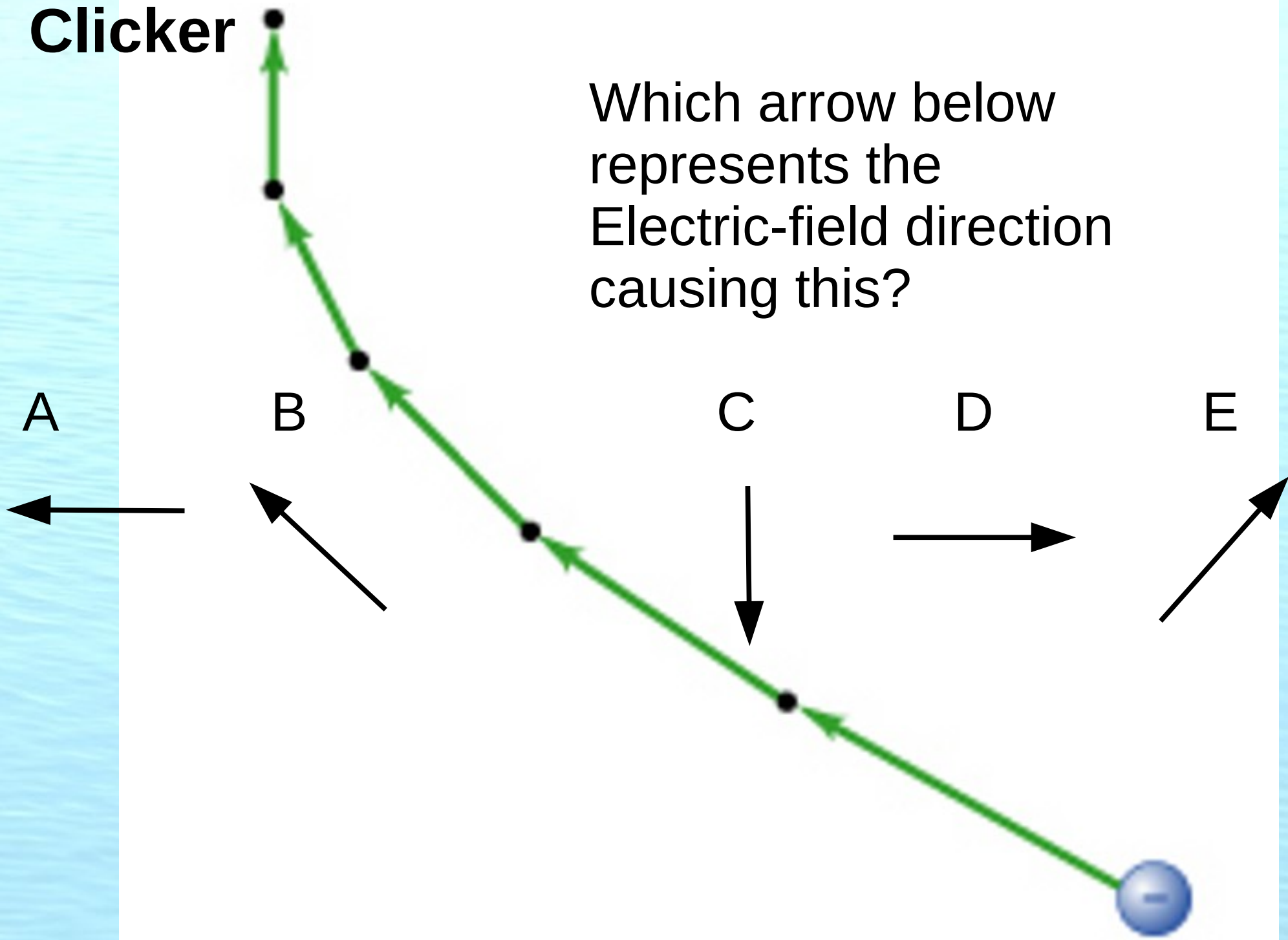
Clicker

Which arrow below represents the Electric-field direction causing this?



Clicker

Which arrow below represents the Electric-field direction causing this?



Physics 122 – Class #15 – Outline

- About Exam #1 (and #2)
- Electric Field lines
- Effect of Electric Field on motion
- **Field of continuous distributions/symmetry**
- Derivation of field of a line

Relation between symmetry and Electric Field

If you can't physically tell where you are with respect to a charge, a line, or a surface (or any

Other charge distribution) then the Electric field direction cannot give you a hint.

Consider first an infinitely long cylinder.

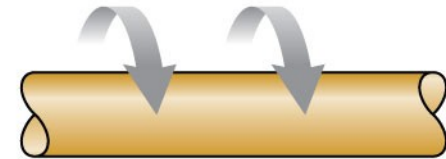
Relation between symmetry and Electric Field



