

Name: _____

ID #: _____

Physics 221 - Fall 2019
★ Homework ★
Chapter 1

1) **Two vectors are given by: $\mathbf{A} = 1\hat{x} + 4\hat{y} - 6\hat{z}$ and $\mathbf{B} = 4\hat{x} - 1\hat{y} + 2\hat{z}$. Evaluate:**

- a) $|\mathbf{A}| \equiv A$
- b) $|\mathbf{B}| \equiv B$
- c) $\mathbf{A} \cdot \mathbf{B}$
- d) θ_b (the angle between these two vectors)
- e) $\mathbf{A} \times \mathbf{B}$

2) **Calculate the partial derivatives with respect to x , y , and z , of the function:**

$$f(x, y, z) = 3y^2 \cos(x) + z$$

3) $\mathbf{Z} = 5 + 4i$.

a) Calculate $Z \times Z$. *Note: Regular multiplication of Z with itself — your answer should be a complex number.*

b) Calculate $(Z^*Z)^{1/2}$. *Note: Absolute square — your answer should be a real number.*

4) **Demonstrate that Euler's equation ($e^{ix} = \cos x + i \sin x$) is correct by taking the (regular) derivative of the following function, $f(x)$, and deducing the consequences.**

Hint: remember i is just a constant.

$$f(x) = e^{-ix}(\cos x + i \sin x)$$

- 5) **1.2**
- 6) **1.4**
- 7) **1.5**
- 8) **1.6**
- 9) **1.7**
- 10) **1.9**
- 11) **1.10**
- 12) **1.11**
- 13) **1.13**
- 14) **1.14**
- 15) **1.15**