

$$y = 2.25t^2$$

$$y = y_0 + v_{y0}t + \frac{1}{2}a_y t^2$$

compare these two, we get

$$\frac{1}{2}a_y = 2.25, \quad y_0 = 0$$

$$a_y = 4.50 \text{ m/s}^2 \quad v_{y0} = 0$$

$$v_y = v_{y0} + a_y t \quad \rightarrow \quad \text{at } t = 2.1 \text{ s,}$$

$$v_y = a_y t \quad v_y = (4.5 \frac{\text{m}}{\text{s}^2})(2.1 \text{ s})$$

$$= 9.5 \text{ m/s}$$

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Alternative solution

$$v_y = \frac{dy}{dt} = \frac{d}{dt} (2.25t^2)$$

$$= 4.5t$$

$$\text{At } t = 2.1 \text{ s, } v_y = (4.5 \frac{\text{m}}{\text{s}^2})(2.1 \text{ s})$$

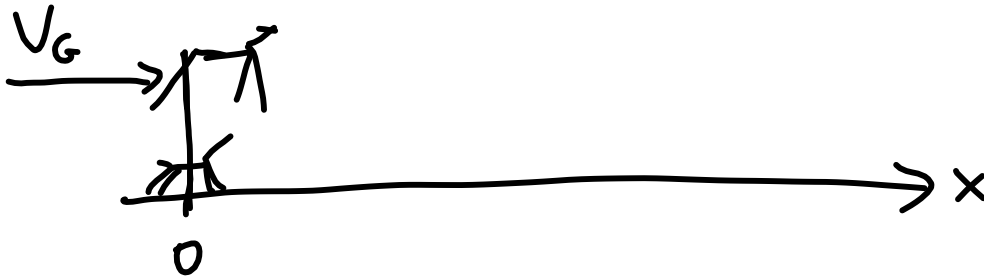
$$= 9.5 \text{ m/s}$$

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Example 3.13, cheetah & gazelle

Let X_c = position of cheetah (V_c, a_c)

X_G = " " gazelle (V_G, a_G)



$V_G = \text{constant} = 10 \text{ m/s}$. $a_G = 0$

$X_{c0} = 0$

$V_{c0} = 0$

$X_{G0} = 0$

$a_c = 4 \text{ m/s}^2$

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$$X_G = X_{G0}^0 + V_{G0}t + \frac{1}{2}a_G t^2$$

$$X_c = X_{c0}^0 + V_{c0}t^0 + \frac{1}{2}a_c t^2$$

put in our values, (zeros)

$$X_G = V_G t$$

$$X_c = \frac{1}{2}a_c t^2$$

at what time
does $X_G = X_c$?

$$V_G t = \frac{1}{2}a_c t^2$$

$$t = \frac{2 V_G}{a_c}$$

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Gravitational Force

$$F = \underset{\substack{\uparrow \\ \text{const.}}}{G} \frac{Mm}{r^2}$$



But $F = ma$

Set equal, $\cancel{m}a = G \frac{M\cancel{m}}{r^2}$

near Earth's
surface

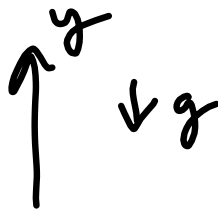
$$a = G \frac{M}{r^2} \approx \text{const.}$$

$\longrightarrow a = g = 9.8 \text{ m/s}^2$

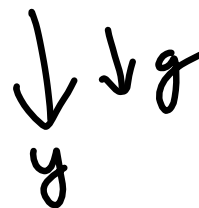
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For free fall, use equations of motion, and substitute for a

i) $a = -g$ if $+y$ is upward from surface

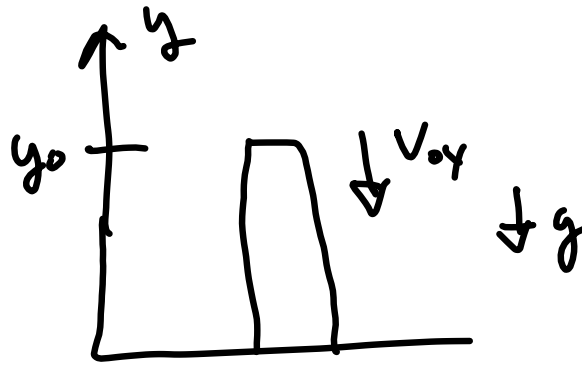


ii) $a = g$ if $+y$ is downward



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Ex 3.14



$$y = y_0 + v_{oy}t + \frac{1}{2}a_y t^2 \quad \text{where } a_y = -g$$

$$y = y_0 + v_{oy}t - \frac{1}{2}gt^2$$

when ball hits ground, $y = 0$

$$0 = y_0 + v_{oy}t - \frac{1}{2}gt^2 \quad \left. \vphantom{0 = y_0 + v_{oy}t - \frac{1}{2}gt^2} \right\} \begin{array}{l} \text{use quadratic equation} \\ \text{(use only one root!)} \end{array}$$

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