Original cylinder



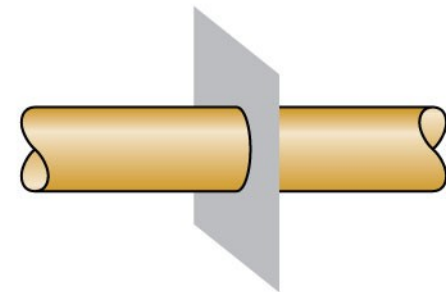
Translation parallel to the axis



Rotation about the axis



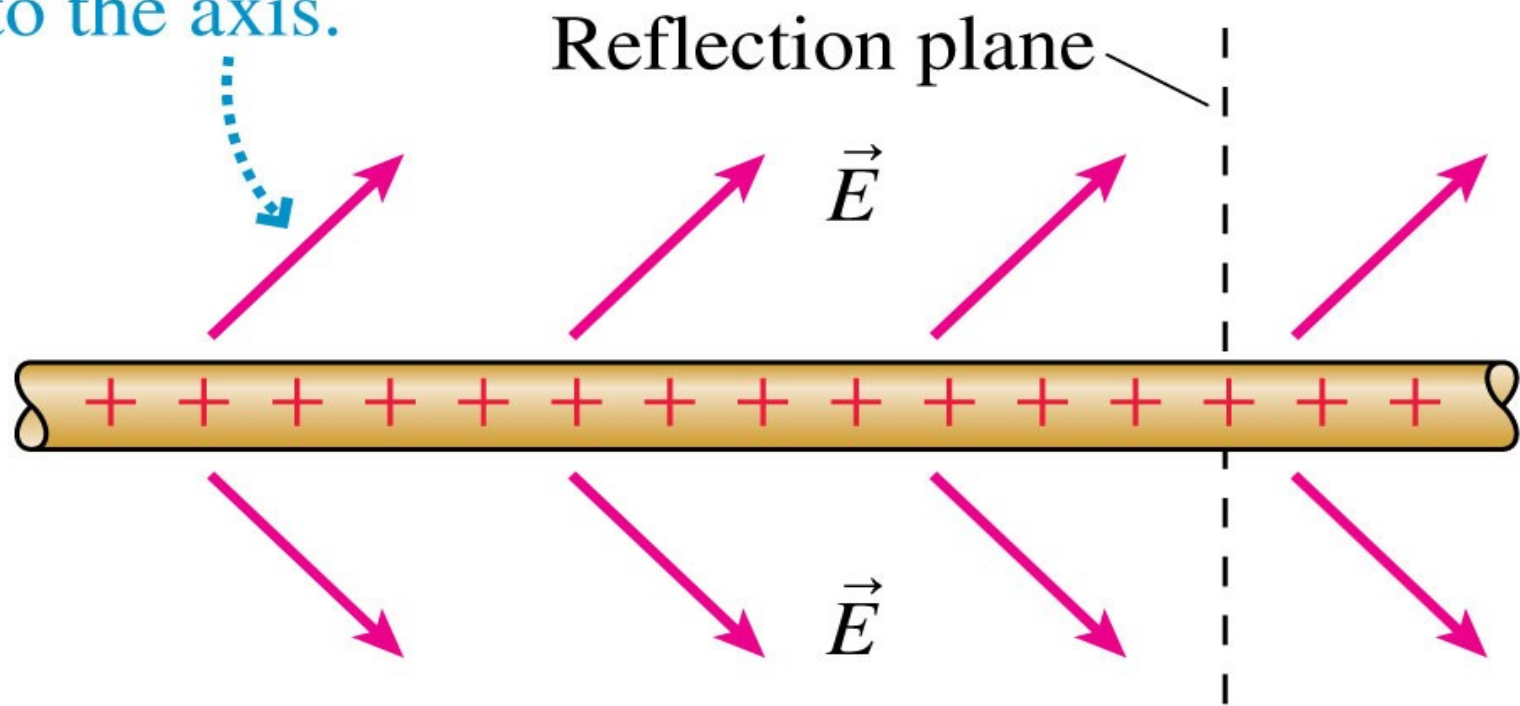
Reflection in plane containing the axis



Reflection perpendicular to the axis

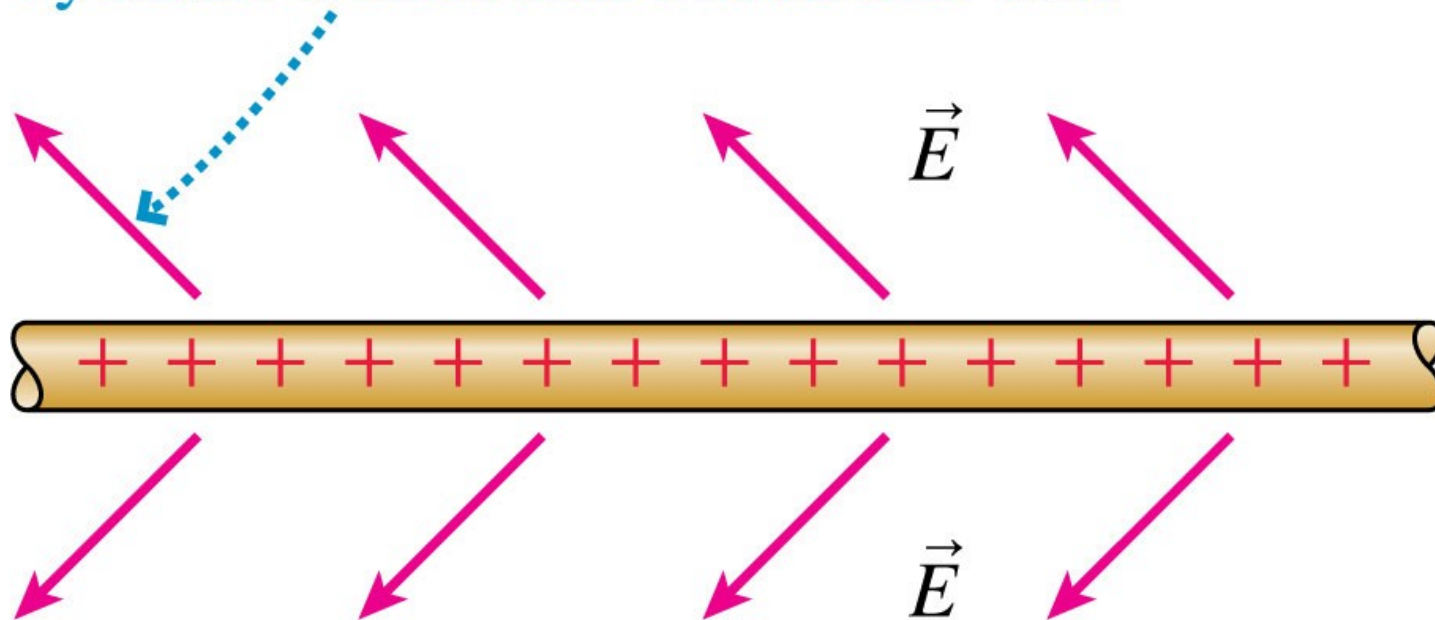
Relation between symmetry and Electric Field

- (a) Is this a possible electric field of an infinitely long charged cylinder? Suppose the charge and the field are reflected in a plane perpendicular to the axis.



Relation between symmetry and Electric Field

(b) The charge distribution is not changed by the reflection, but the field is. This field doesn't match the symmetry of the cylinder, so the cylinder's field can't look like this.

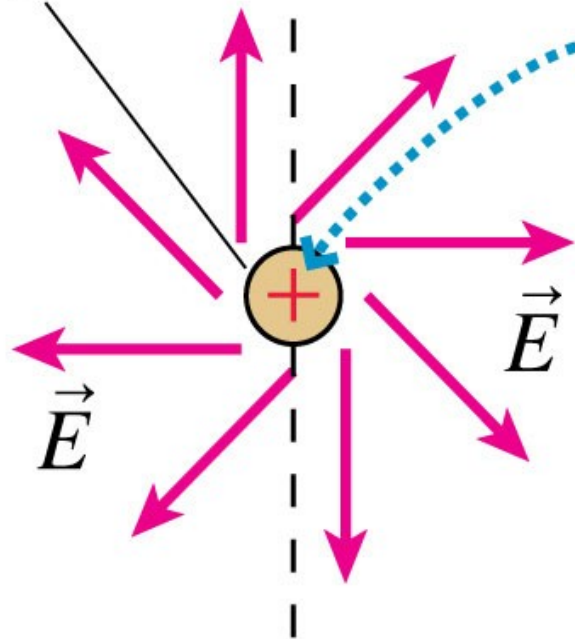


Relation between symmetry and Electric Field

(a)

End view
of cylinder

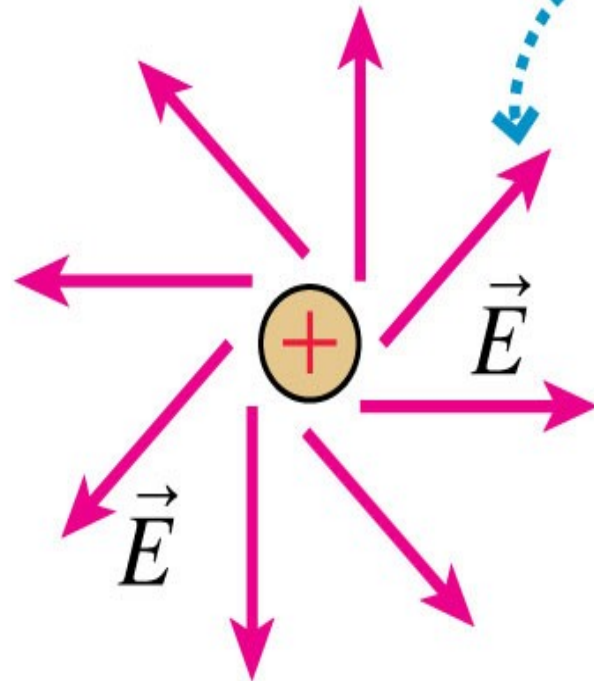
Reflection plane



The charge distribution is not changed by reflecting it in a plane containing the axis.

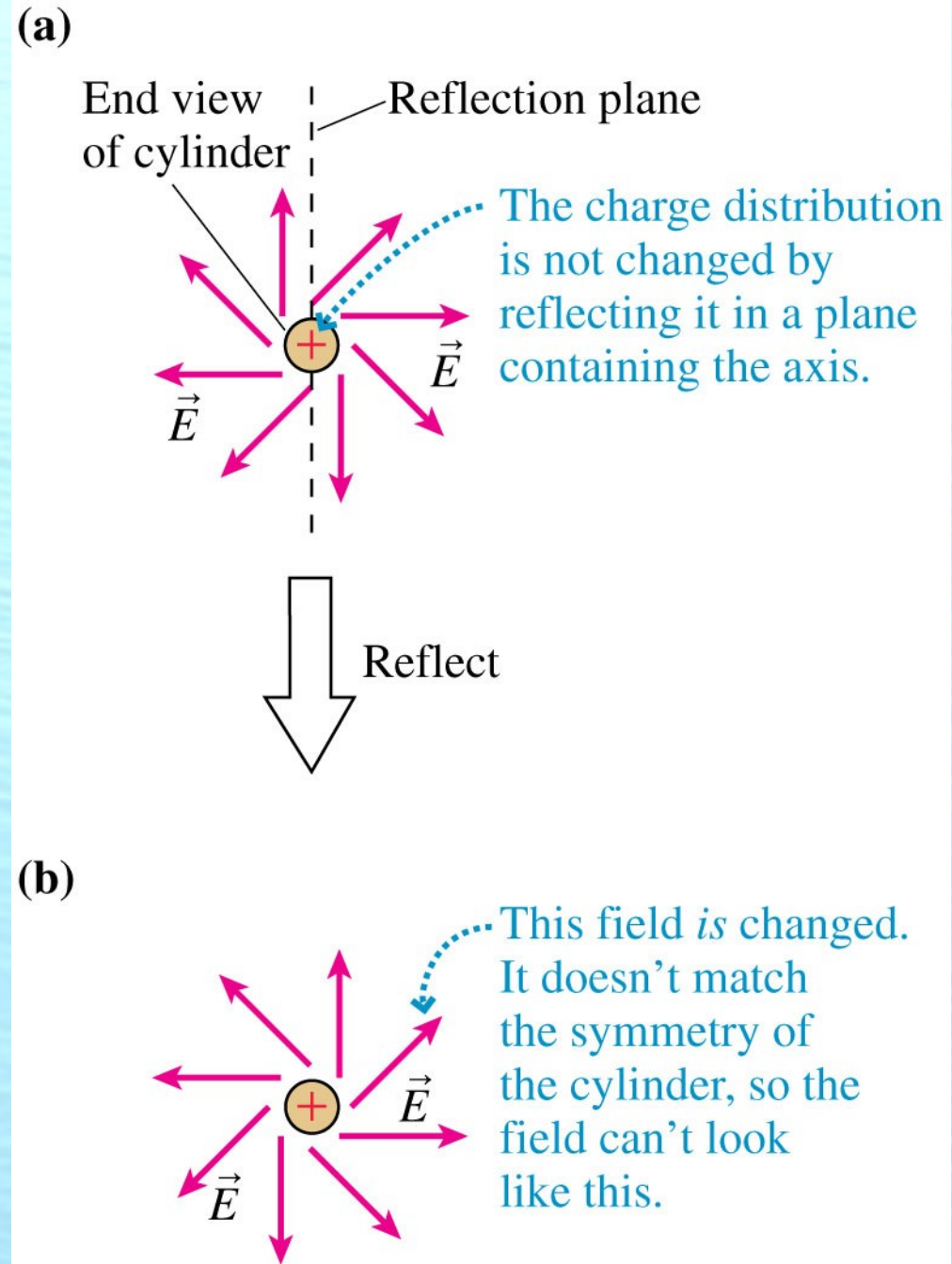
Relation between symmetry and Electric Field

(b)



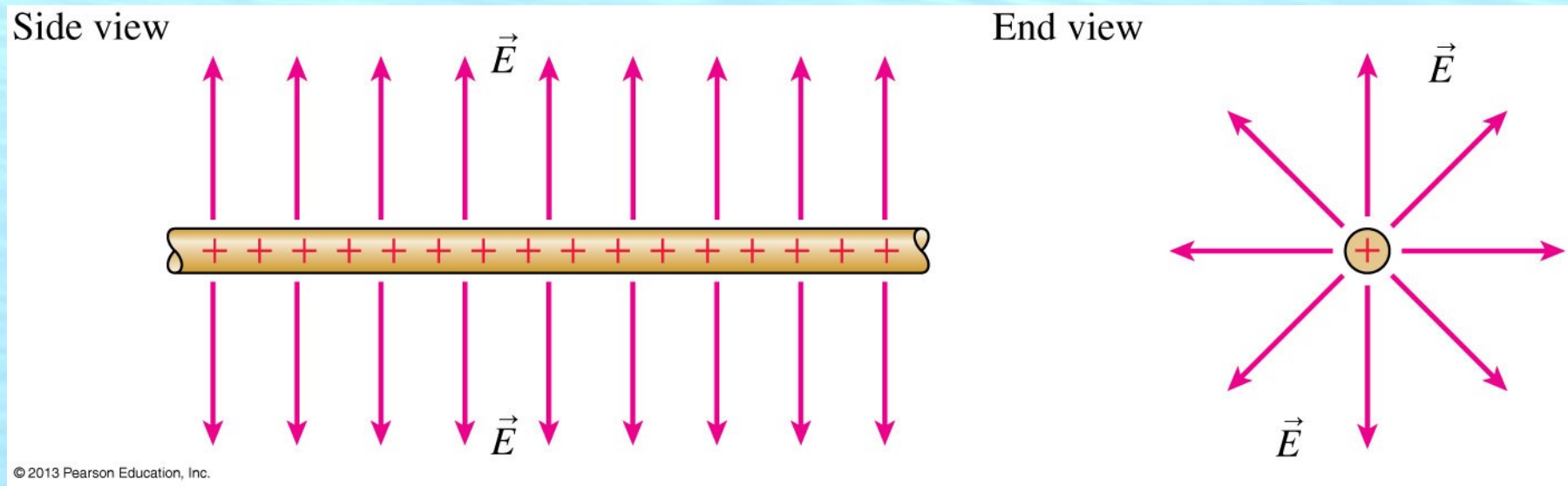
This field *is* changed. It doesn't match the symmetry of the cylinder, so the field can't look like this.

Relation between symmetry and Electric Field



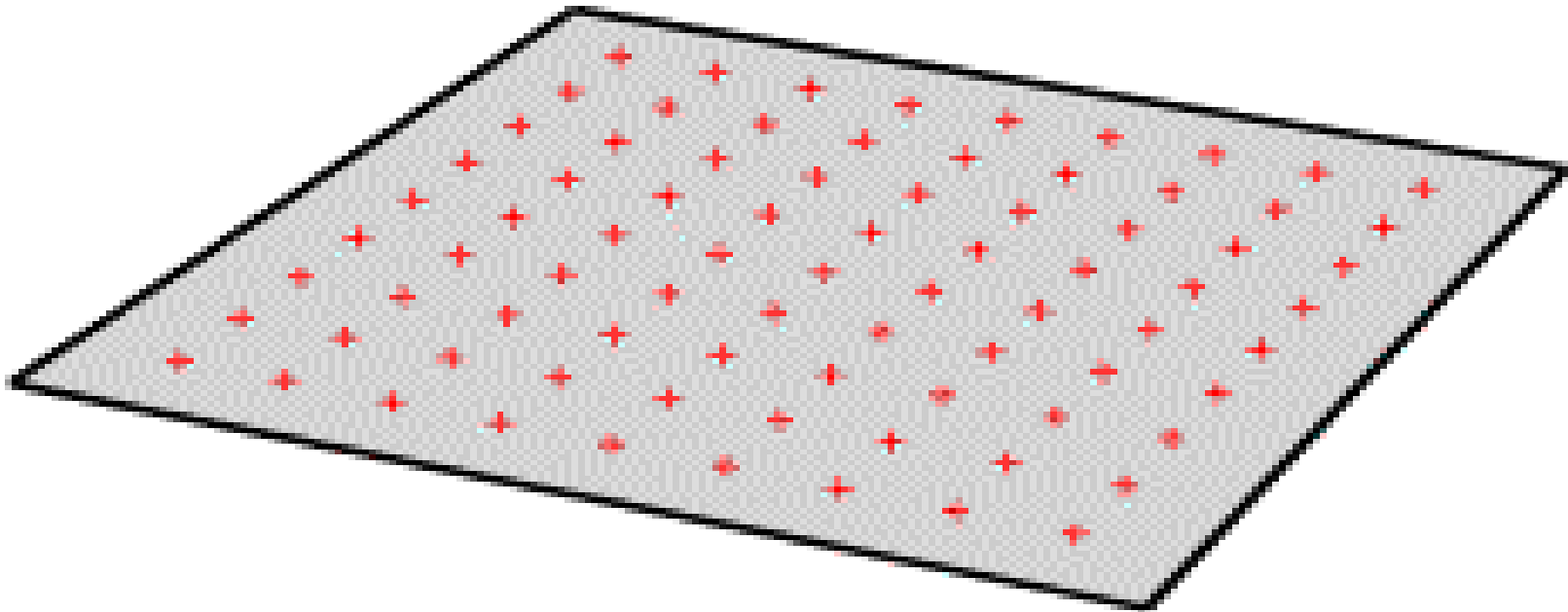
Relation between symmetry and Electric Field

The **ONLY** field consistent with symmetry of an infinitely long cylinder points radially outward.



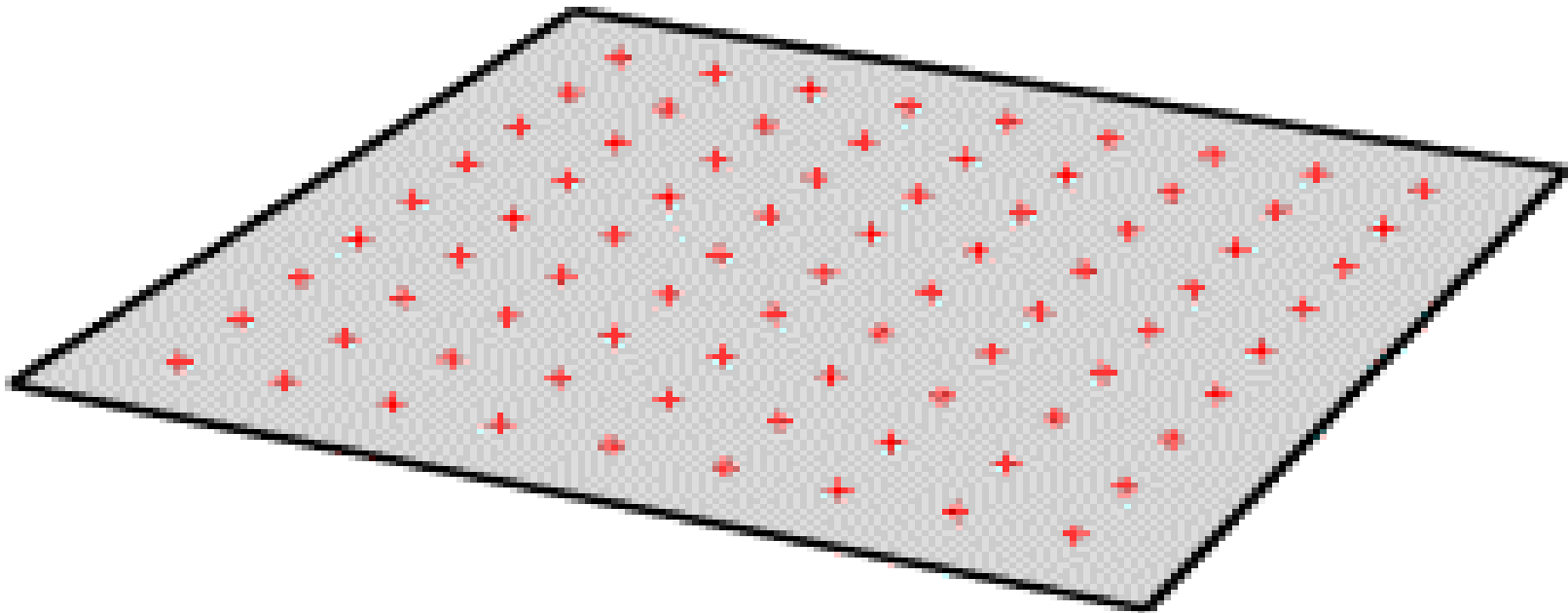
Relation between symmetry and Electric Field

Now imagine an infinite plane of charge.



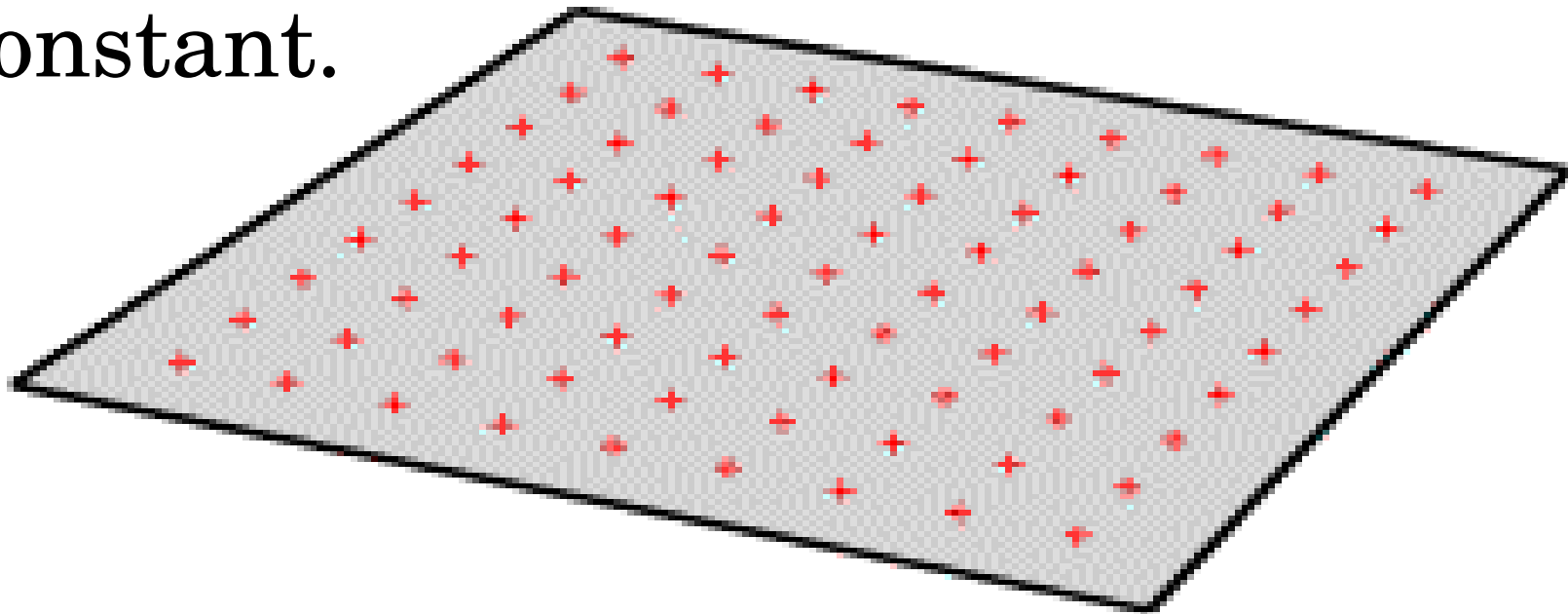
Relation between symmetry and Electric Field

Because you can't tell what direction you are facing, the field must be **ONLY** Perpendicular to the plane.



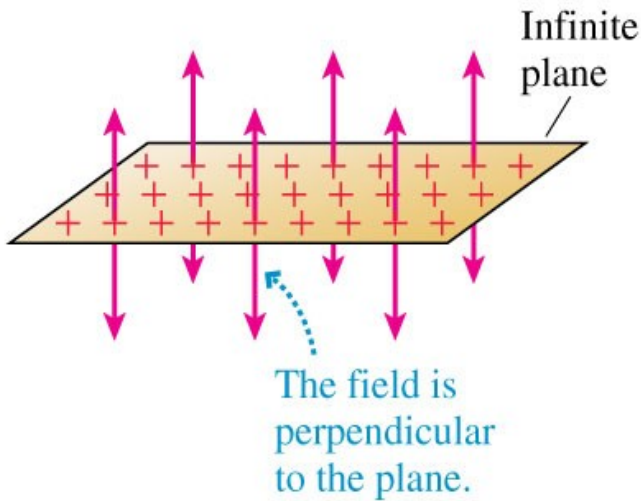
Relation between symmetry and Electric Field

Because you *ALSO* can't tell how far away you are from the plane, the field cannot change magnitude. It must be constant.



$$\vec{E} = \frac{\sigma}{2\epsilon_0} \hat{j}$$

Planar symmetry

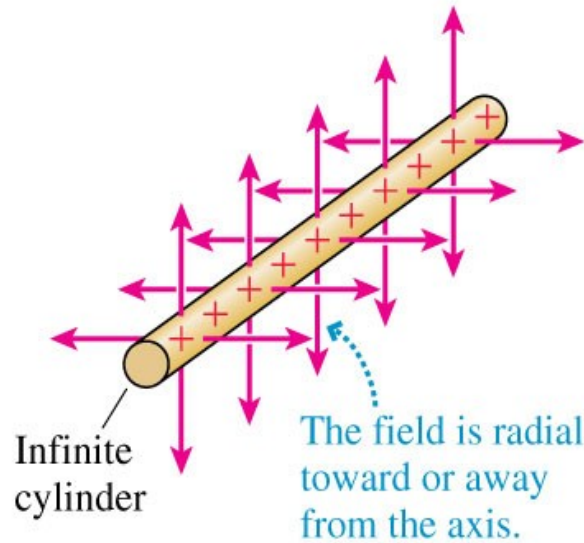


Infinite parallel-plate capacitor

$$\vec{E} = \frac{\lambda}{2\pi r \epsilon_0} \hat{r}$$

Cylindrical symmetry

$$\vec{E} = 2 \frac{k}{r} \hat{r}$$

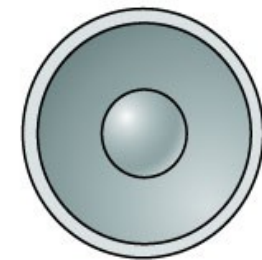
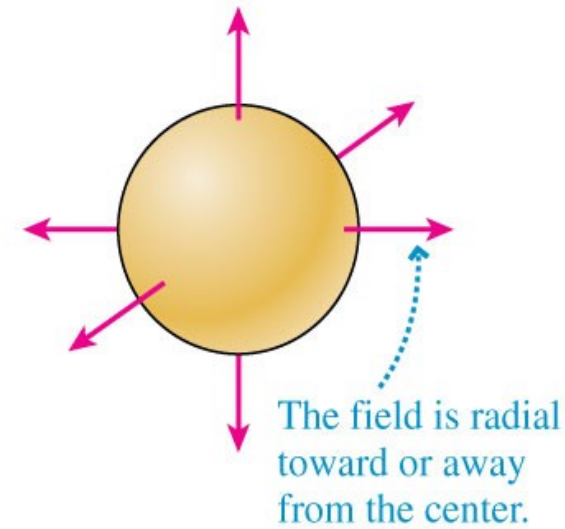


Coaxial cylinders

$$\vec{E} = \frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

Spherical symmetry

$$\vec{E} = k \frac{Q}{r^2} \hat{r}$$

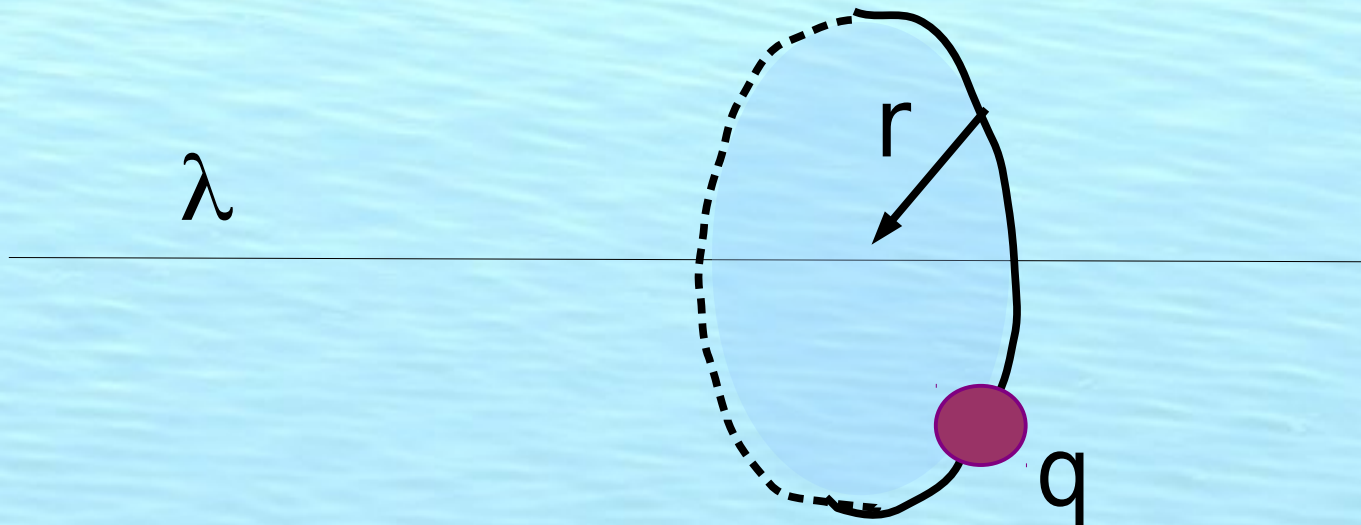


Concentric spheres

Problem

What is line charge density on a long wire if a 10 microgram particle carrying 3 nC orbits at 300 m/s?

$$\vec{E}_{\text{wire}} = 2k \frac{\lambda}{r} \hat{r} \qquad \lambda = \frac{Q}{L}$$



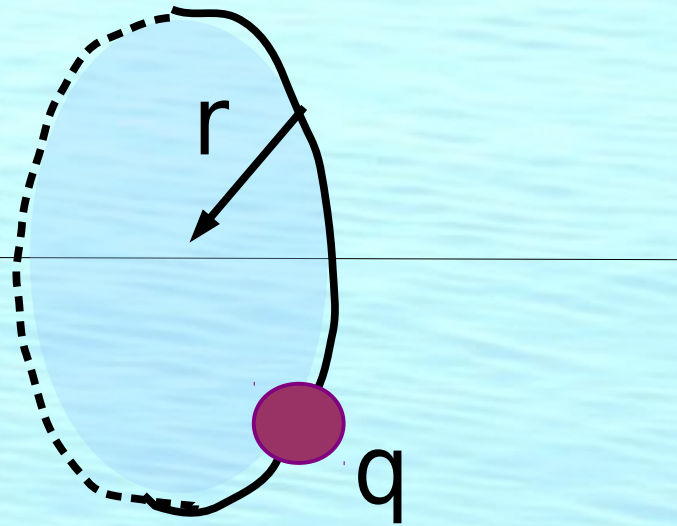
Problem

What is line charge density on a long wire if a 10 microgram particle carrying 3 nC orbits at 300 m/s?

$$\vec{E}_{\text{wire}} = 2k \frac{\lambda}{r} \hat{r}$$

λ

$$\lambda = \frac{Q}{L}$$



Clicker

You are 1 cm away from a 10 meter long charged wire, and the electric field has magnitude 27 N/C. What is the field if you go 3 cm away?

[A] 27 N/C

[B] 13.5 N/C

[C] 9 N/C

[D] 3 N/C

$$\vec{E}_{\text{PLANE}} = \frac{\sigma}{2\epsilon_0} \hat{i} \quad \vec{E}_{\text{LINE}} = \frac{\lambda}{2\pi r \epsilon_0} \hat{r} \quad \vec{E}_{\text{SPHERE}} = \frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

Clicker

You are 1 cm away from a 10 m square charged
To 2 nCoul. What is the electric field?

[A] 1.13 V/m

$$\vec{E}_{\text{PLANE}} = \frac{\sigma}{2\epsilon_0} \hat{i}$$

[B] 2.26 V/m

[C] 113 N/C

$$\vec{E}_{\text{SPHERE}} = k \frac{Q}{r^2} \hat{r} = \frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

[D] 2×10^{-9} V/m

[E] 2×10^{-11} V/m

Clicker

You are 100 m away from a 10 m square charged to 2 nCoul. What is the electric field?

[A] 1.13 V/m

$$\vec{E}_{\text{PLANE}} = \frac{\sigma}{2\epsilon_0} \hat{i}$$

[B] 1.13×10^{-2} V/m

[C] 113 V/m

$$\vec{E}_{\text{SPHERE}} = k \frac{Q}{r^2} \hat{r} = \frac{Q}{4\pi r^2 \epsilon_0} \hat{r}$$

[D] 18×10^{-2} V/m

[E] 18×10^{-4} V/m

Physics 122 – Class #15 – Outline

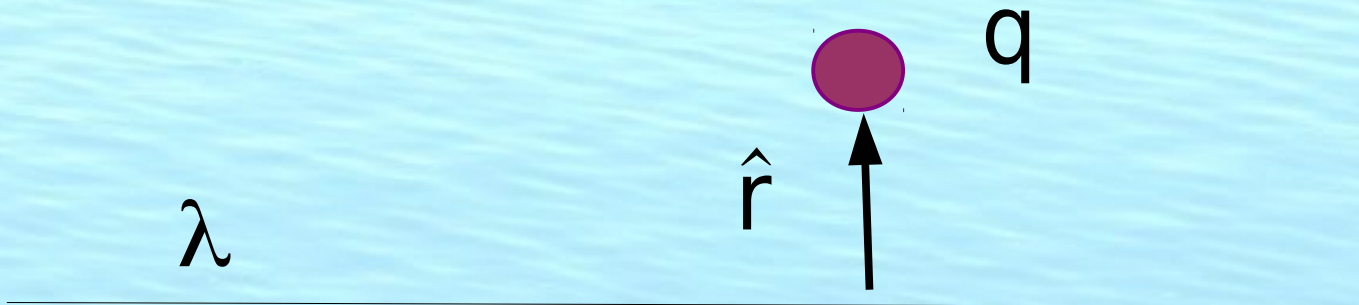
- About Exam #1 (and #2)
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Electric field of a charged wire

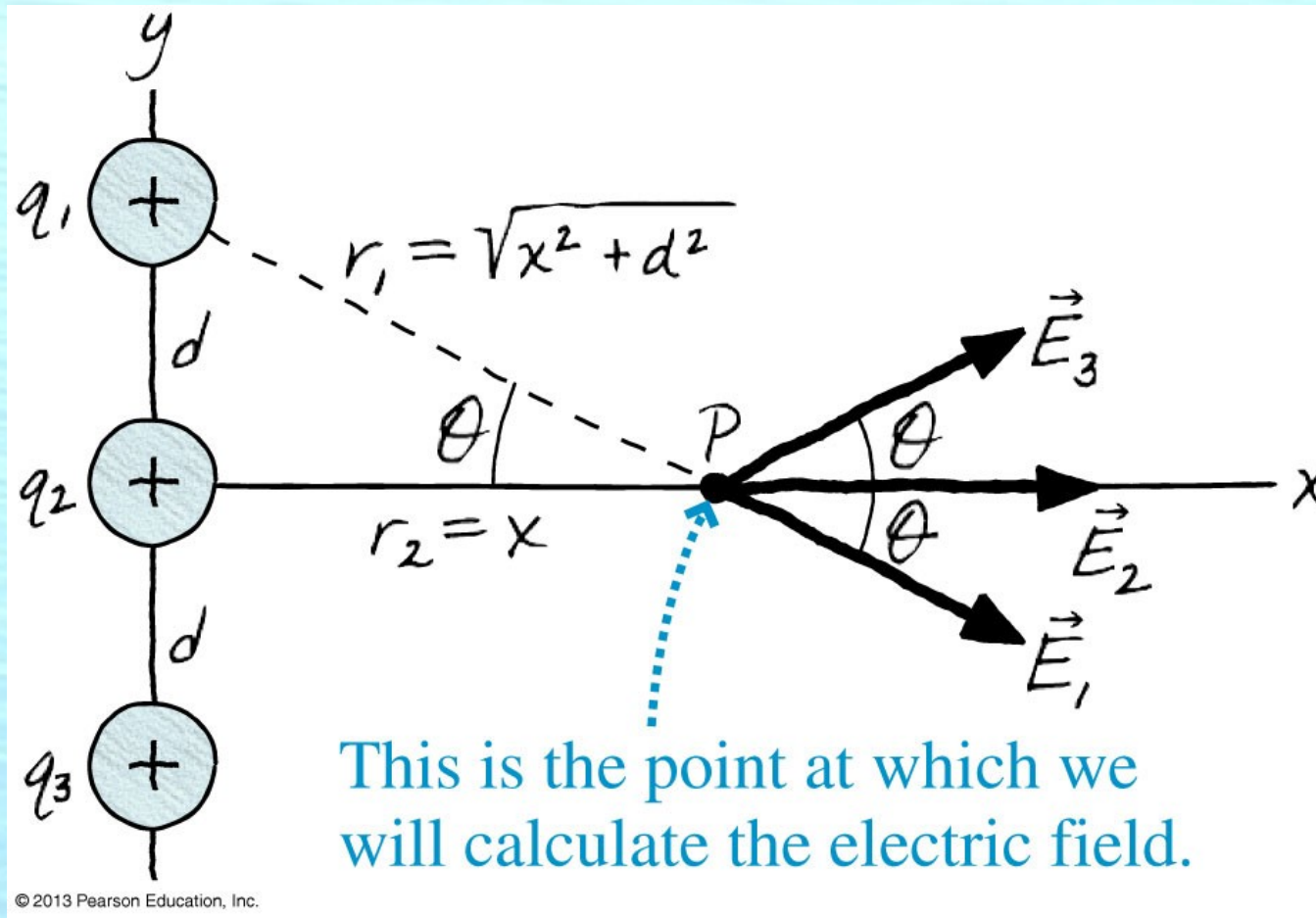
- Derivation

$$\vec{E}_{\text{wire}} = 2k \frac{\lambda}{r} \hat{r} \qquad \lambda = \frac{Q}{L}$$

$$\vec{E} = \int k \frac{dq}{r^2} \hat{r}$$



Electric field of three charges



Electric field of three charges

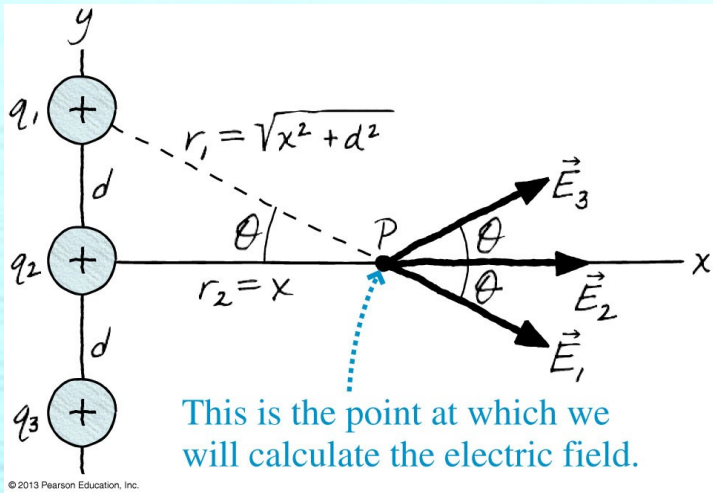
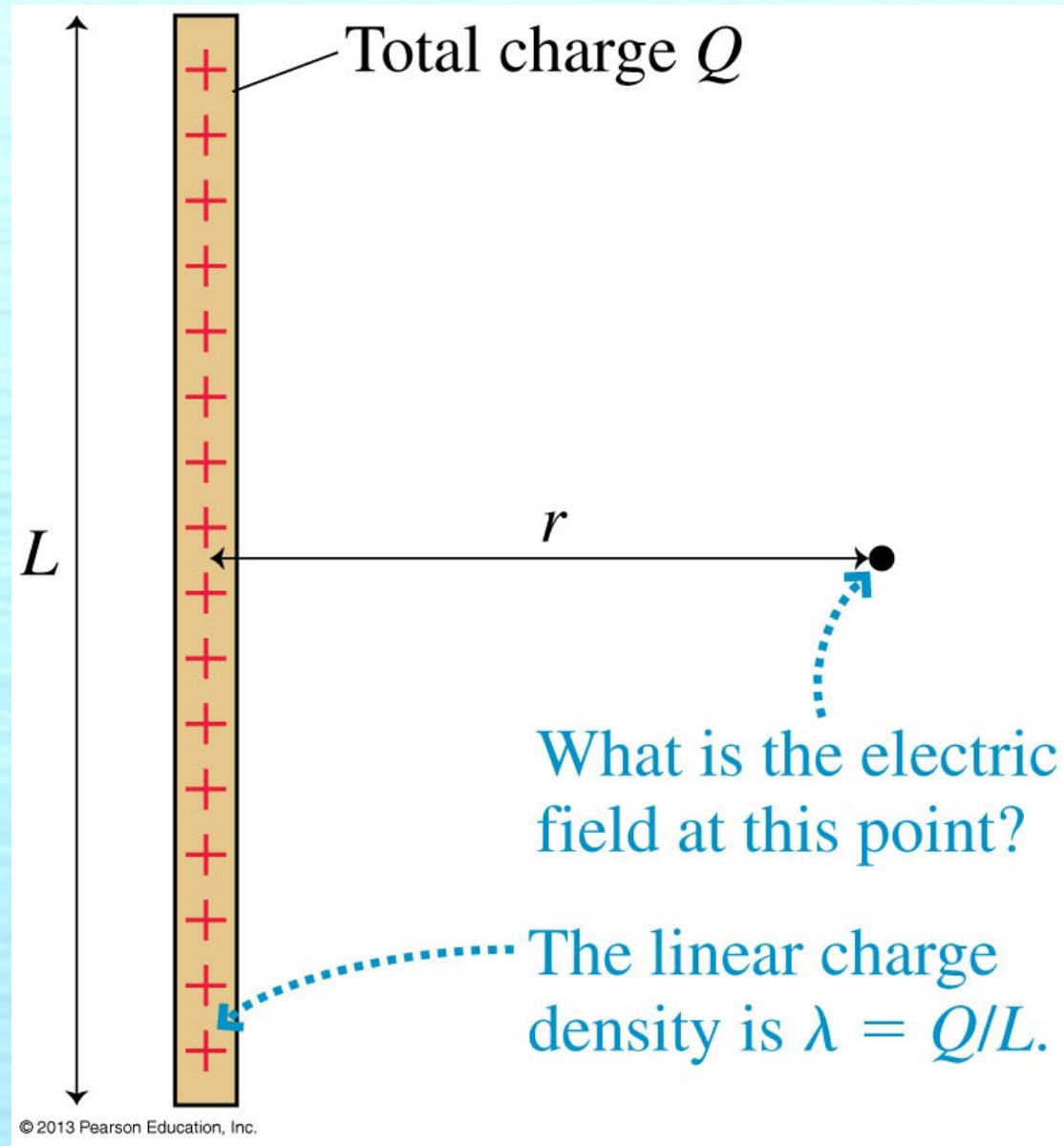


Figure 26.11

Electric field of charged wire



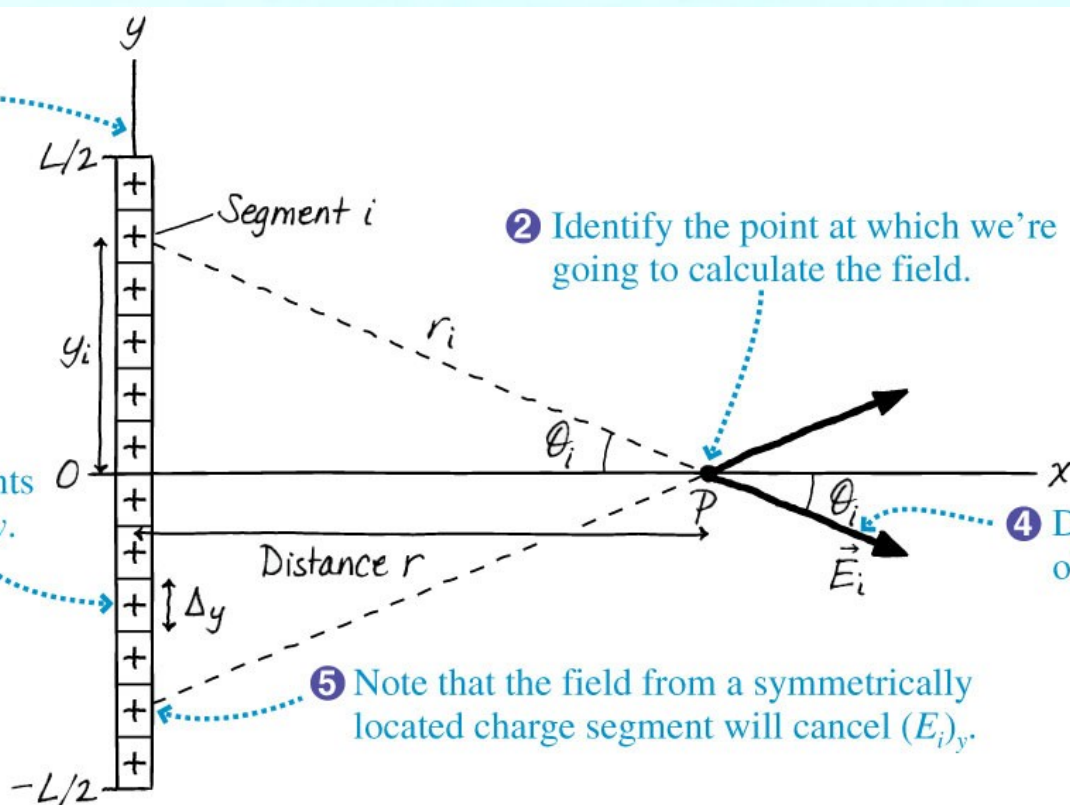
1 Choose a coordinate system with the origin at the center of the rod.

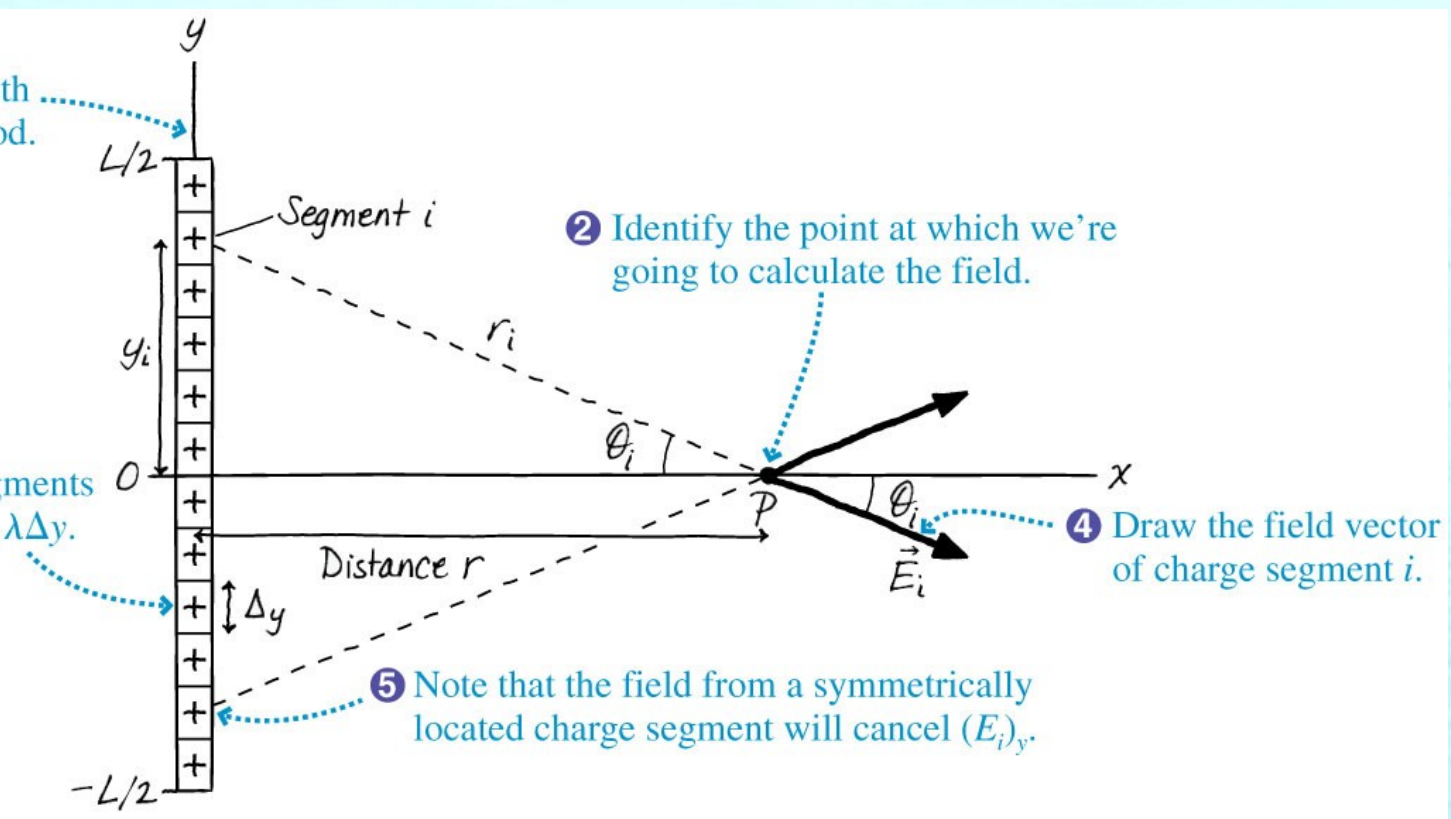
2 Identify the point at which we're going to calculate the field.

3 Divide the rod into N small segments of length Δy and charge $\Delta Q = \lambda \Delta y$.

4 Draw the field vector of charge segment i .

5 Note that the field from a symmetrically located charge segment will cancel $(E_i)_y$.





Electric field of a charged wire